

# STRUCTURED CONCURRENCY LUCIAN RADU TEODORESCU



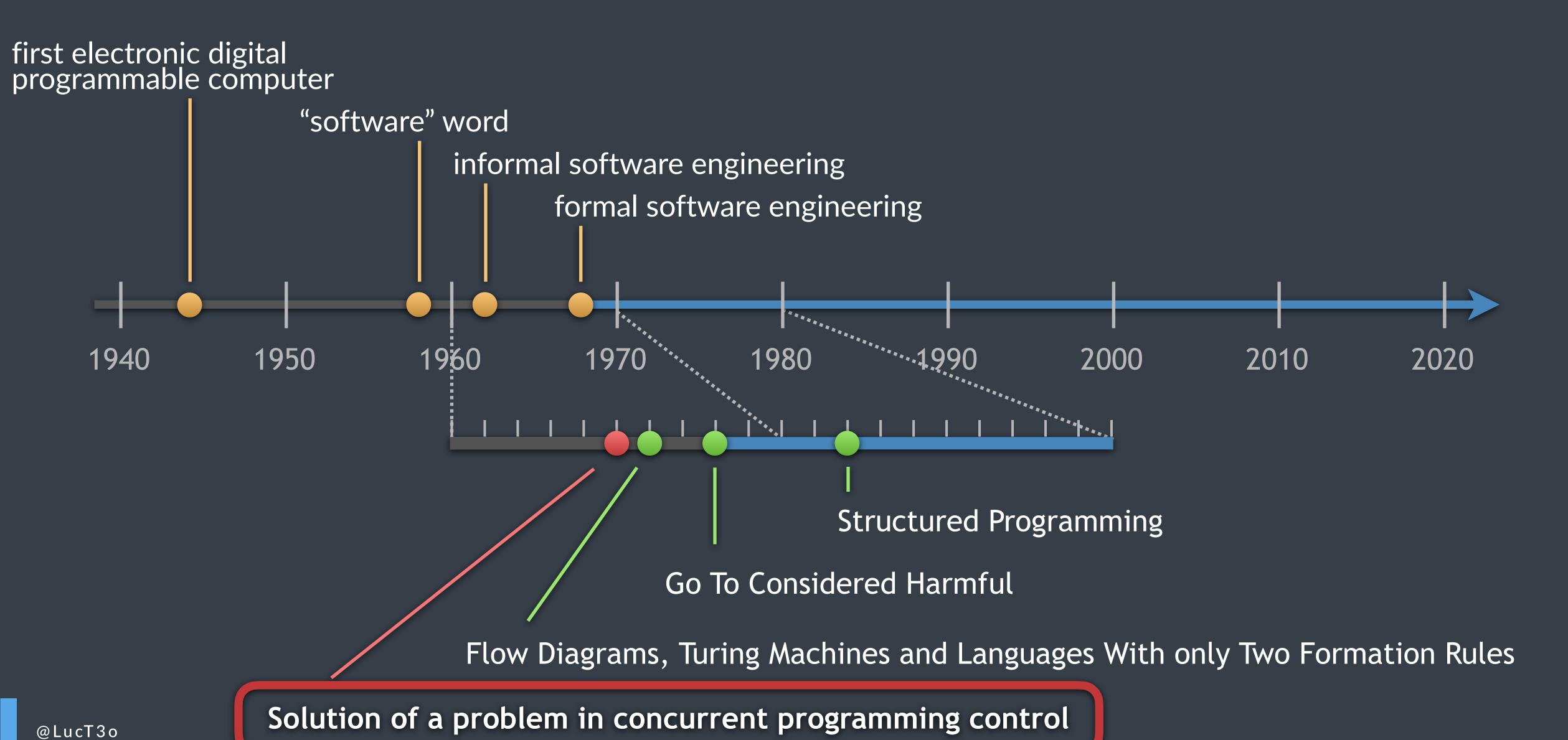


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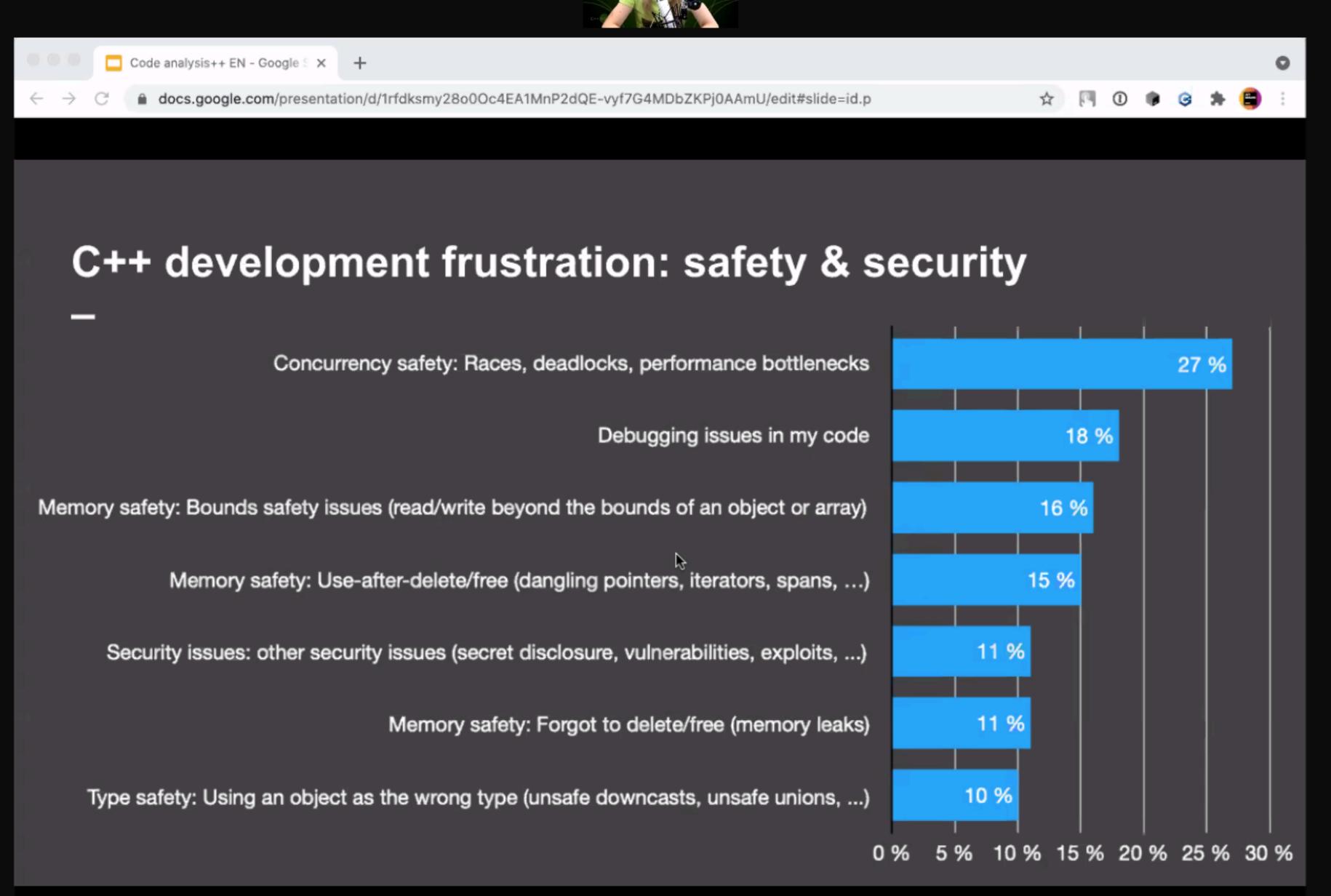
#### a tale of two problems

complexity concurrency

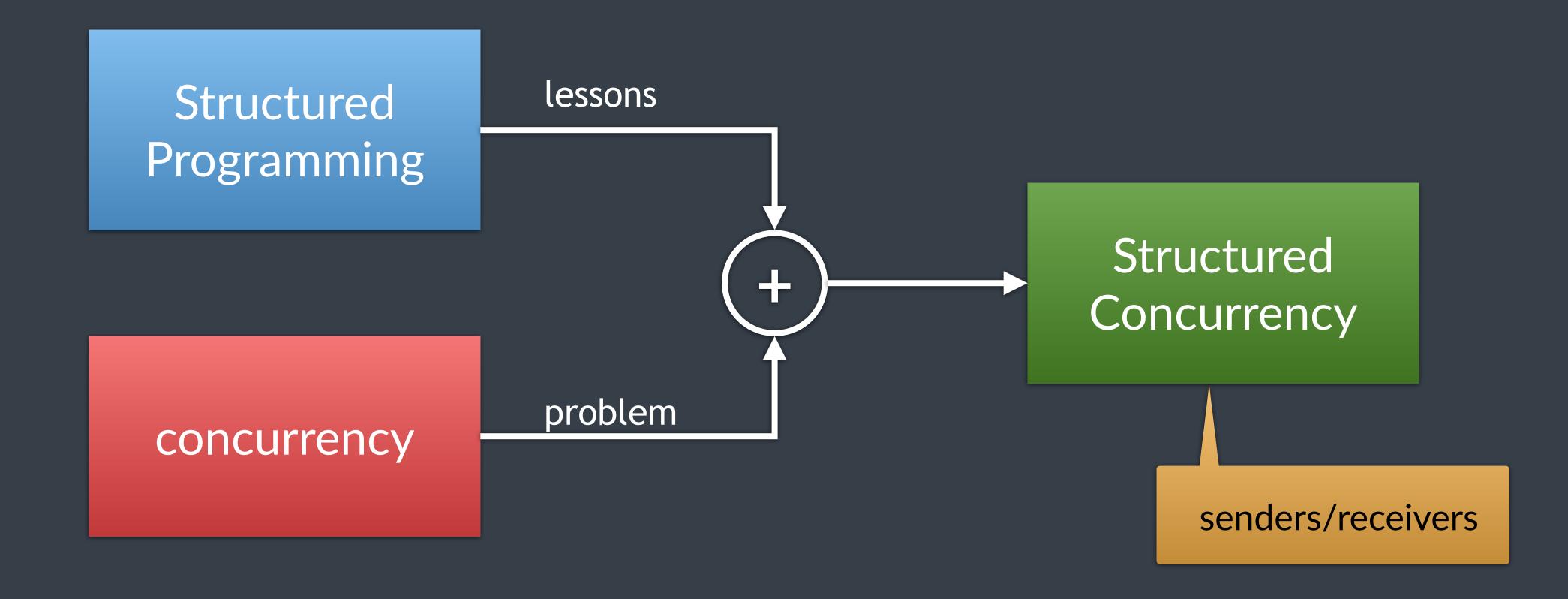
#### relevant timeline







#### this talk



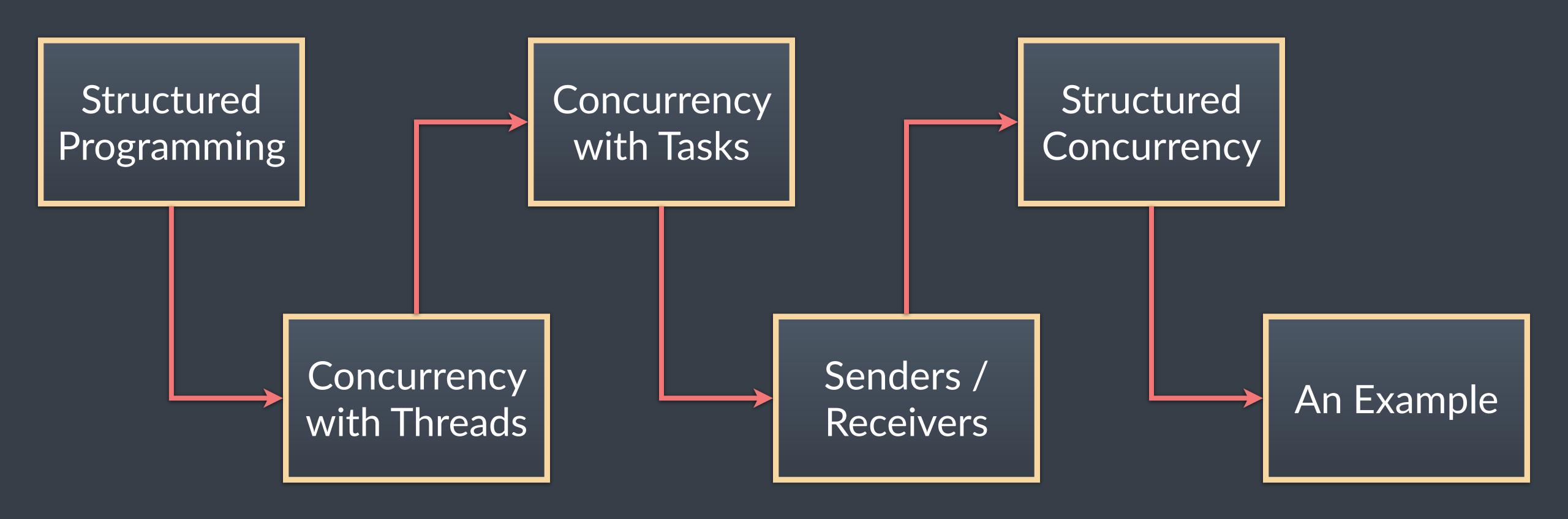
#### what to expect

general picture the why

#### what NOT to expect

introduction to senders/receivers deep dive into details

#### Agenda



## Structured Programming



#### Computational Linguistics

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D. G. BOBROW, Editor

#### Flow Diagrams, Turing Machines And Languages With Only Two Formation Rules

Corrado Böhm and Giuseppe Jacopini International Computation Centre and Istituto Nazionale per le Applicazioni del Calcolo, Roma, Italy

In the first part of the paper, flow diagrams are introduced to represent inter al. mappings of a set into itself. Although not every diagram is decomposable into a finite number of given base diagrams, this becomes true at a semantical level due to a suitable extension of the given set and of the basic mappings defined in it. Two normalization methods of flow diagrams are given. The first has three base diagrams; the second, only two.

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#### 1. Introduction and Summary

The set of block or flow diagrams is a two-dimensional programming language, which was used at the beginning of automatic computing and which now still enjoys a certain favor. As far as is known, a systematic theory of this language does not exist. At the most, there are some papers by Peter [1], Gorn [2], Hermes [3], Ciampa [4], Riguet [5], Ianov [6], Asser [7], where flow diagrams are introduced with different purposes and defined in connection with the descriptions of algorithms or programs.

This paper was presented as an invited talk at the 1964 International Colloquium on Algebraic Linguistics and Automata Theory, Jerusalem, Israel. Preparation of the manuscript was supported by National Science Foundation Grant GP-2880.

