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How to Build Digital Signatures From Hash Functions

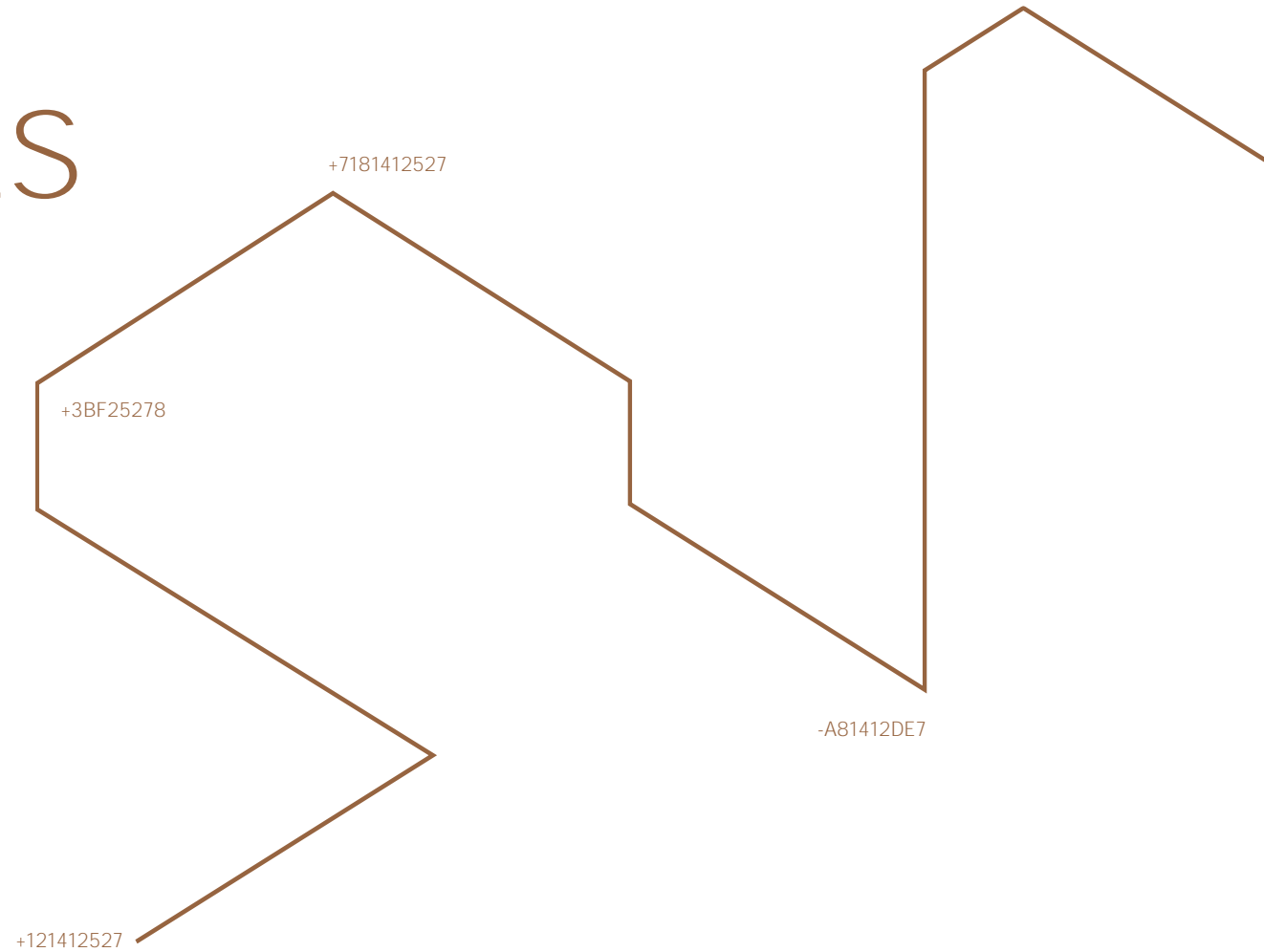
Ahto Truu



HOW TO BUILD DIGITAL SIGNATURES FROM HASH FUNCTIONS

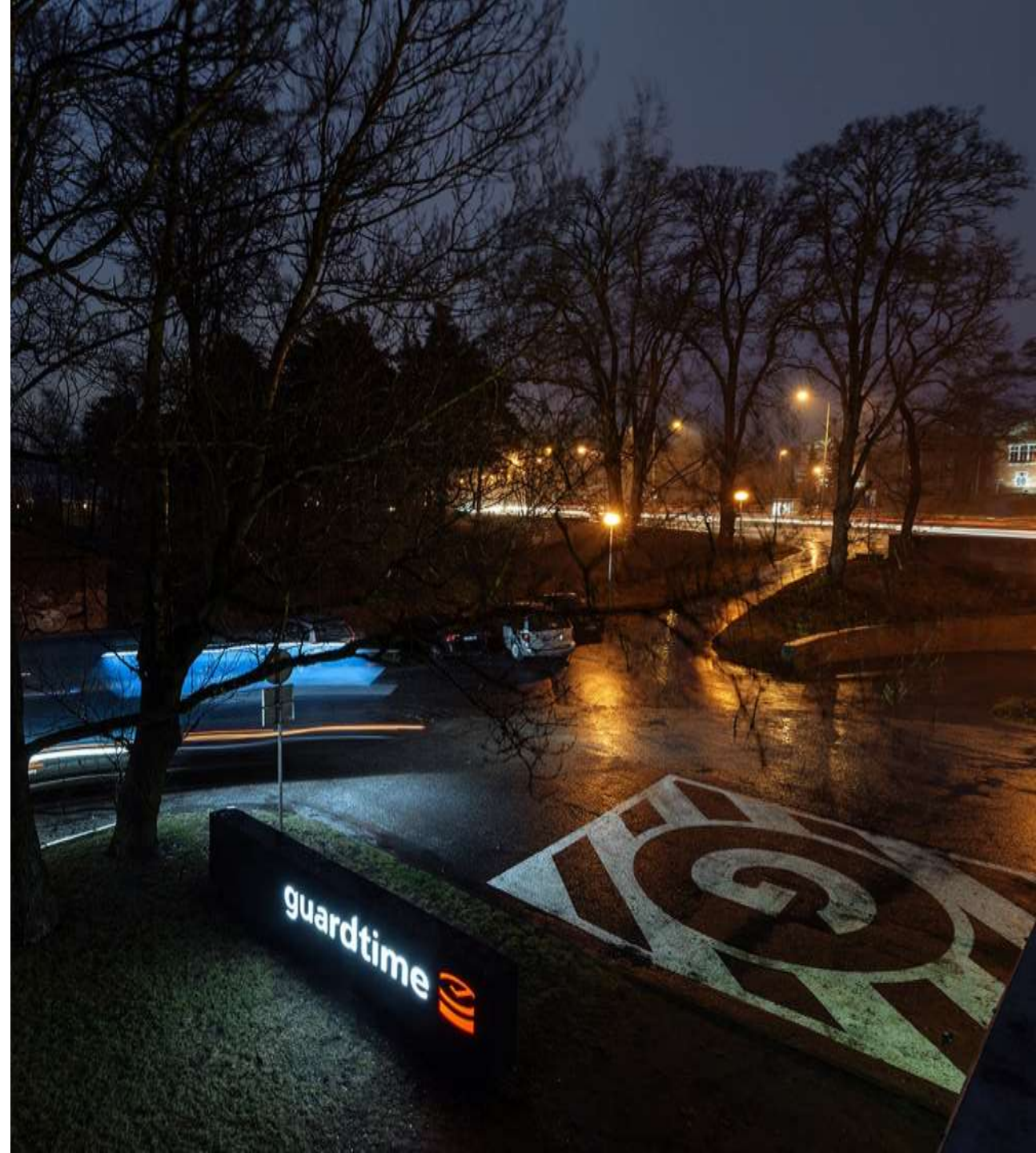
AHTO TRUU
SOFTWARE ARCHITECT, GUARDTIME

ACCU CONFERENCE, 12-MAR-2021



ABOUT GUARDTIME

- + Systems engineering company focusing on **data security** solutions
- + **Founded** in 2007 in Tallinn, Estonia
- + **Global HQ** in Lausanne, Switzerland
- + **Offices** in US, EU and China
- + 150 employees
- + 80% engineers and researchers
- + <https://guardtime.com/>