This work was carried out at the Istituto Nazionale per le Applicazioni del Calcolo (INAC) in collaboration with the International Computation Centre (ICC), under the Italian Consiglio Nazionale delle Ricerche (CNR) Research Group No. 22

Communications of the ACM

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#### 2. Normalization of Flow Diagrams

It is a well-known fact that a flow daigram is suitable for representing programs, computers, Turing machines, etc. Diagrams are usually composed of boxes mutually connected by oriented lines. The boxes are of functional

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Edgar Dijkstra: Go To Statement Considered Harmful

#### Go To Statement Considered Harmful

Key Words and Phrases: go to statement, jump instruction, branch instruction, conditional clause, alternative clause, repetitive clause, program intelligibility, program sequencing CR Categories: 4.22, 5.23, 5.24

#### EDITOR:

For a number of years I have been familiar with the observation that the quality of programmers is a decreasing function of the density of go to statements in the programs they produce. More recently I discovered why the use of the go to statement has such disastrous effects, and I became convinced that the go to statement should be abolished from all "higher level" programming languages (i.e. everything except, perhaps, plain machine code). At that time I did not attach too much importance to this discovery; I now submit my considerations for publication because in very recent discussions in which the subject turned up. I have been urged to do so.

My first remark is that, although the programmer's activity ends when he has constructed a correct program, the process taking place under control of his program is the true subject matter of his activity, for it is this process that has to accomplish the desired effect; it is this process that in its dynamic behavior has to satisfy the desired specifications. Yet, once the program has been made, the "making" of the corresponding process is delegated to the machine.

dynamic progress is only characterized when we also give to which call of the procedure we refer. With the inclusion of procedures we can characterize the progress of the process via a sequence of textual indices, the length of this sequence being equal to the dynamic depth of procedure calling.

Let us now consider repetition clauses (like, while B repeat A or repeat A until B). Logically speaking, such clauses are now superfluous, because we can express repetition with the aid of recursive procedures. For reasons of realism I don't wish to exclude them: on the one hand, repetition clauses can be implemented quite comfortably with present day finite equipment; on the other hand, the reasoning pattern known as "induction" makes us well equipped to retain our intellectual grasp on the processes generated by repetition clauses. With the inclusion of the repetition clauses textual indices are no longer sufficient to describe the dynamic progress of the process. With each entry into a repetition clause, however, we can associate a so-called "dynamic index," inexorably counting the ordinal number of the corresponding current repetition. As repetition clauses (just as procedure calls) may be applied nestedly, we find that now the progress of the process can always be uniquely characterized by a (mixed) sequence of textual and/or dynamic indices.

The main point is that the values of these indices are outside programmer's control; they are generated (either by the write-up of his program or by the dynamic evolution of the process) whether

APIC Studies in Data Processing No. 8

#### 

O.-J. Dahl, E. W. Dijkstra and C. A. R. Hoare

**Academic Press** London New York San Francisco

A Subsidiary of Harcourt Brace Jovanovich, Publishers



@LucT3o

## what is Structured Programming?

- 1. abstractions as building blocks
- 2. recursive decomposition
- 3. local reasoning
- 4. single entry, single exit point
- 5. soundness and completeness

#### 1. abstractions as building blocks





### example: variable

keep: type, single value

drop: the current value

```
int i = 0;
while ( a[i] <= 10 )
    i++;
print(i);</pre>
```

#### example: function

**keep**: signature, entry/exit semantics, main idea **drop**: implementation details

#### example: function

**keep**: signature, entry/exit semantics, main idea **drop**: implementation details

name: summarisation of semantics



## Plato's man: featherless biped



### abstraction helps our mind

focus on essential

### in Structured Programming

functions data structures

## 2. recursive decomposition

divide et impera

#### building programs

recursively decompose programs into parts make one decision at a time (local context) later decisions don't influence prev. decisions

successive refinement

#### example

print the first 1000 prime numbers

```
auto main() -> int {
    print_first_1000_prime_numbers();
    return 0;
}
```

```
auto print_first_1000_prime_numbers() -> void {
    // TODO: define array p of 1000 elements
    // TODO: fill array p with first 1000 prime numbers
    // TODO: print array p
}
```

## step 2 (refinement)

```
auto print_first_1000_prime_numbers() -> void {
   int p[1000];
   fill_with_first_1000_prime_numbers(p);
   print_array(p);
}
```

```
auto fill_with_first_1000_prime_numbers(int* p) -> void {
    int num_primes = 0;
    int val = 1;
    while (num_primes < 1000) {
        // TODO: increase val until next prime number
        p[num_primes++] = val;
    }
}</pre>
```

```
auto fill_with_first_1000_prime_numbers(int* p) -> void {
   int num_primes = 0;
   int val = 1;
   while (num_primes < 1000) {
        do {
            val++; // WARNING: inefficient
        } while (!is_prime(val, p, num_primes));
        p[num_primes++] = val;
   }
}</pre>
```

## step 5 (revision)

```
auto fill_with_first_1000_prime_numbers(int* p) -> void {
    p[0] = 2;
    int num_primes = 1;
    int val = 1;
    while (num_primes < 1000) {
        do {
            val += 2;
        } while (!is_prime(val, p, num_primes));
        p[num_primes++] = val;
    }
}</pre>
```

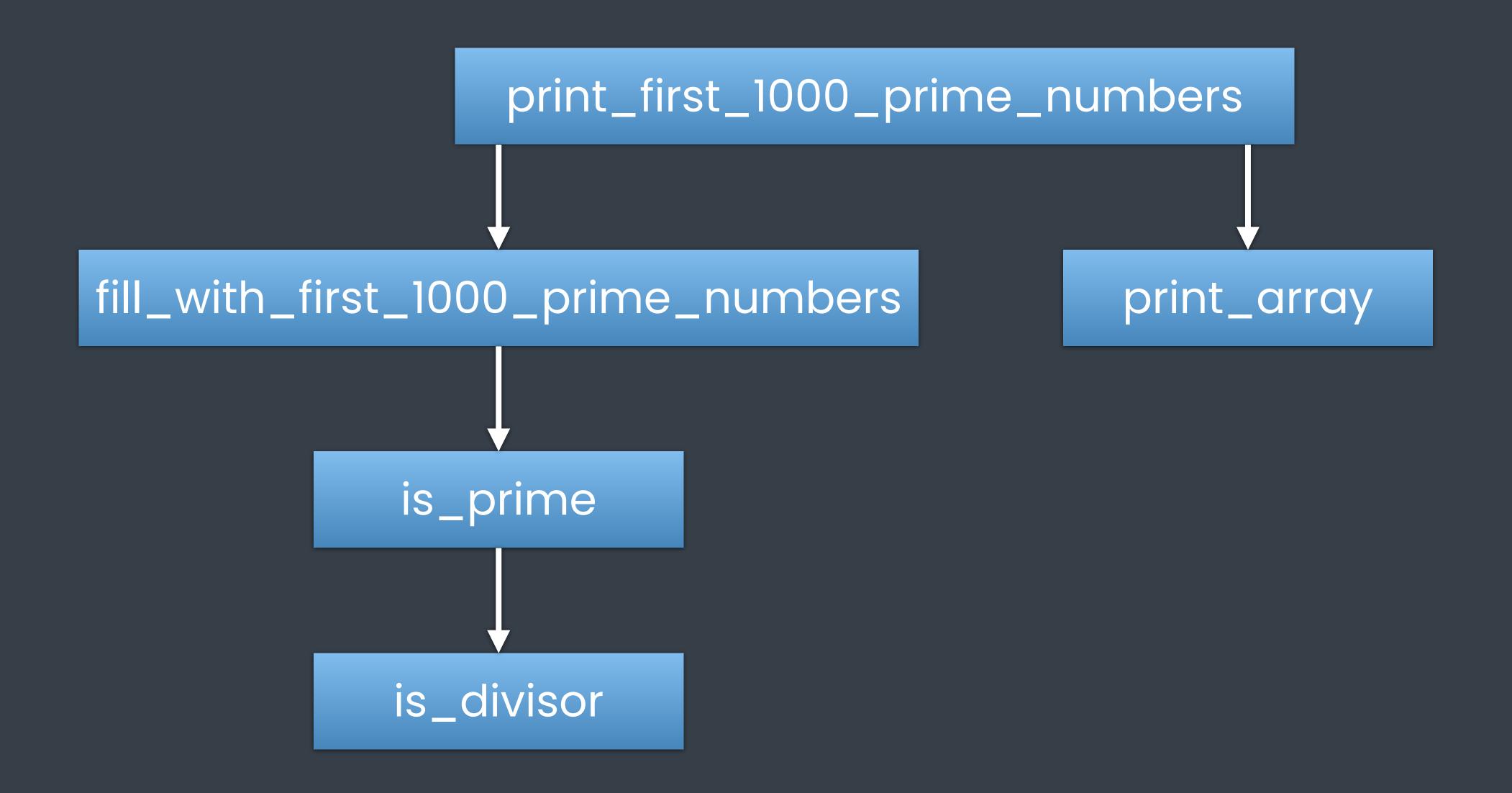
```
auto is_prime(int val, int* p, int num_primes) -> bool {
    // TODO: for all previously found primes, starting with 3, up until sqrt(val)
    // ... check if there is a divisor of val
}
```

## step 7 (refinement)

```
auto is_prime(int val, int* p, int num_primes) -> bool {
   bool val_is_prime = true;
   for (int i = 1; i < num_primes && p[i] * p[i] <= val && val_is_prime; i++) {
      val_is_prime = !is_divisor(p[i], val);
   }
   return val_is_prime;
}</pre>
```

```
auto is_divisor(int div, int val) -> bool {
    return (val % div) == 0;
}
```

```
auto print_array(int* p) -> void {
    for (int i = 0; i < 1000; i++)
        printf("%d\n", p[i]);
}</pre>
```



## 3. local reasoning

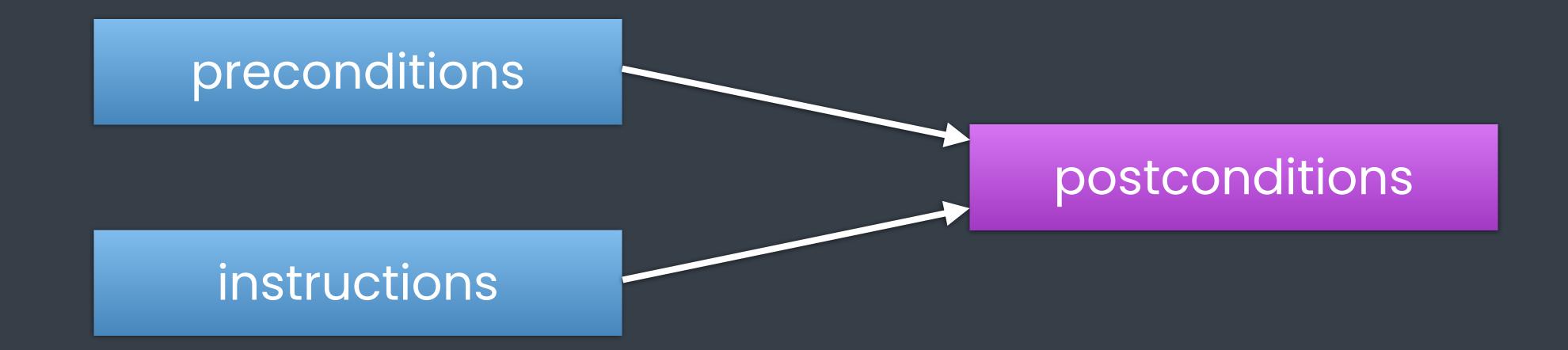
nested scopes encapsulation of local concerns

#### small example

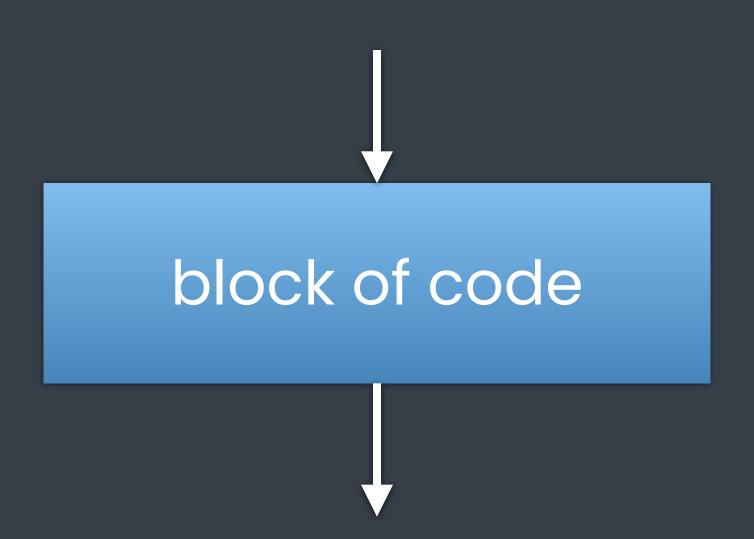
```
for (int i=0; i<10; i++) {
    int x = i;
    {
        for (int i=0; i<10; i++) {
            int y = i;
            printf("%d/%d\n", x, y);
        }
    }
}</pre>
```

#### focus

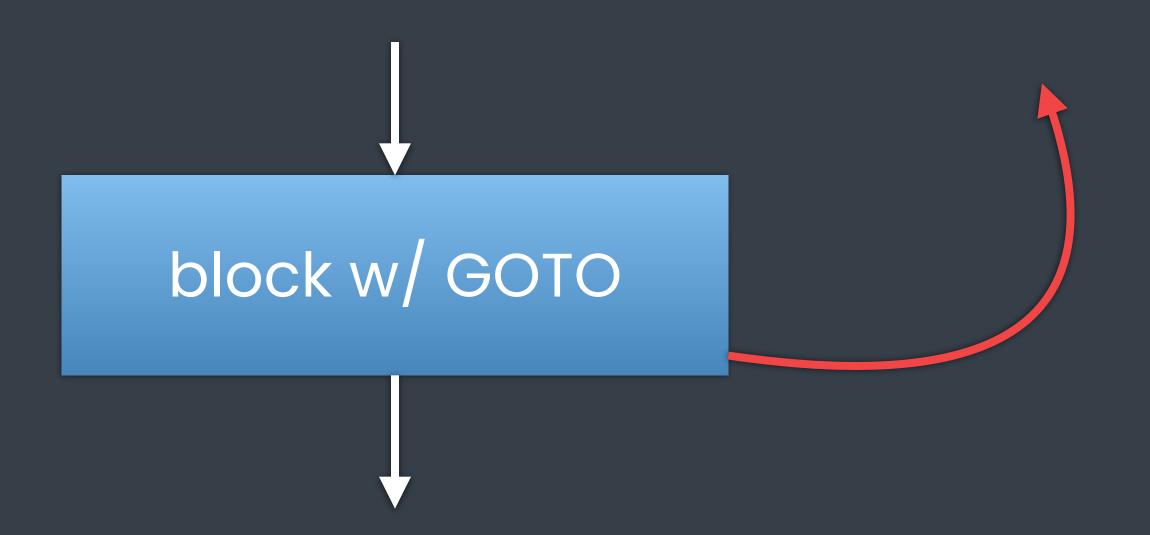
one thing at a time



## 4. single entry, single exit point



#### GOTO excluded



#### reasons?

linear reasoning code & execution have the same flow

## same shape

instruction
function call
block of code
alternatives
loops

#### exit in C++

return a value
throw an exception
abort (internal or external)

```
auto sum(Matrix a, Matrix b) -> Matrix;

Matrix a = ...;
Matrix b = ...;
Matrix c = sum(a, b);
```

## 5. soundness and completeness

can Structured Programming be applied?

#### soundness

applying SP should lead to correct programs

## completeness

applying SP for all programs

## Böhm-Jacopini theorem

#### **Computational Linguistics**

D. G. BOBROW, Editor

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## Structured Programming

- 1. abstractions as building blocks
- 2. recursive decomposition
- 3. local reasoning
- 4. single entry, single exit point
- 5. soundness and completeness

# Concurrency with Threads



## primitives

threads locks (mutexes, semaphores, etc.)

## 1. abstractions as building blocks

threads and locks are not good abstractions

## 2. recursive decomposition

into what?

## 3. local reasoning

threads and locks have non-local effects (by design)

## 4. single entry, single exit point

N/A

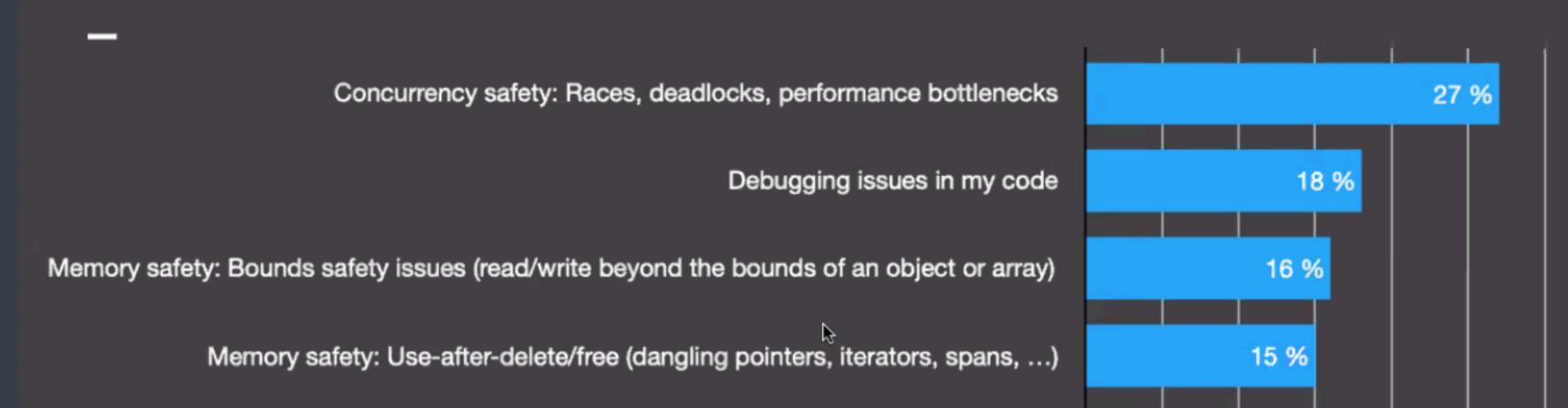
## 5. soundness and completeness

complete but not sound

#### unsound

#### no general strategy





#### structured?

no

no	abstractions as building blocks
no	recursive decomposition
no	local reasoning
	single entry, single exit point
1/2	soundness and completeness

# Concurrency with Tasks



## primitives

tasks (independent units of work)

#### two models

raw tasks

with continuations



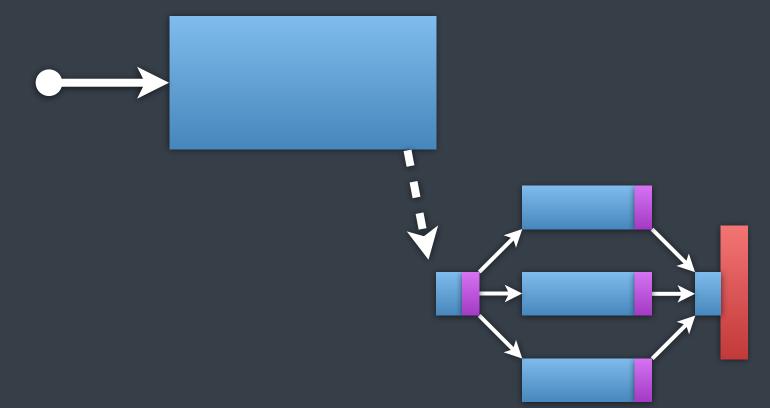


#### two models

raw tasks

with continuations





#### two models

raw tasks

with continuations

just like functions

can represent larger concurrent parts

#### raw tasks — structured?

partial

abstractions as building blocks yes recursive decomposition no local reasoning yes single entry, single exit point no soundness and completeness yes

## tasks w/cont. — structured?

partial

abstractions as building blocks
recursive decomposition
local reasoning
no
single entry, single exit point
soundness and completeness
yes

# Senders/Receivers

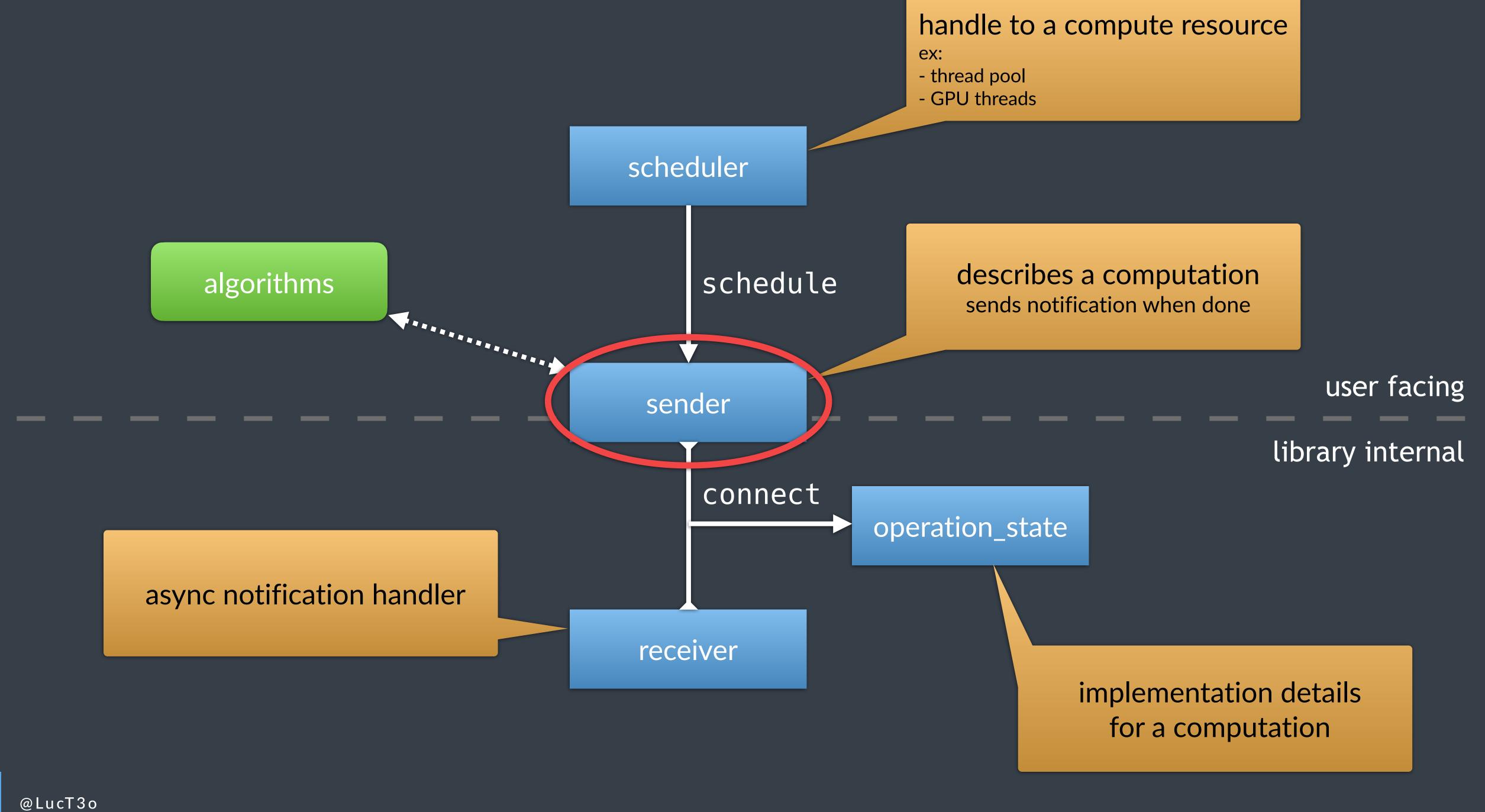


#### P2300 — std::execution

C++ proposal did not make it to C++23

#### P2300 — std::execution

concepts
initial set of algorithms
utilities



## senders describe computations

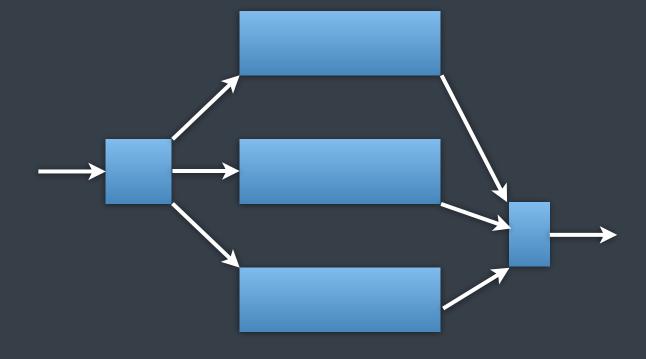
any chunk of work, with one entry and one exit point

atask

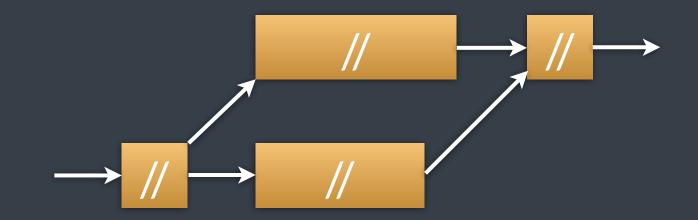


a task

tasks over multiple threads



a task
tasks over multiple threads
group of computations

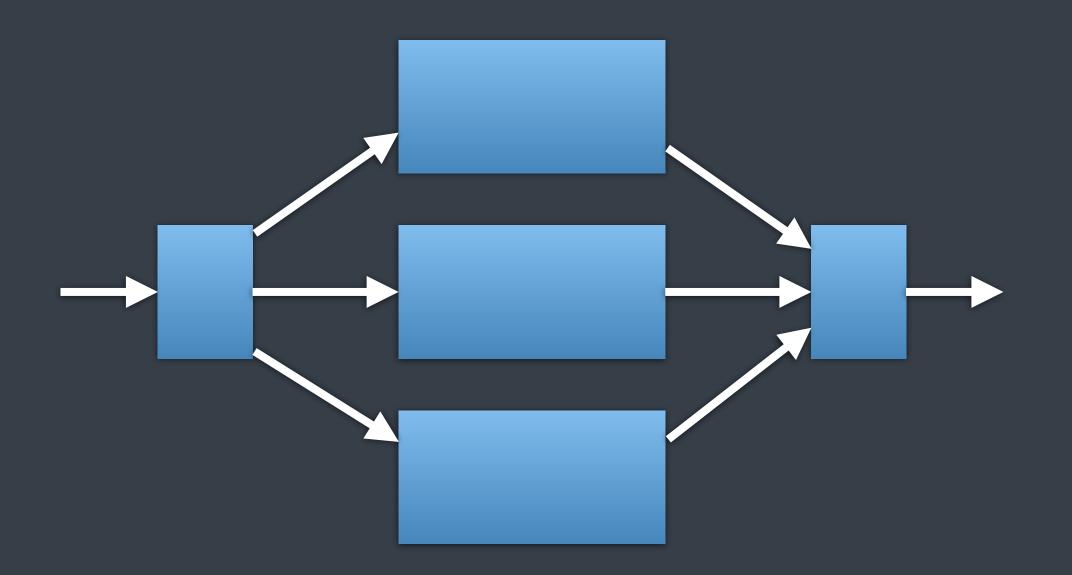


a task
asks over multiple threads
group of computations
the entire application



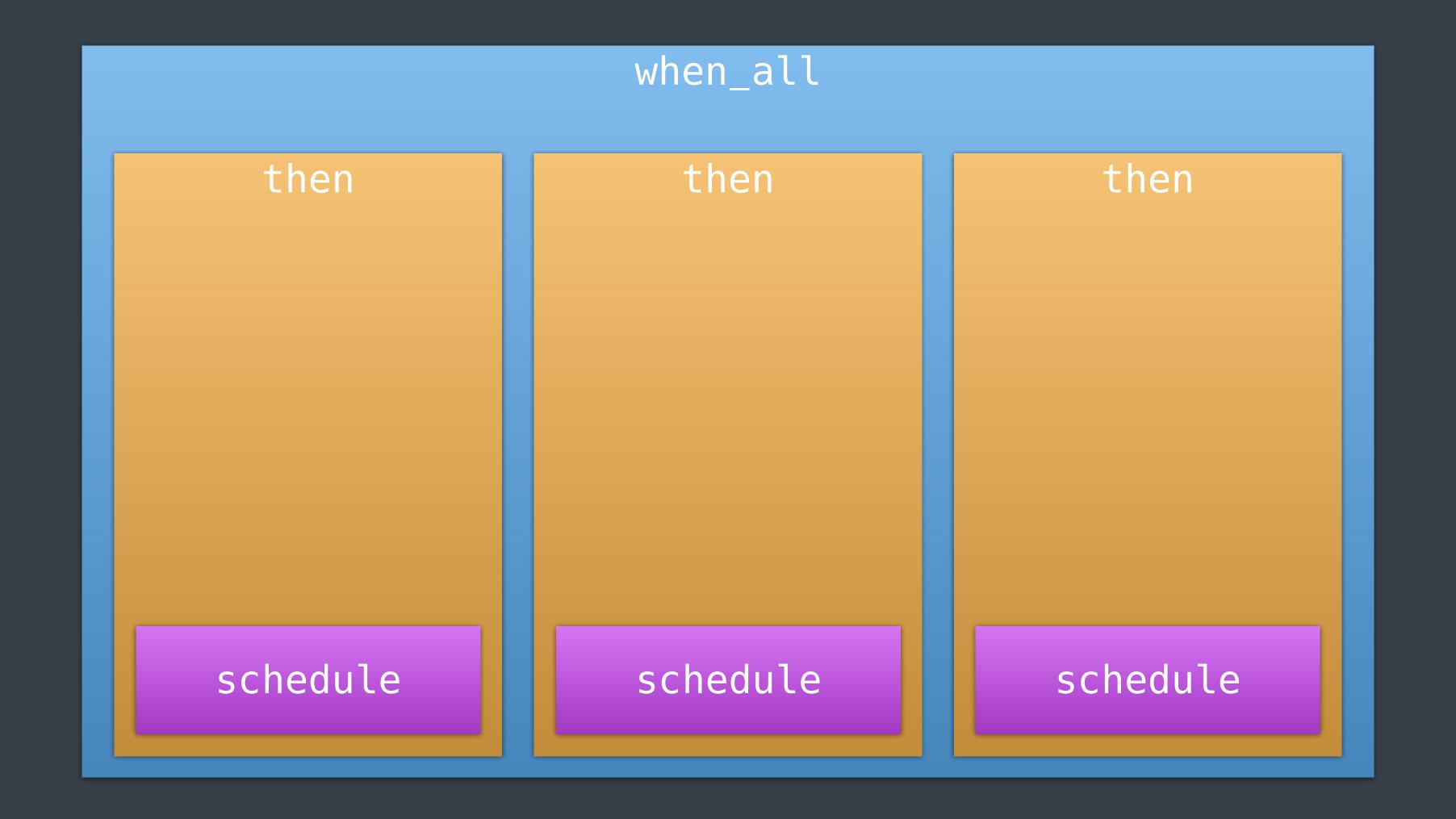
tasks over multiple threads group of computations the entire application