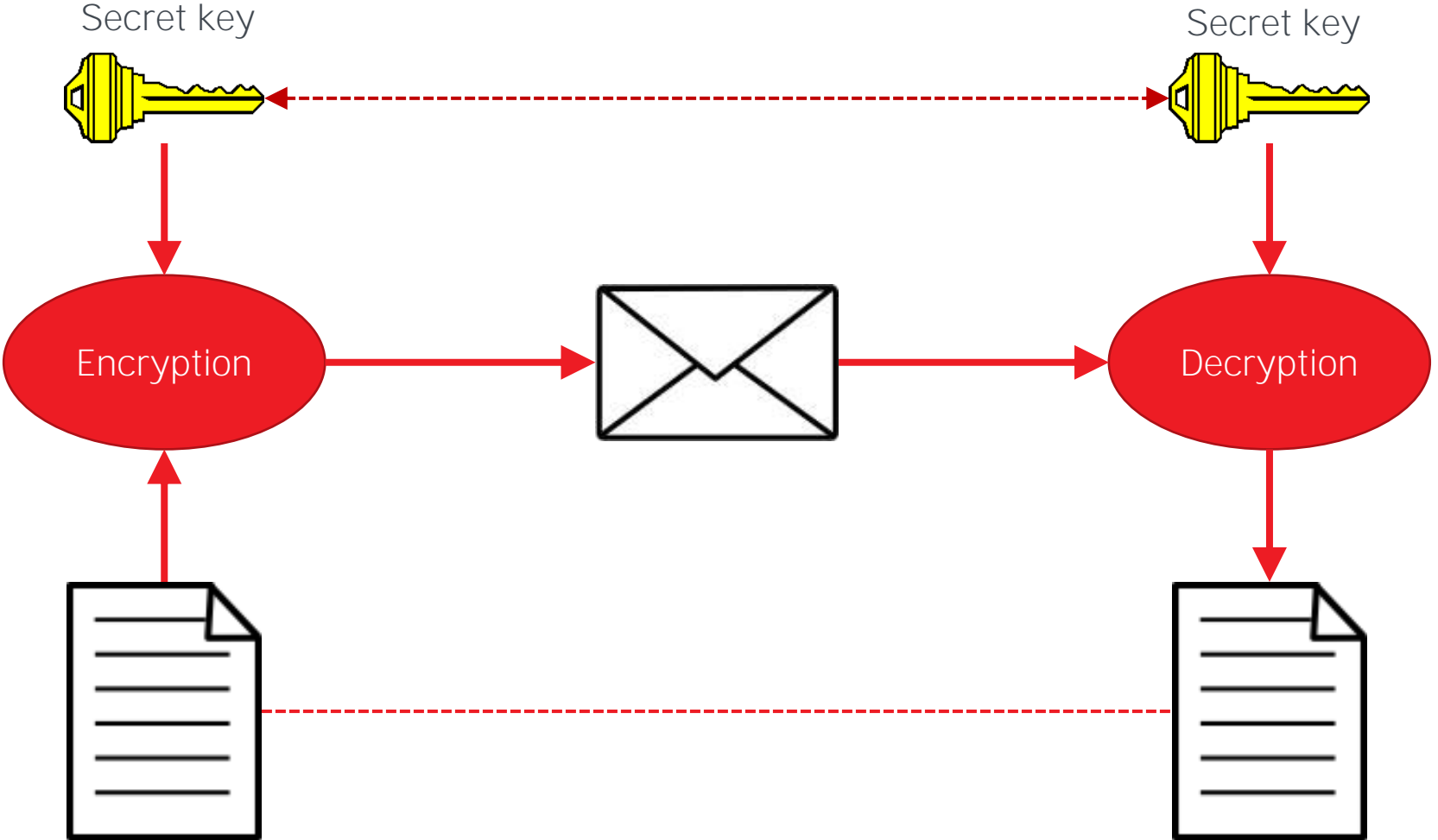


AGENDA

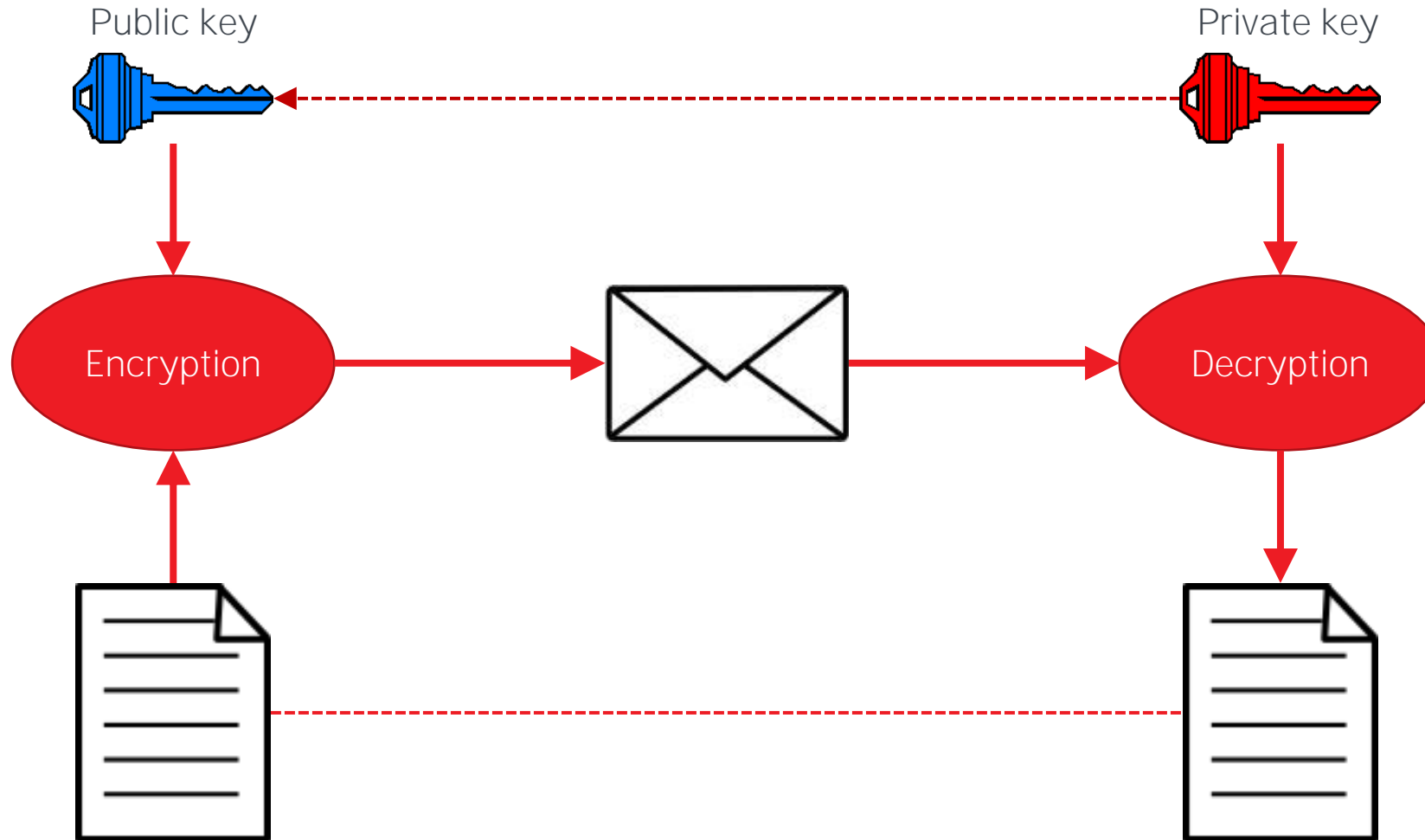
- + Introduction
- + Digital signatures
- + Hash functions
- + Hash signatures
- + Time-stamping
- + BLT signatures