### example



#### example

```
auto work1() -> int;
auto work2() -> double;
auto work3() -> std::string;
auto combine_res(int i, double d, const std::string& s) -> int;
auto compute_in_parallel() -> int {
    static_thread_pool pool{8};
    ex::scheduler auto sched = pool.get_scheduler();
    ex::sender auto work =
        ex::when all
            ex::schedule(sched)
                                  ex::then(work1),
                                  ex::then(work2),
            ex::schedule(sched)
            ex::schedule(sched)
                                  ex::then(work3)
   auto [i, d, s] = std::this_thread::sync_wait(std::move(work)).value();
    return combine_res(i, d, s);
```



#### senders's completion

promises to call on completion, one of:

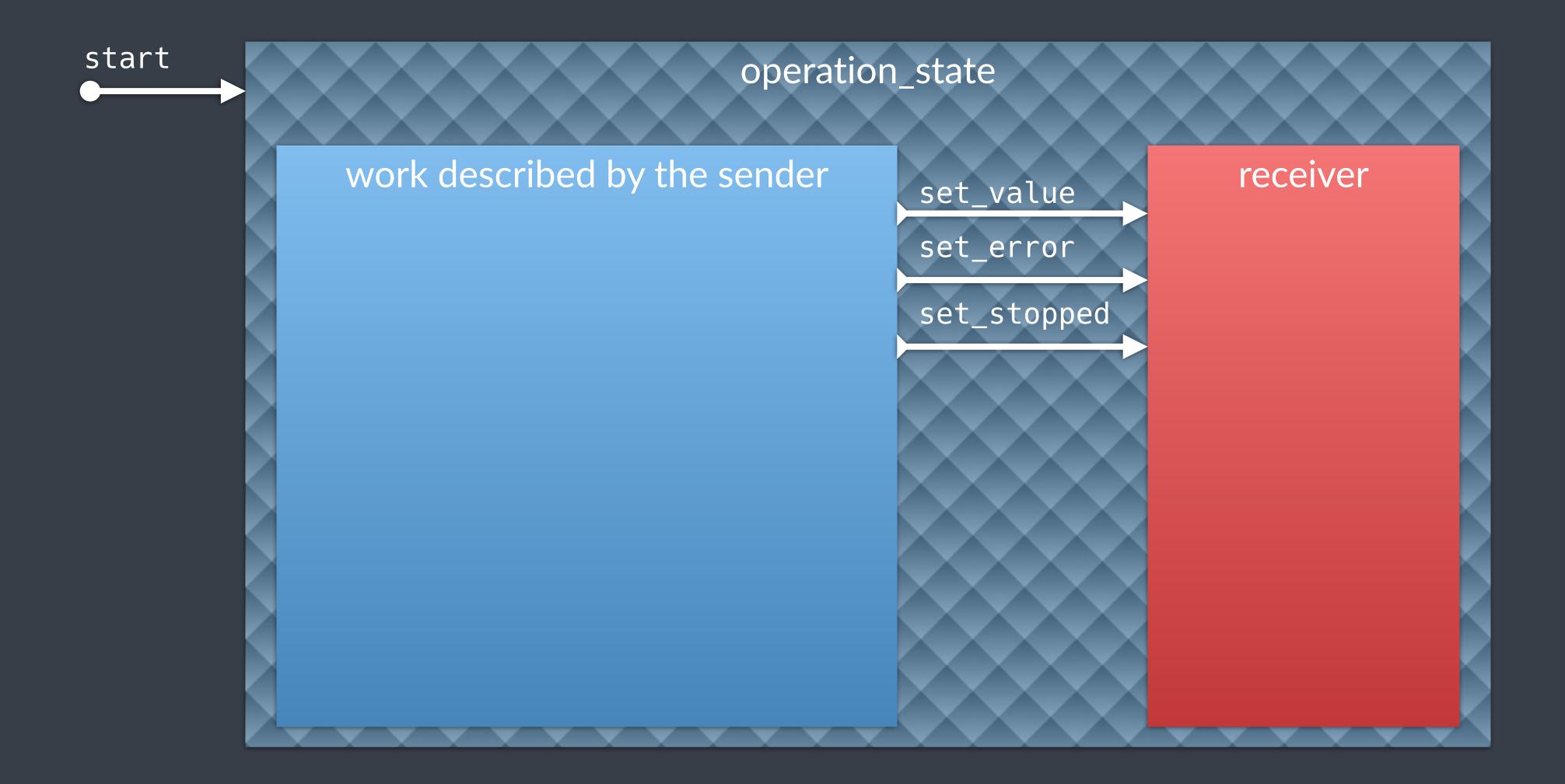
```
- set_value(dest, values...)
```

- set\_error(dest, error)
- set\_stopped(dest)

#### receiver

something that is called with one of:

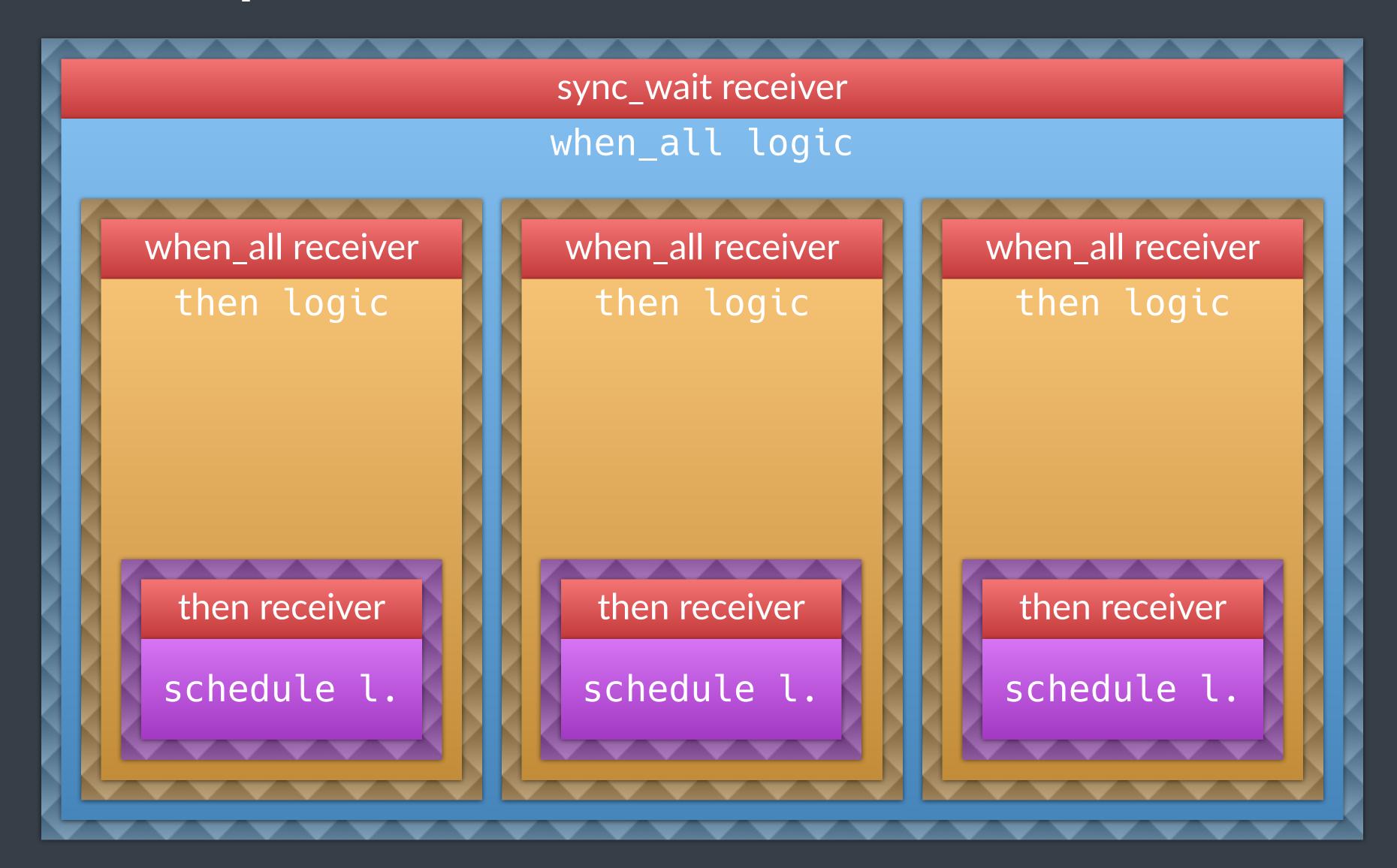
- set\_value(recv, values...)
- set\_error(recv, error)
- set\_stopped(recv)