1/ INTRODUCTION

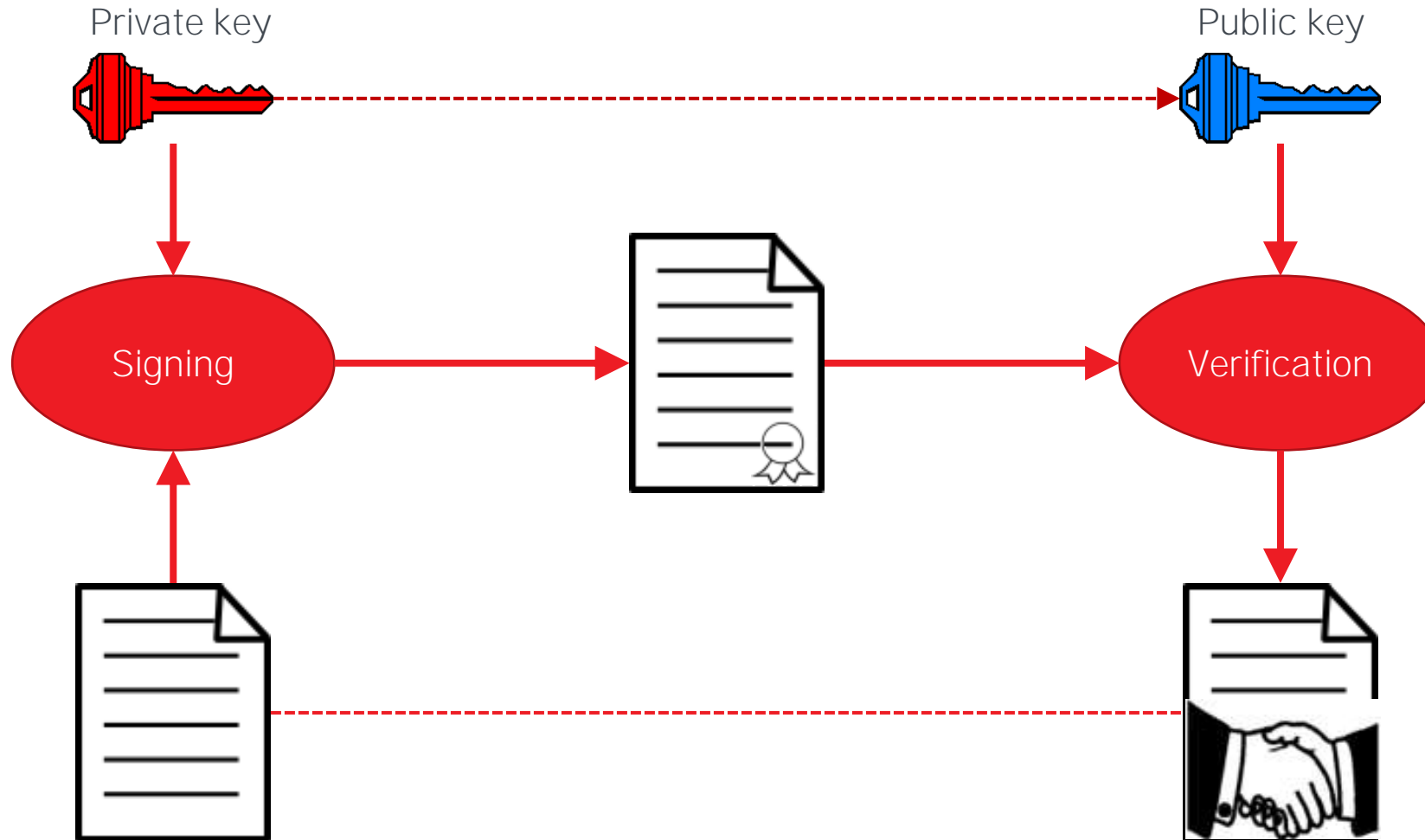
SYMMETRIC ENCRYPTION



ASYMMETRIC ENCRYPTION



DIGITAL SIGNATURES



2/ DIGITAL SIGNATURES

DIGITAL SIGNATURES: WHAT ARE THEY

Aim to be the electronic equivalent of hand-written signatures

- Intent: **signer's endorsement of the content**
- Integrity: authenticity of content
- Identity: authenticity of origin
- Time: authenticity of signing time
- Non-repudiation: **signer can't deny a signature afterwards**

DIGITAL SIGNATURES: USE-CASES

Relying party (recipient of a signed document) can:

- Verify the authenticity of the document for themselves
- Prove the authenticity of the document to third parties

Main use case types:

- Document signing
- Access control

DIGITAL SIGNATURES: MATHEMATICAL MODEL

- + Each signer has two related keys:
 - Private key for creating signatures
 - Public key for verifying signatures

- + A signature scheme consists of three algorithms:
 - Key generation: creates a pair of related keys
 - Signing: gets a document and a private key and creates a signature
 - Verifying: gets a document, a signature, and a public key; checks whether the signature was created with the private key corresponding to the public key

DIGITAL SIGNATURES: SECURITY MODEL

- + For a signature scheme to be secure, it must be infeasible for an attacker to:
 - Change the document without making the verification fail
 - Derive the private signing key from the public verification key
 - Create a signature without access to the private key

- + **Also need to make sure unauthorized parties can't access the private key:**
 - Best practice to generate the key pair in a secure hardware module
 - Only the public key is exported, the private key never leaves the module
 - For signing, data is sent to the module and signature exported

DIGITAL SIGNATURES: SIGNER IDENTITY

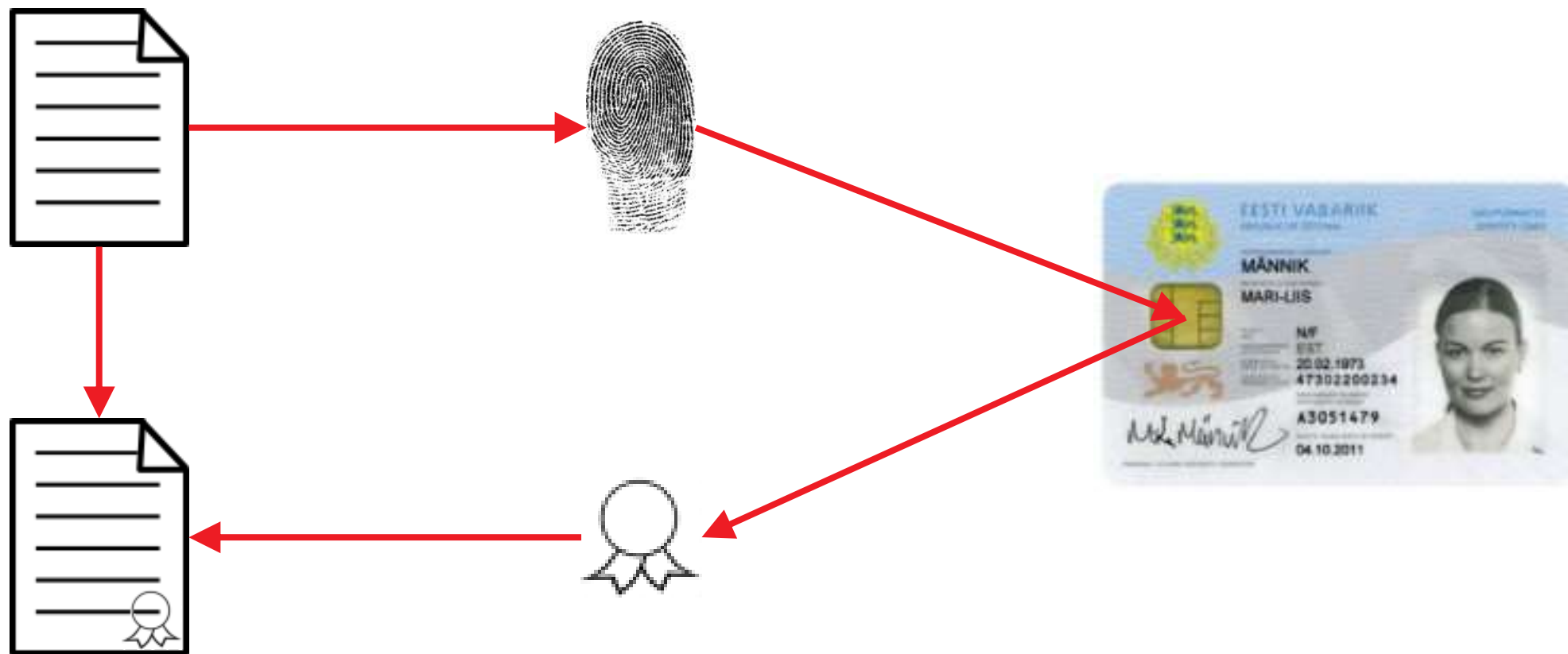
- + A public key is just a piece of data: large random-looking number
- + To authenticate the origin, public keys must be bound to the identities of their holders:
 - The key holder hands the public key directly to the relying party:
Mostly used in access control systems
 - Identity of key holder witnessed by someone the relying party knows:
Used in the PGP web of trust system, for example
 - Identity of key holder witnessed by a designated authority:
Used in the PKI model, where certificates are statements binding public keys to the identities of their holders, signed by dedicated certificate authorities