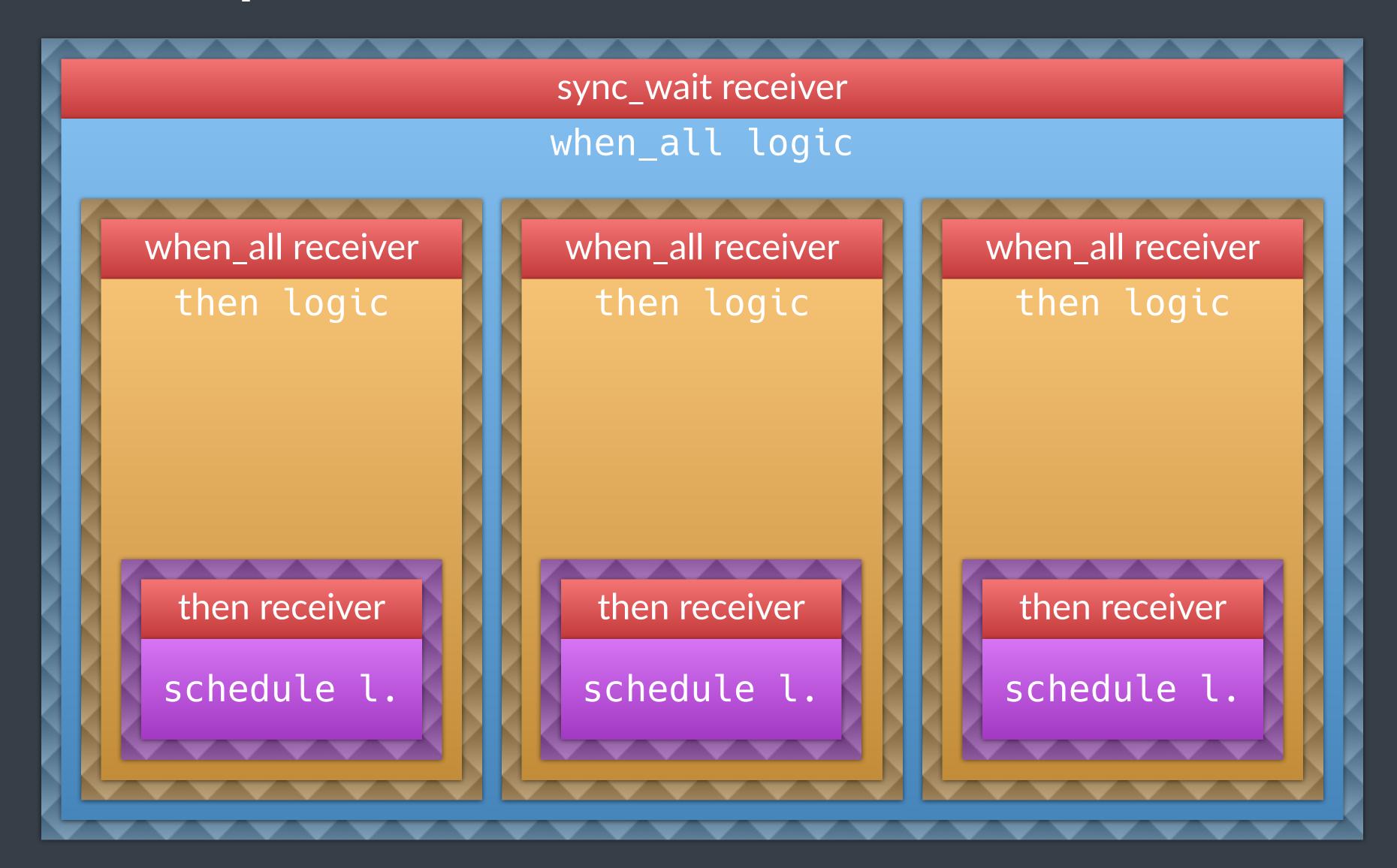
#### operation state object

alive during the whole duration

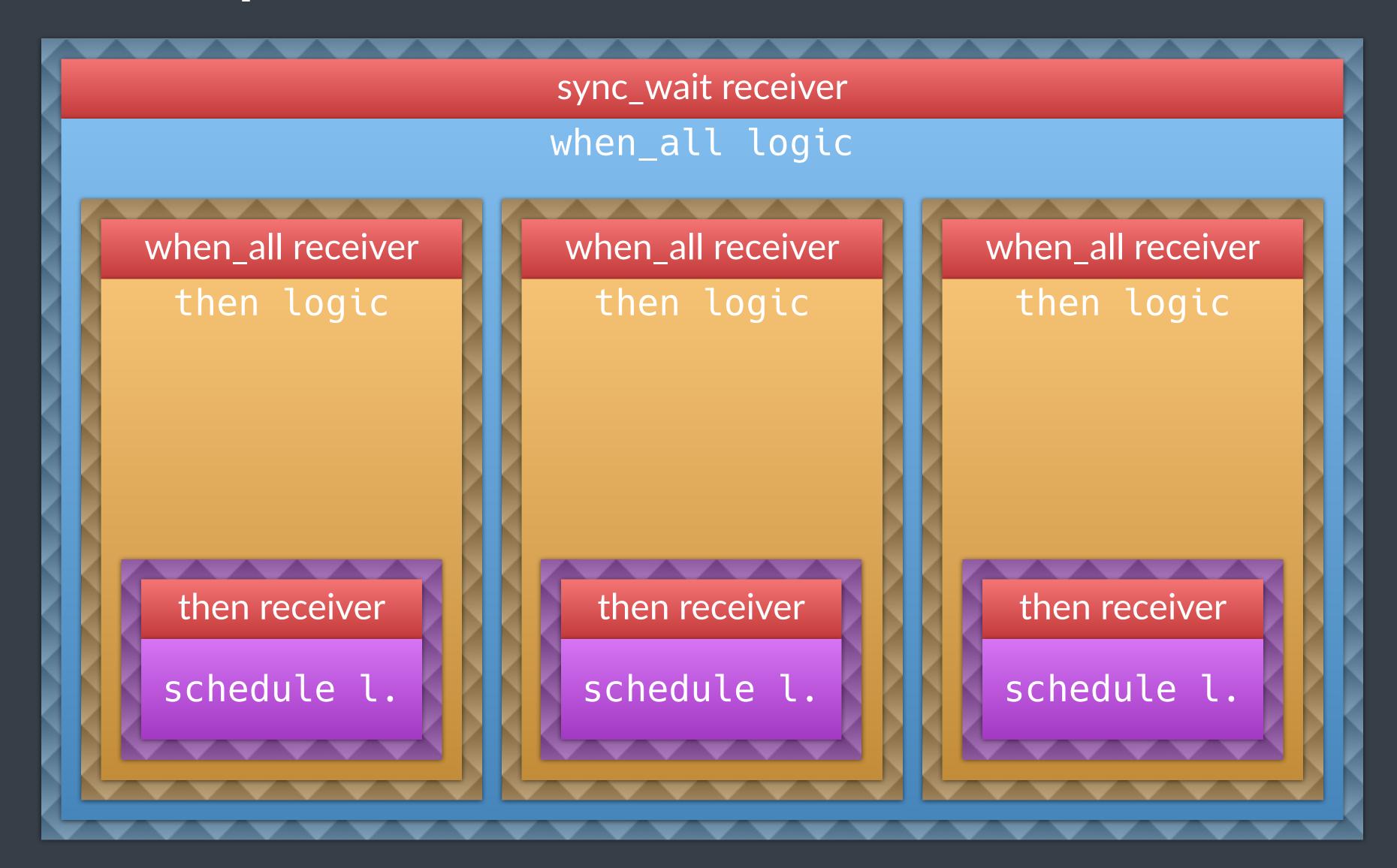
#### operation state creation

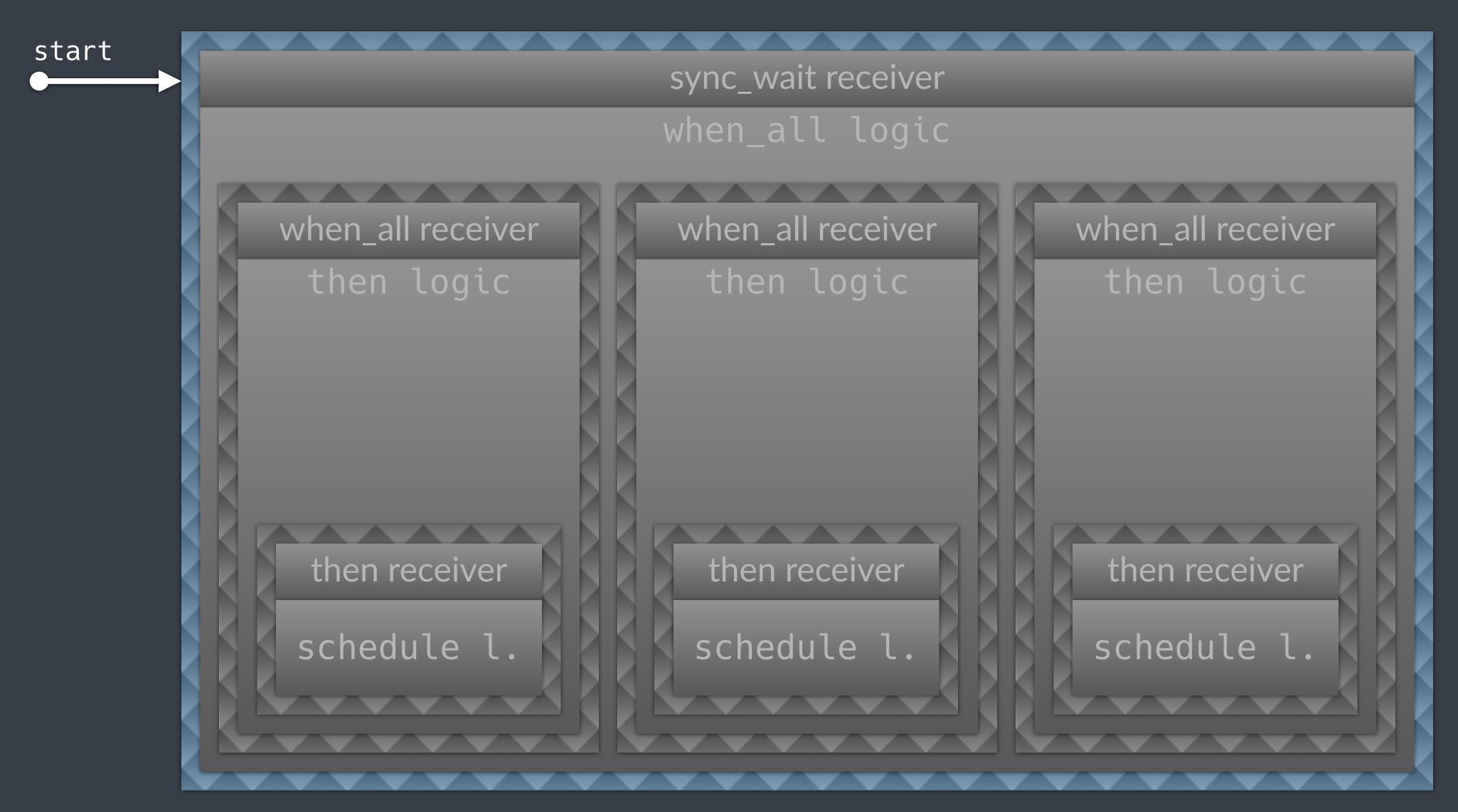


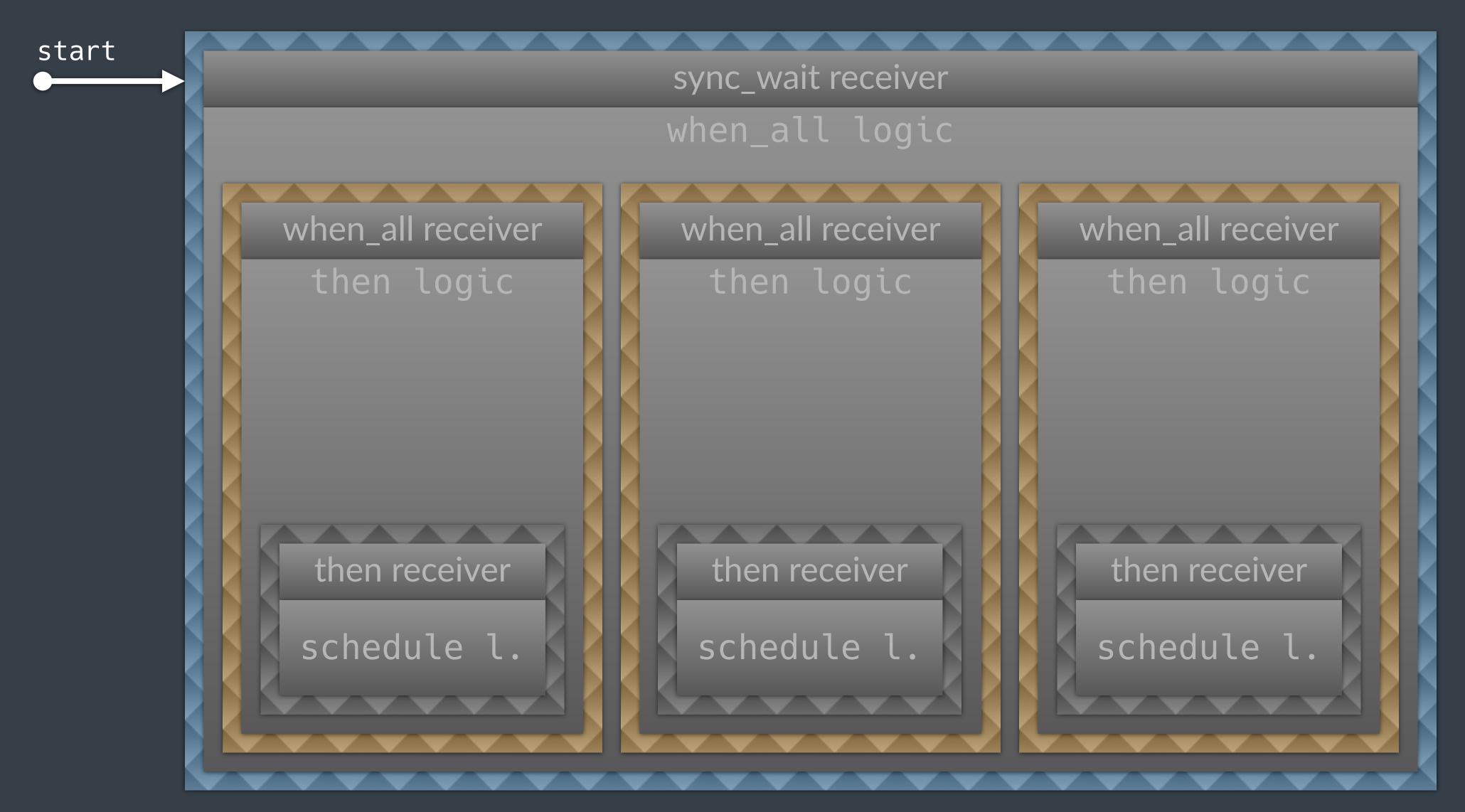
#### operation state creation

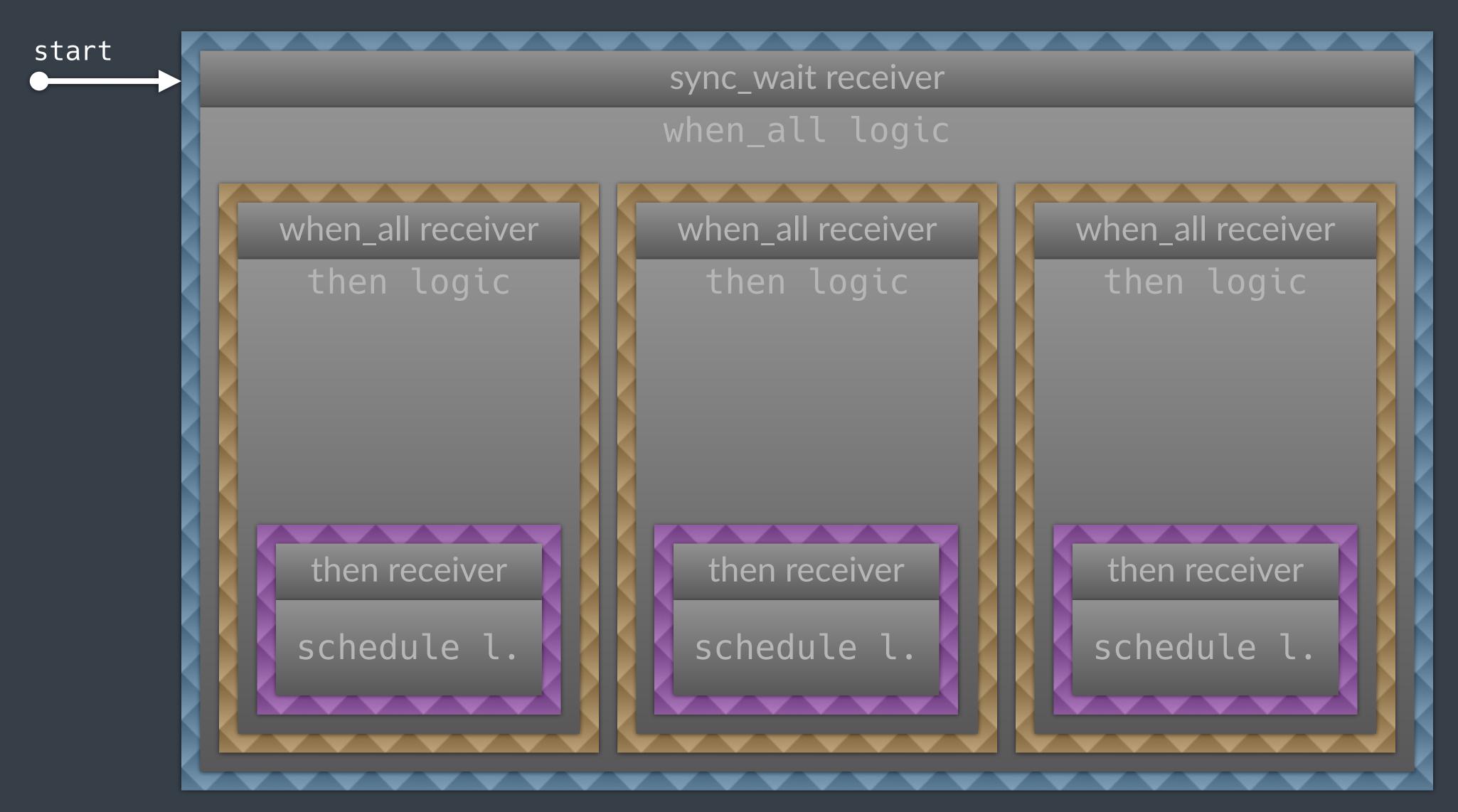


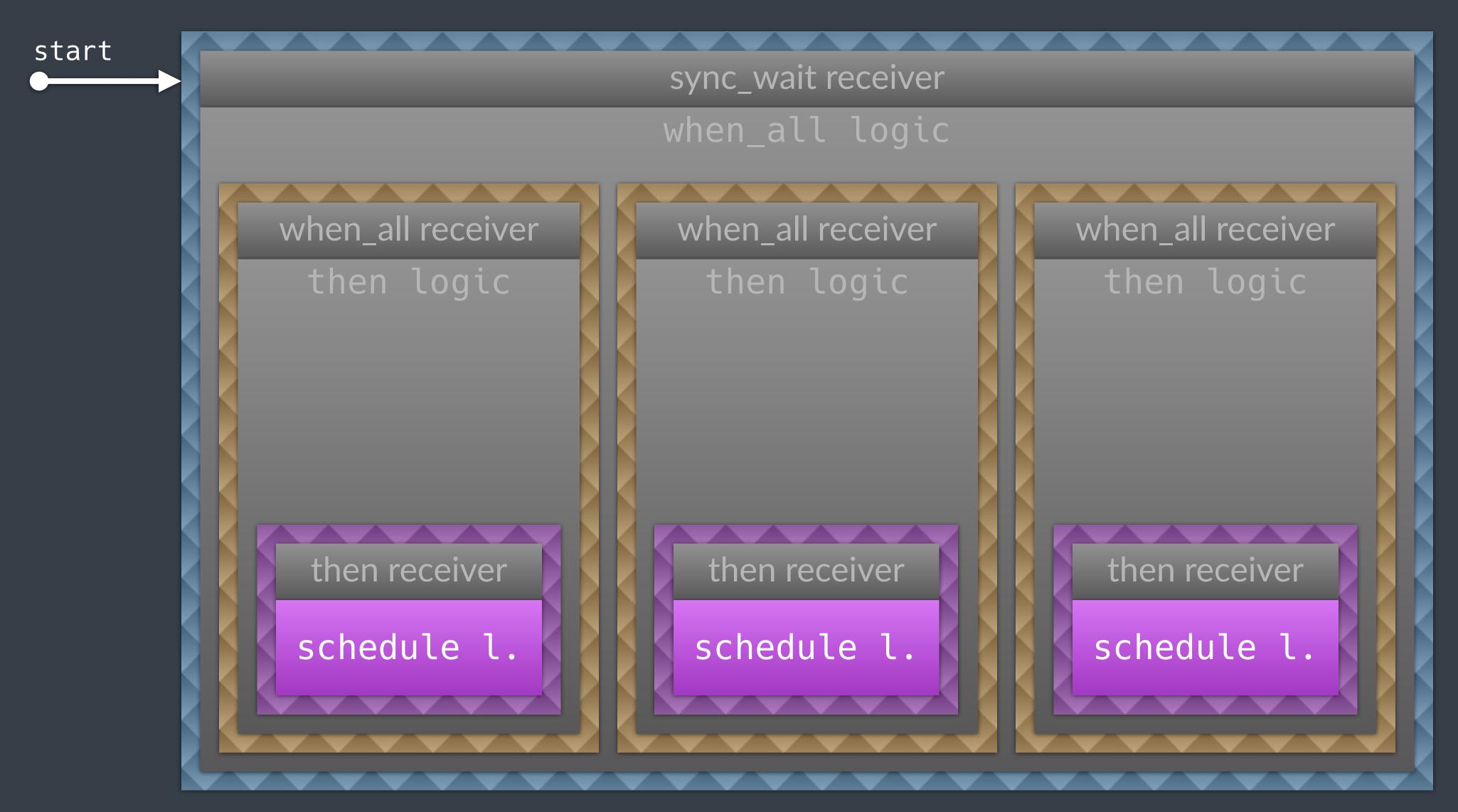
#### operation state creation

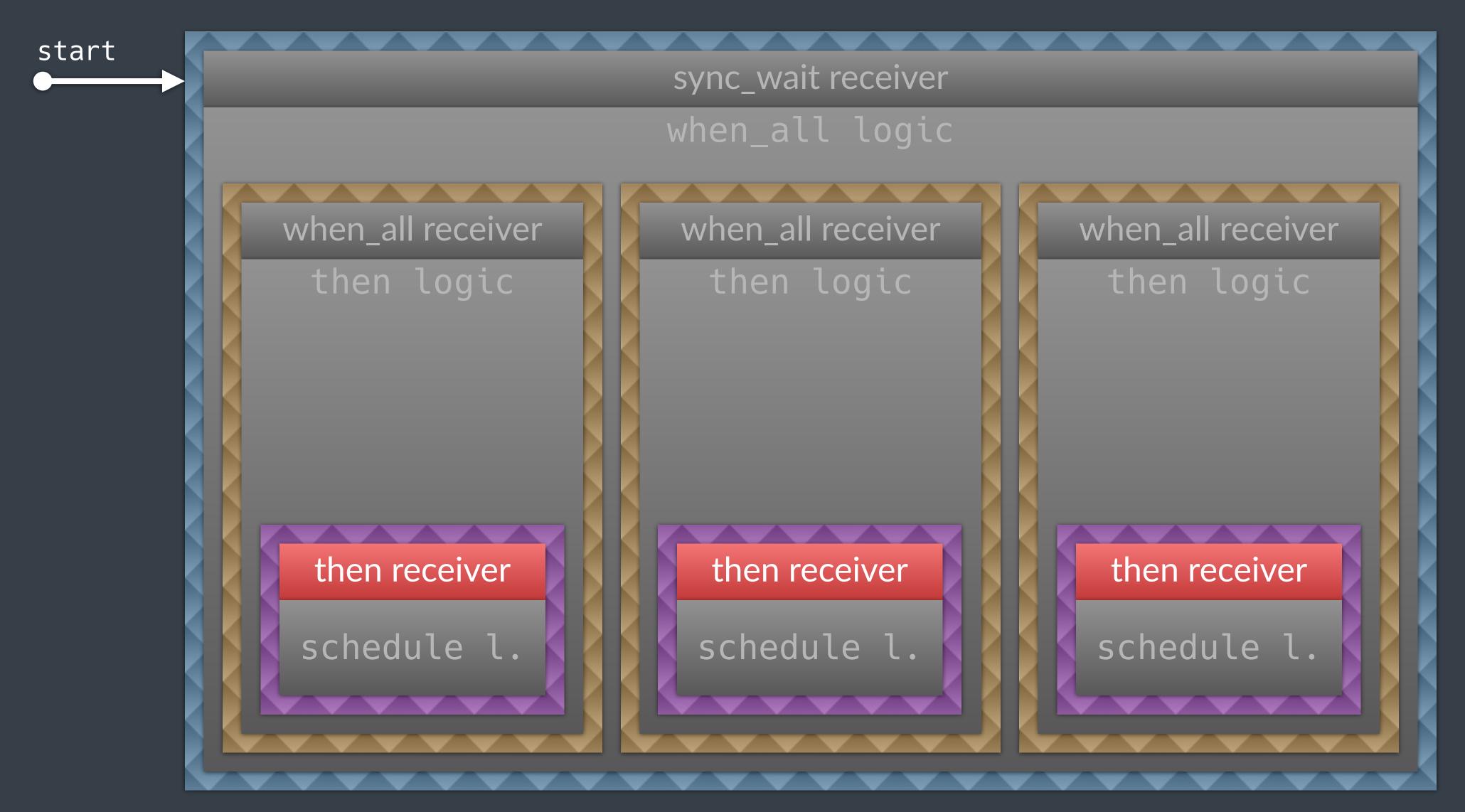


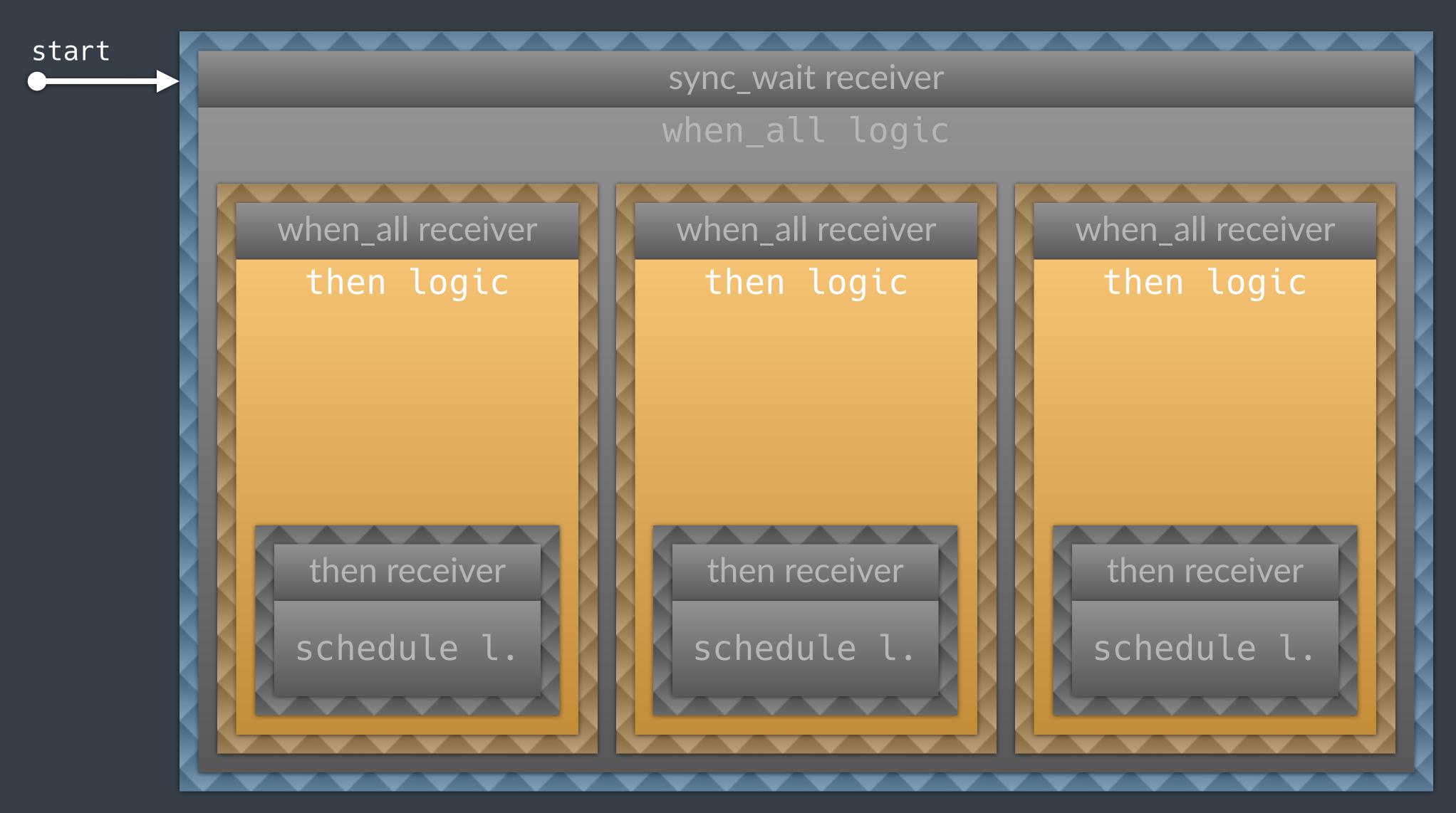


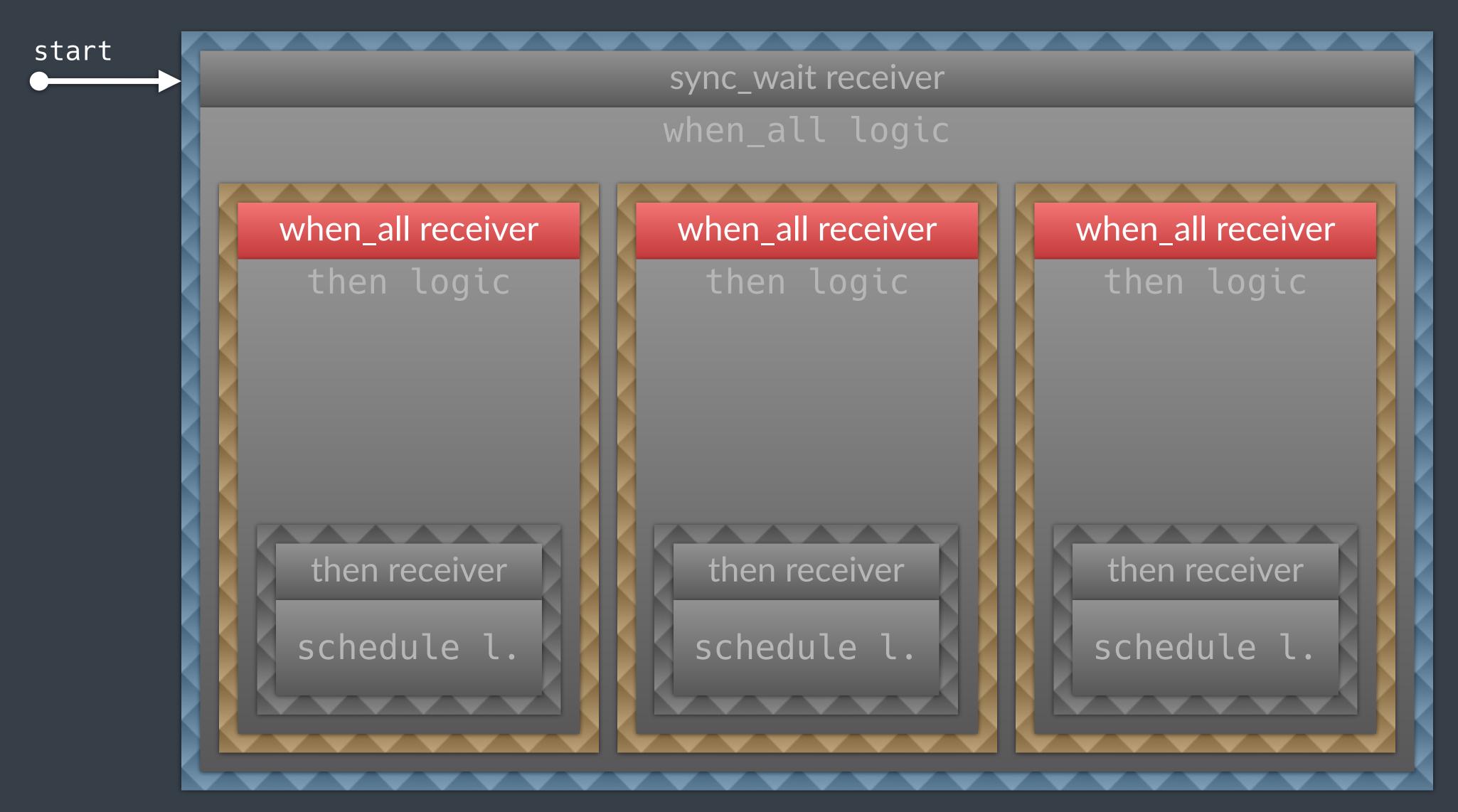


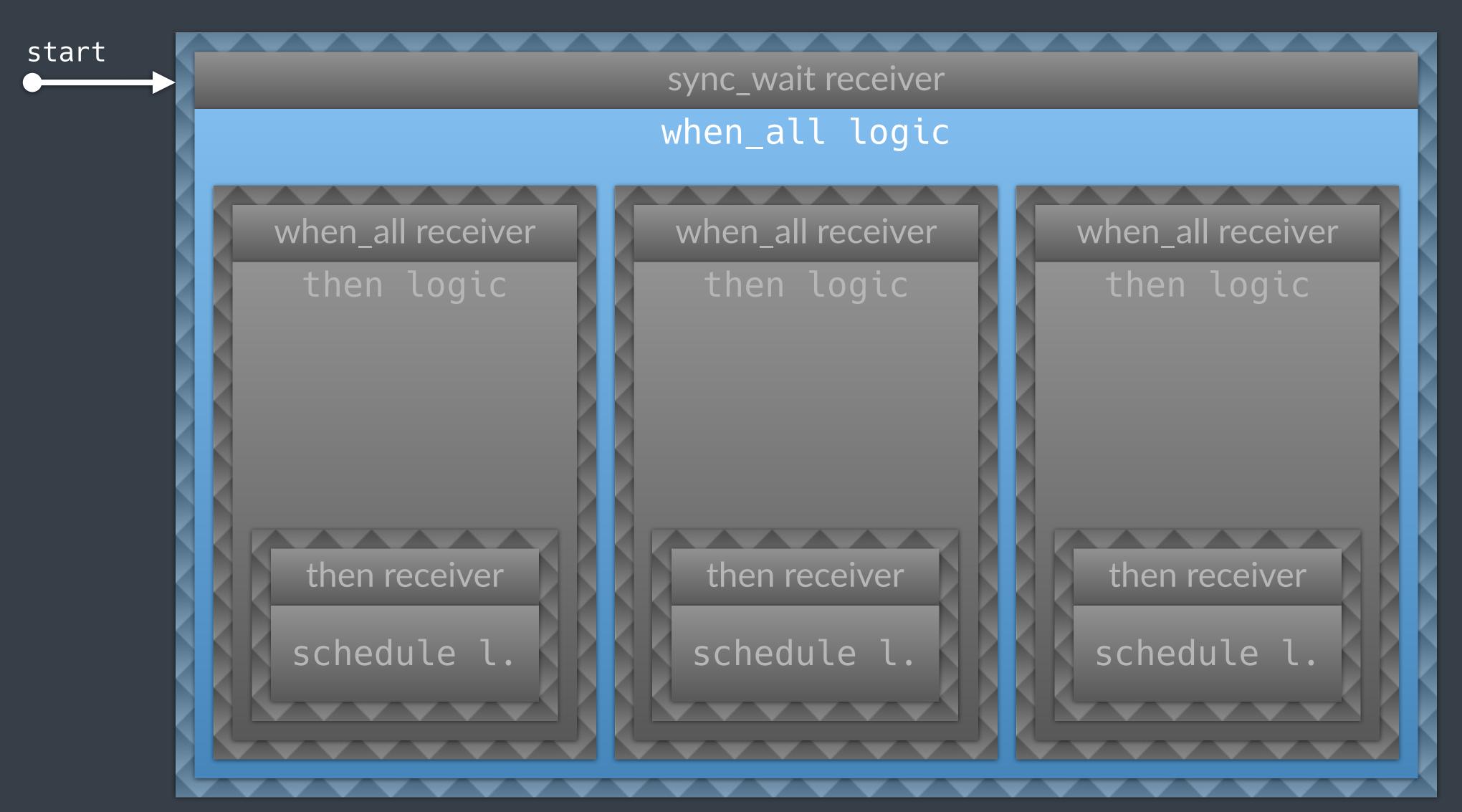


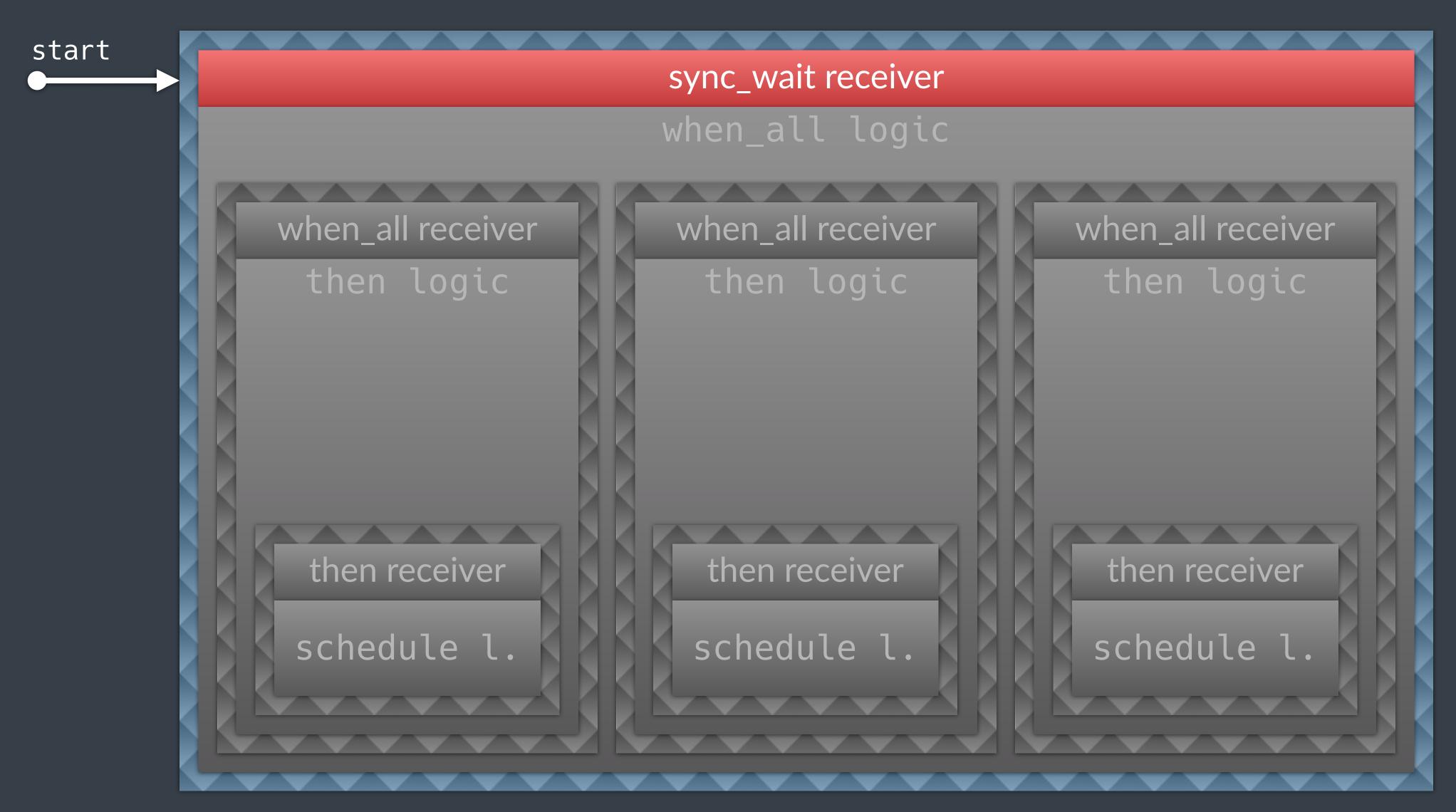




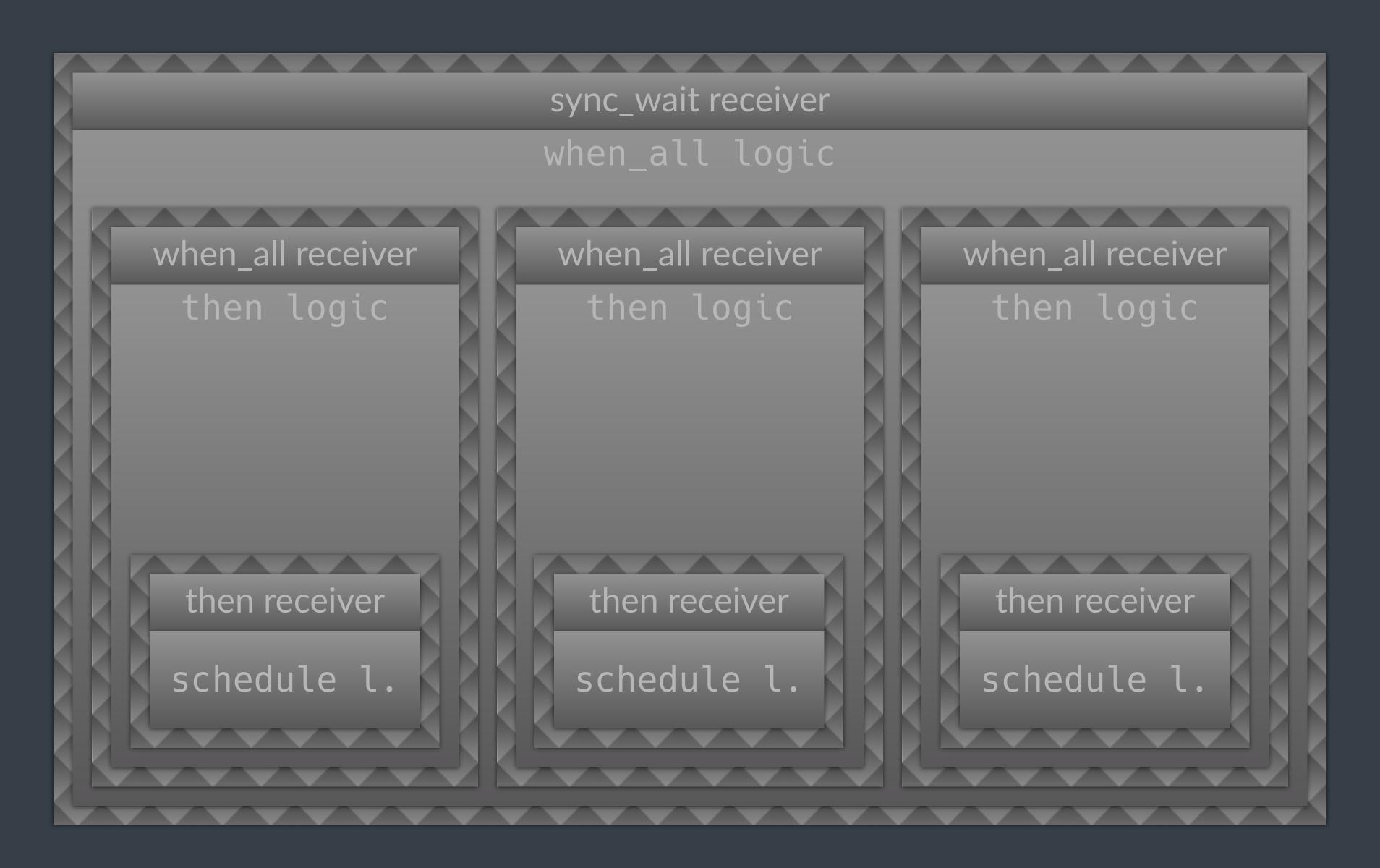








#### done



#### focus of the talk

senders describe computations

#### functions

#### computations

same thread

entry thread ≠ exit thread

generalisation of functions

# computations are for concurrency what functions are for Structured Programming

## Structured Concurrency



#### functions

#### computations

Structured Programming

Structured Concurrency

#### functions

#### senders

Structured Programming

Structured Concurrency

#### some theoretical results

#### P2504R0 Computations as a global solution to

concurrency