DIGITAL SIGNATURES: SIGNING TIME

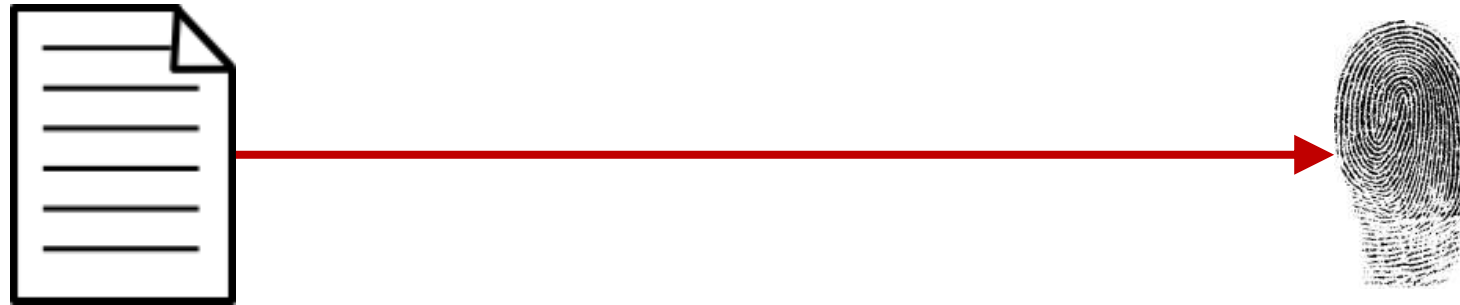
- + Often, digital signature systems must also prove signing time:
 - For legal reasons:
 - In most cases a signature is only valid if created in a specific time frame
 - **For example, a board member's authority to sign on behalf of the company**
 - For technical reasons:
 - When an unauthorized party gets the private key, the key must be revoked
 - But this should not be a way for the key holder to disown all previous signatures
 - Need to be able to distinguish between signatures created before and after the key was revoked
- Usually done with the help of time-stamping services

3/ HASH FUNCTIONS

DIGITAL SIGNATURES IN PRACTICE



HASH FUNCTIONS



PROPERTIES OF HASH FUNCTIONS

- + Efficiently computable
 - Given x , easy to compute $y = f(x)$
- + Pre-image resistant
 - Given y , infeasible to find x such that $f(x) = y$
- + Second pre-image resistant
 - **Given x , infeasible to find $x' \neq x$ such that $f(x') = f(x)$**
- + Collision resistant
 - Infeasible to find $x_1 \neq x_2$ such that $f(x_1) = f(x_2)$

SECOND PRE-IMAGE RESISTANCE

Bob

- Creates the contract X
- Signs it via $h(X)$
- Gives it to Alice

Alice

- **Modifies X to X',**
with $h(X') = h(X)$
- **Claims Bob signed X'**

Forgery after signing



X = "I owe Alice \$10"



X' = "I owe Alice \$1000"