Published Proposal, 2021-12-11

Author:

Lucian Radu Teodorescu

Source:

GitHub

Issue Tracking:

GitHub

Project:

ISO/IEC JTC1/SC22/WG21 14882: Programming Language — C++

Audience:

SG1, LEWG

#### § 1. Introduction

This paper aims at providing proof that the senders/receivers model proposed by [P2300R2] can constitute a global solution to concurrency.

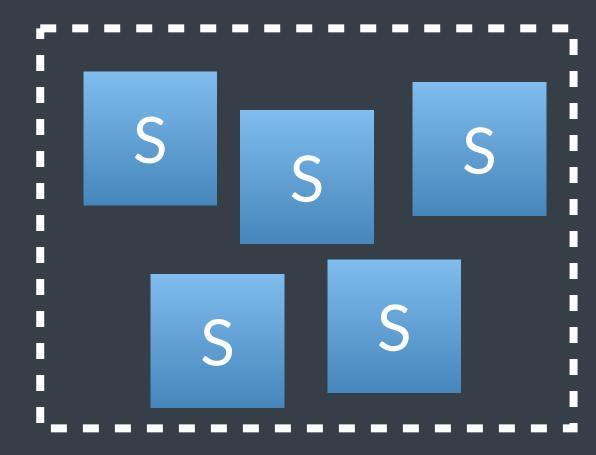
http://wg21.link/P2504



#### some theoretical results (1)

all programs can be described in terms of senders

(w/o the need of synchronisation primitives)



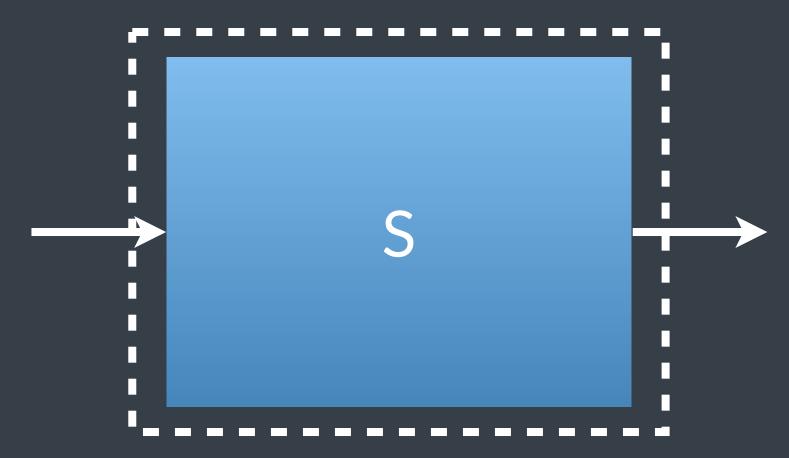
#### some theoretical results (2)

any part of a program,
that has one entry point and one exit point,
can be described as a sender



#### some theoretical results (3)

the entire program can be described as one sender



## some theoretical results (4)

any sufficiently large concurrent chunk of work can be decomposed into smaller chunks of work, which can be described with senders

## some theoretical results (5)

programs can be implemented using senders using maximum efficiency (under certain assumptions)