$h(X) = h(X')$

COLLISION RESISTANCE

Alice

- Creates X_1 and X_2 with $h(X_1) = h(X_2)$

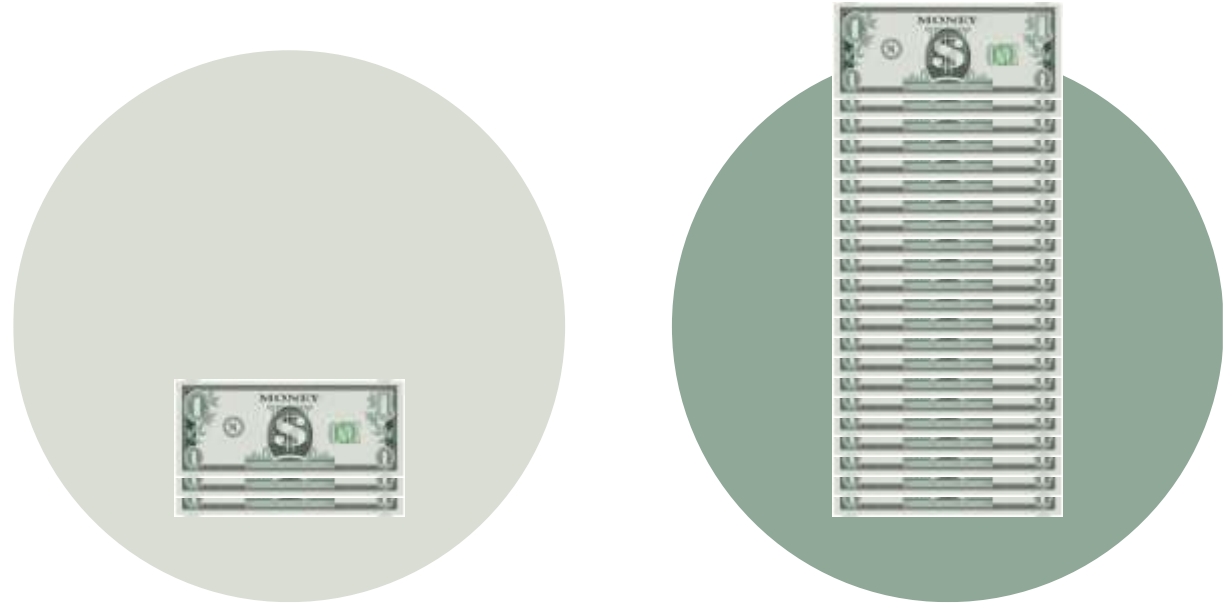
Bob

- Signs X_1 via $h(X_1)$

Alice

- Claims Bob signed X_2

Forgery before signing

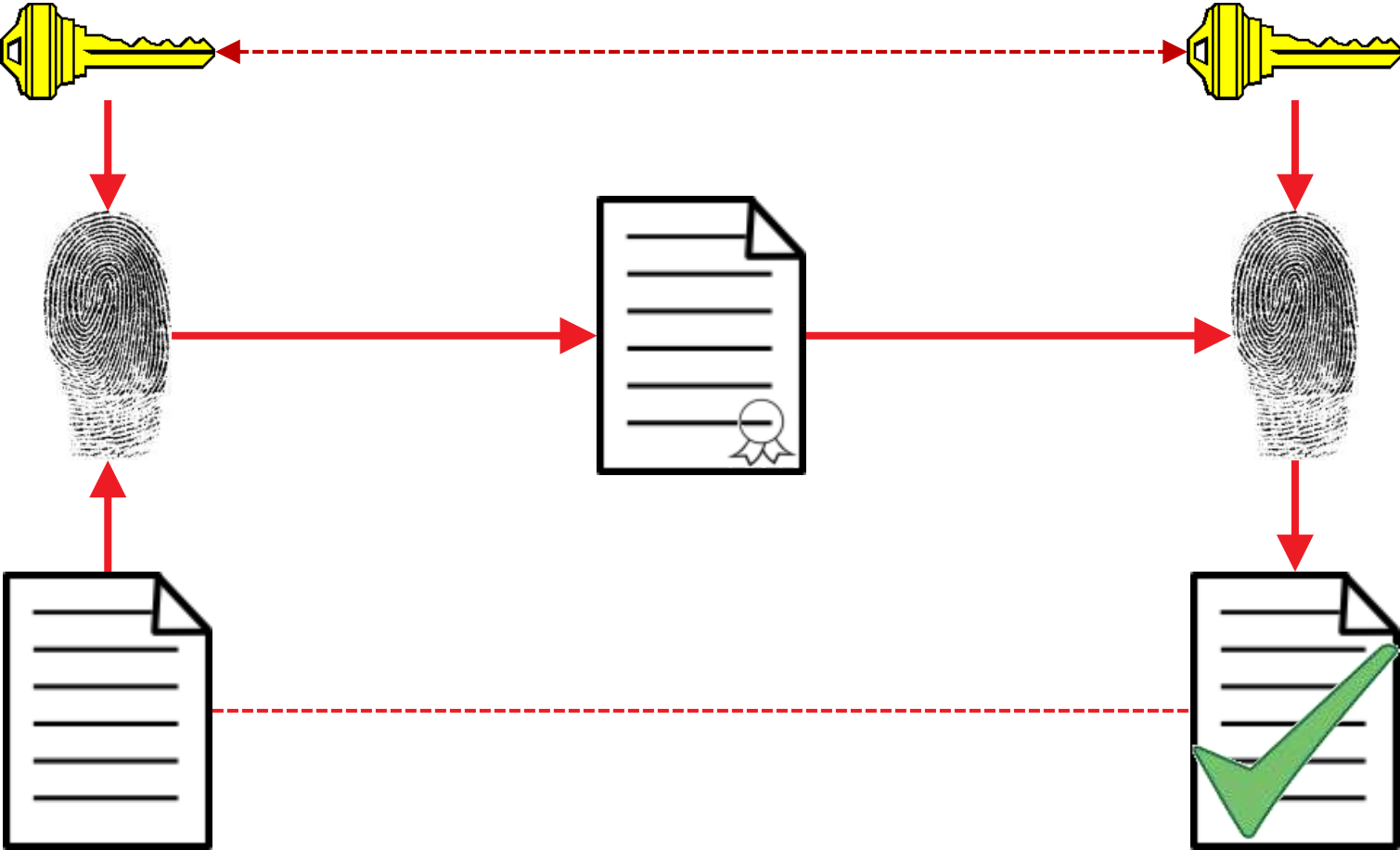


$X_1 = \text{"Bob owes me \$10"} \quad X_2 = \text{"Bob owes me \$1000"}$

$h(X_1) = h(X_2)$

4/ HASH SIGNATURES

MESSAGE AUTHENTICATION CODES



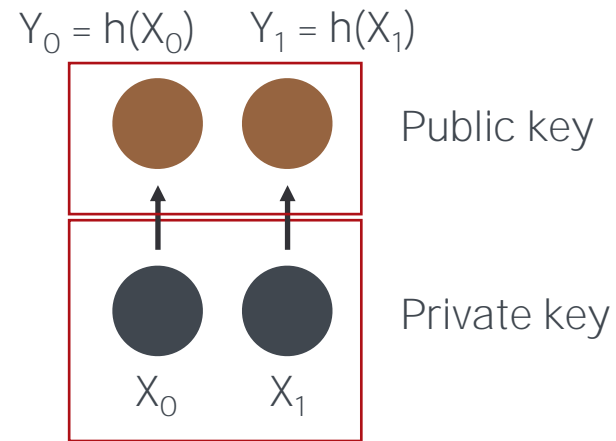
LAMPORT SIGNATURES

+ 1-bit case

- Private key (X_0, X_1)
- Public key (Y_0, Y_1)
- Signature on 0: X_0
(destroy X_1)
- Signature on 1: X_1
(destroy X_0)