# computations fully encapsulate concurrency concerns

# computations are for concurrency what functions are for Structured Programming

#### Structured Concurrency

- 1. abstractions as building blocks
- 2. recursive decomposition
- 3. local reasoning
- 4. single entry, single exit point
- 5. soundness and completeness

### 1. abstractions as building blocks

# use computations (senders)

similar to using functions

## 2. recursive decomposition

divide et impera

# computations can be broken down into smaller computations

senders, from top to bottom

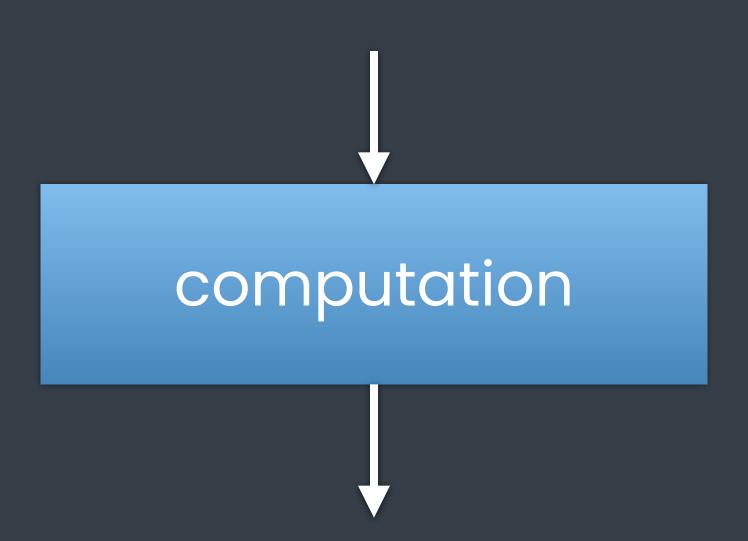
#### 3. local reasoning

nested scopes encapsulation of local concerns

#### no spooky action at a distance

all the concerns are handled locally inputs and outputs are clearly defined senders nests

## 4. single entry, single exit point

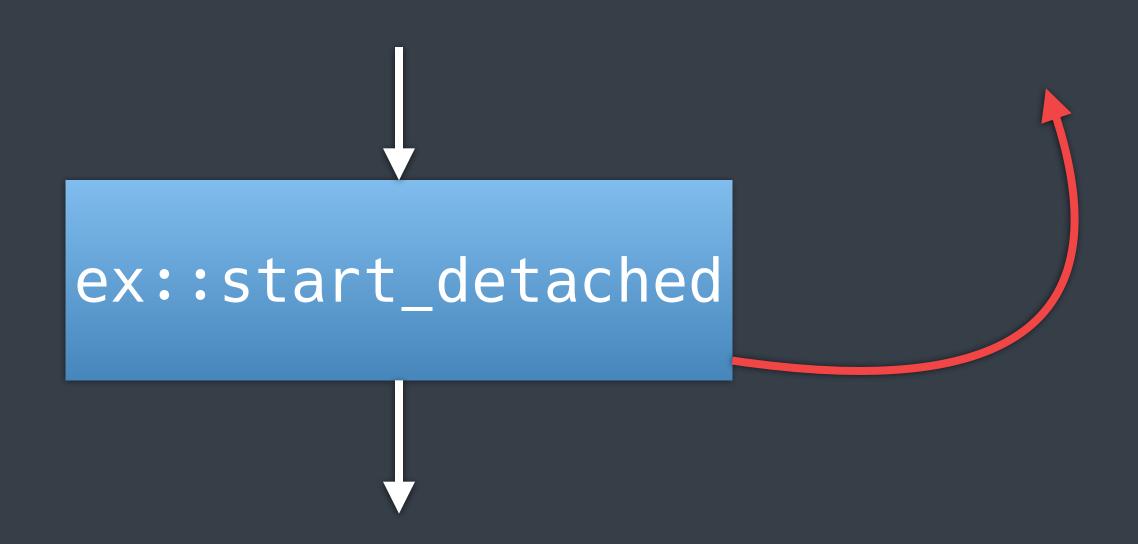


#### by definition

```
input:
- start(op_state)

   output is one of:
- set_value(recv, values...)
- set_error(recv, error)
- set_stopped(recv)
```

## discouraged: fire-and-forget



### computations — same shape

composability of concurrent work

#### 5. soundness and completeness

can Structured Concurrency be applied?

#### soundness

all programs can safely be built with senders (without the need of sync. primitives)

### completeness

all programs can be described by senders

#### Structured Concurrency



- 1. abstractions as building blocks
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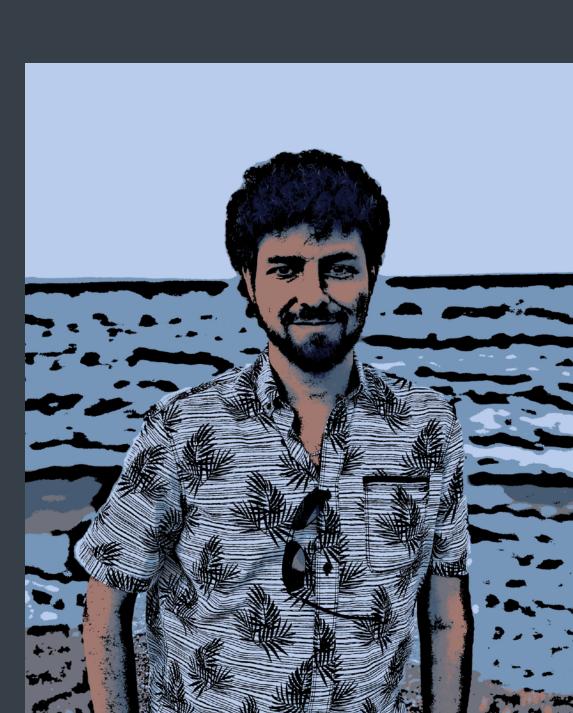
# An Example





## application

HTTP server image processing



#### goals

senders as building blocks
recursive decomposition with senders
local reasoning
single entry and single exit point (\*)

## secondary goals

interaction with coroutines type erasure for senders



## the entire app is a sender

```
auto main() -> int {
    auto [r] = std::this_thread::sync_wait(get_main_sender()).value();
    return r;
}
```

## the entire app is a sender

#### top-level logic

```
auto get_main_sender() {
    return ex::just() | ex::then([] {
        int port = 8080;
        static_thread_pool pool{8};
        io::io_context ctx;
        set_sig_handler(ctx, SIGTERM);
        ex::sender auto snd = ex::on(ctx.get_scheduler(), listener(port, ctx, pool));
        ex::start_detached(std::move(snd));
        ctx.run();
        return 0;
```

#### listener

```
auto listener(int port, io::io_context& ctx, static_thread_pool& pool)-> task<bool> {
    // ...
    co_return true;
}
```

#### listener

```
auto listener(int port, io::io_context& ctx, static_thread_pool& pool)-> task<bool> {
    io::listening_socket listen_sock;
    listen_sock.bind(port);
    listen_sock.listen();
   while (!ctx.is_stopped()) {
        io::connection conn = co_await io::async_accept(ctx, listen_sock);
        conn_data data{std::move(conn), ctx, pool};
        ex::sender auto snd =
                ex::just()
                  ex::let_value([data = std::move(data)]() { //
                      return handle_connection(data);
        ex::start_detached(std::move(snd));
   co_return true;
```

@LucT3o

#### async\_accept -> a sender

```
inline auto async_accept(io_context& ctx, const listening_socket& sock)
          -> detail::async_accept_sender {
        return {&ctx, sock.fd()};
}
```

#### handle\_connection

#### just\_500\_response

#### read\_http\_request

```
auto read_http_request(io::io_context& ctx, const io::connection& conn)
        -> task<http_server::http_request> {
   http_server::request_parser parser;
   std::string buf;
   buf.reserve(1024 * 1024);
    io::out_buffer out_buf{buf};
    while (true) {
        std::size_t n = co_await io::async_read(ctx, conn, out_buf);
        auto data = std::string_view{buf.data(), n};
        auto r = parser.parse_next_packet(data);
        if (r)
            co_return {std::move(r.value())};
```

#### async\_read -> a sender

#### write\_http\_request

```
auto write_http_response(io::io_context& ctx, const io::connection& conn,
        http_server::http_response resp) -> task<std::size_t> {
    std::vector<std::string_view> out_buffers;
    http_server::to_buffers(resp, out_buffers);
    std::size_t bytes_written{0};
    for (auto buf : out_buffers) {
        while (!buf.empty()) {
            auto n = co_await io::async_write(ctx, conn, buf);
            bytes_written += n;
            buf = buf.substr(n);
    co_return bytes_written;
```

#### async\_write -> a sender

#### handle\_request

```
auto handle_request(const conn_data& cdata, http_server::http_request req)
        -> task<http_server::http_response> {
   auto puri = parse_uri(req.uri_);
    if (puri.path_ == "/transform/blur")
        co_return handle_blur(cdata, std::move(req), puri);
   else if (puri.path_ == "/transform/adaptthresh")
        co_return handle_adaptthresh(cdata, std::move(req), puri);
   else if (puri.path_ == "/transform/reducecolors")
        co_return handle_reducecolors(cdata, std::move(req), puri);
    else if (puri.path_ == "/transform/cartoonify")
        co_return co_await handle_cartoonify(cdata, std::move(req), puri);
   else if (puri.path_ == "/transform/oilpainting")
        co_return handle_oilpainting(cdata, std::move(req), puri);
   else if (puri.path_ == "/transform/contourpaint")
        co_return co_await handle_contourpaint(cdata, std::move(req), puri);
   co_return http_server::create_response(http_server::status_code::s_404_not_found);
```

```
auto handle_cartoonify(const conn_data& cdata, http_server::http_request&& req, parsed_uri puri)
        -> task<http_server::http_response> {
    int blur_size = get_param_int(puri, "blur_size", 3);
    int num_colors = get_param_int(puri, "num_colors", 5);
    int block_size = get_param_int(puri, "block_size", 5);
    int diff = get_param_int(puri, "diff", 5);
    auto src = to_cv(req.body_);
    ex::sender auto snd = ex::when_all(
        ex::transfer_just(cdata.pool_.get_scheduler(), src)
               ex::then([=](const cv::Mat& src) {
                  auto gray = tr_to_grayscale(tr_blur(src, blur_size));
                  return tr adaptthresh(gray, block size, diff);
               }),
        ex::transfer_just(cdata.pool_.get_scheduler(), src)
                   ex::then([=](const cv::Mat& src) {
                       return tr_reducecolors(src, num_colors);
        ex::then([](const cv::Mat& edges, const cv::Mat& reduced_colors) {
            return tr_apply_mask(reduced_colors, edges);
        ex::then(img_to_response);
    co_return co_await std::move(snd);
```

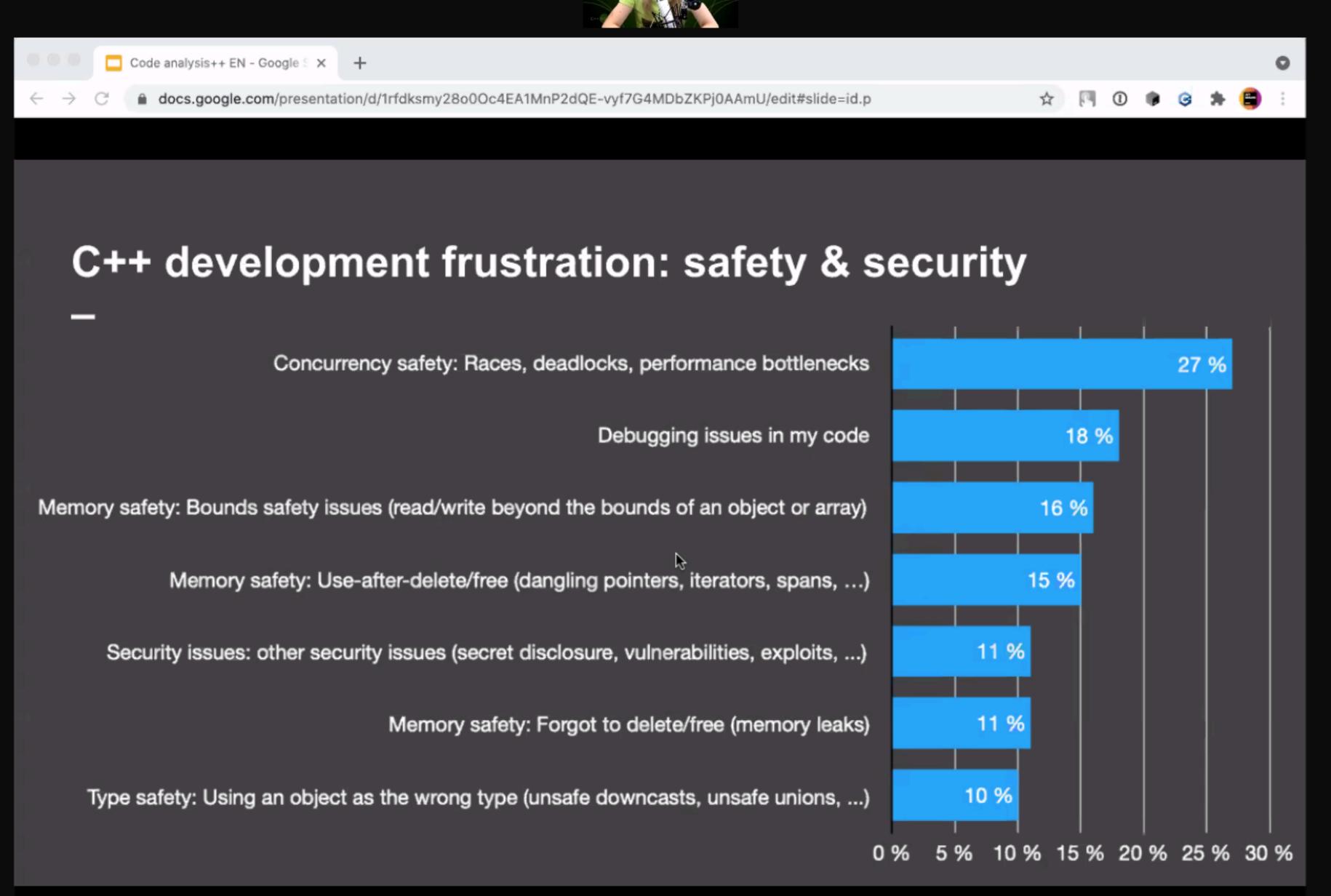
## recursive decomposition

- get\_main\_sender
  - listener
    - async\_accept
    - handle\_connection
      - read\_http\_request
        - async\_read
      - handle\_request
        - handle\_cartoonify
        - •
      - just\_500\_response
      - write\_http\_response
        - async\_write

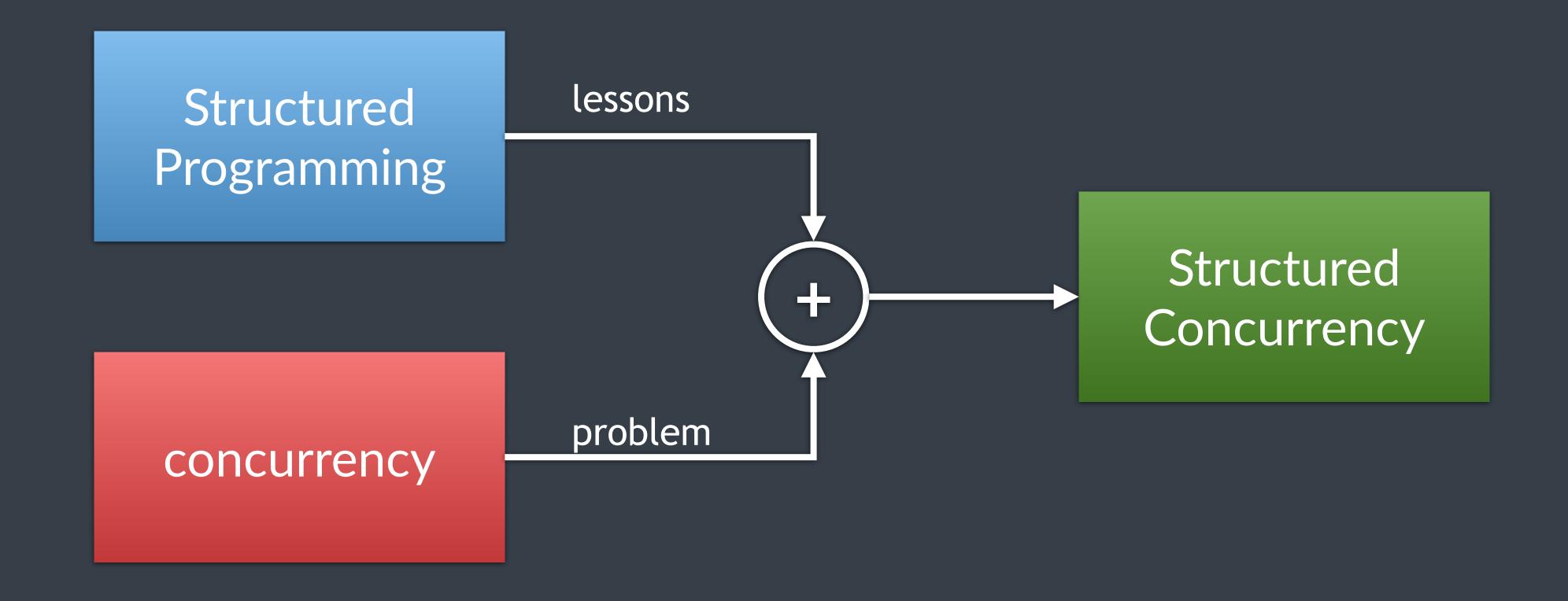
# Conclusions







#### what we did



## key insight

functions → Structured Programming

computations → Structured Concurrency

#### Structured Concurrency

- 1. abstractions as building blocks
- 2. recursive decomposition
- 3. local reasoning
- 4. single entry, single exit point
- 5. soundness and completeness