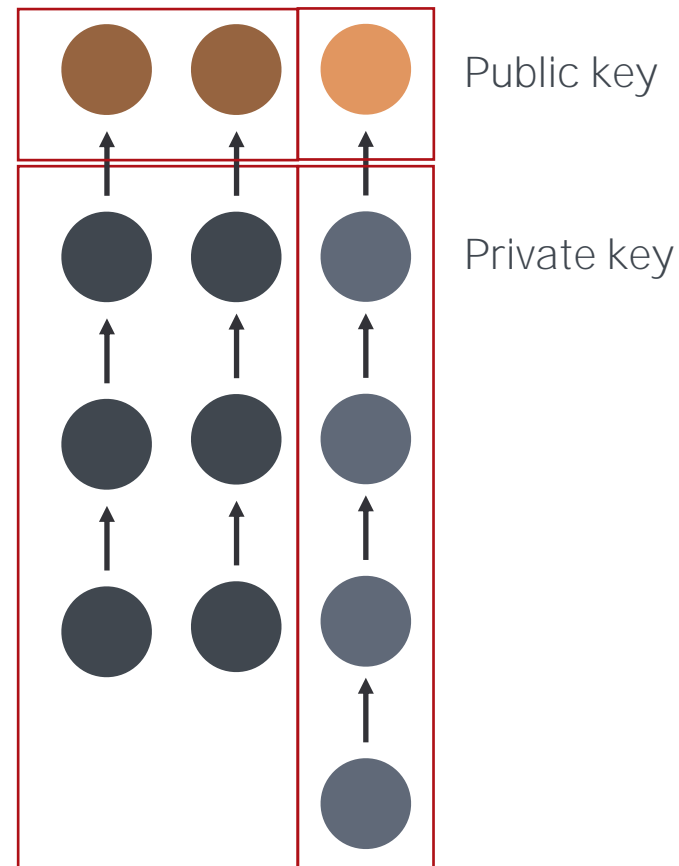
+ Longer inputs

- Sign each bit
separately



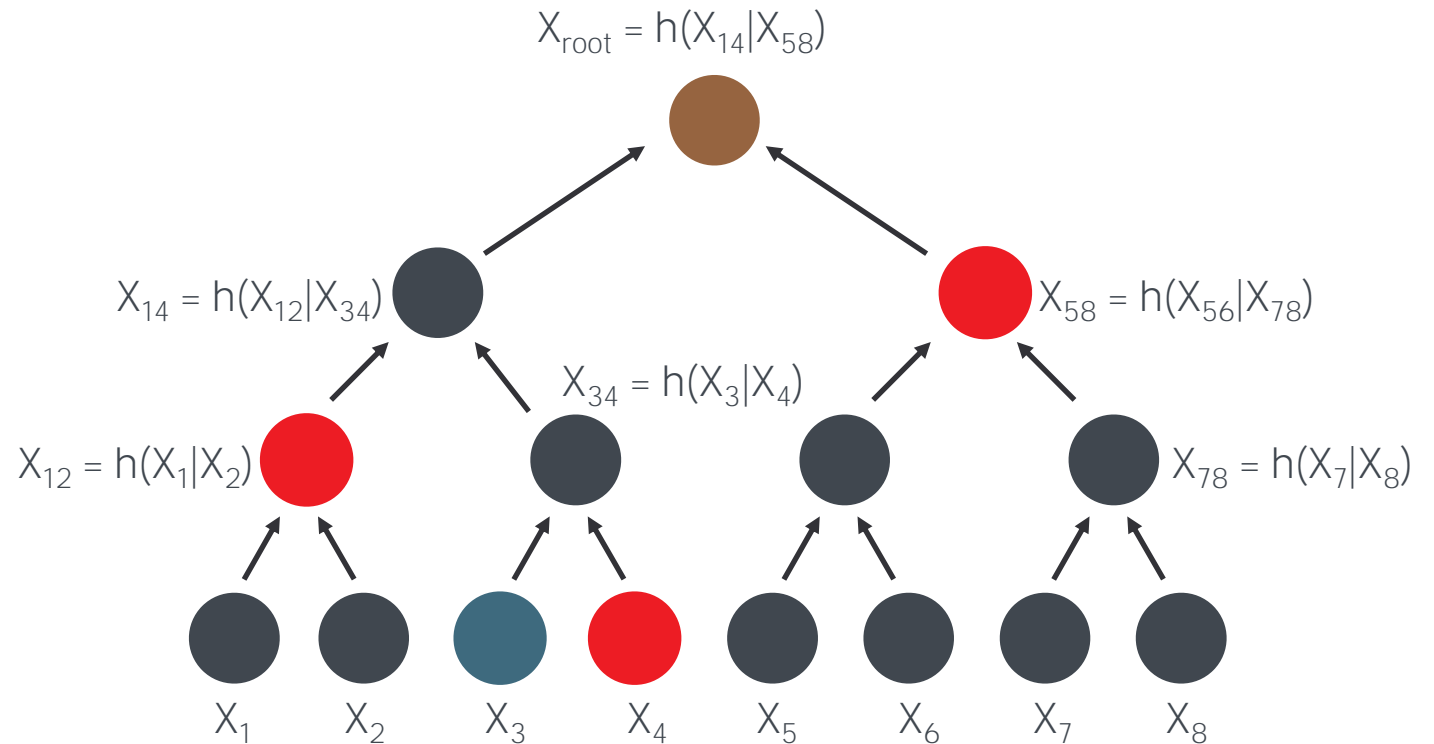
WINTERNITZ SIGNATURES

- + W -bit groups
 - 2^W -step hash chains
 - $X_i = h(X_{i-1})$
 - Signature on value k : X_k
- + Checksum
 - Sign the total number of steps to public key components



MERKLE TREES

- + A hash tree, or a Merkle tree, aggregates many inputs into a single hash value
- + Afterwards, a compact proof of participation can be extracted for each input

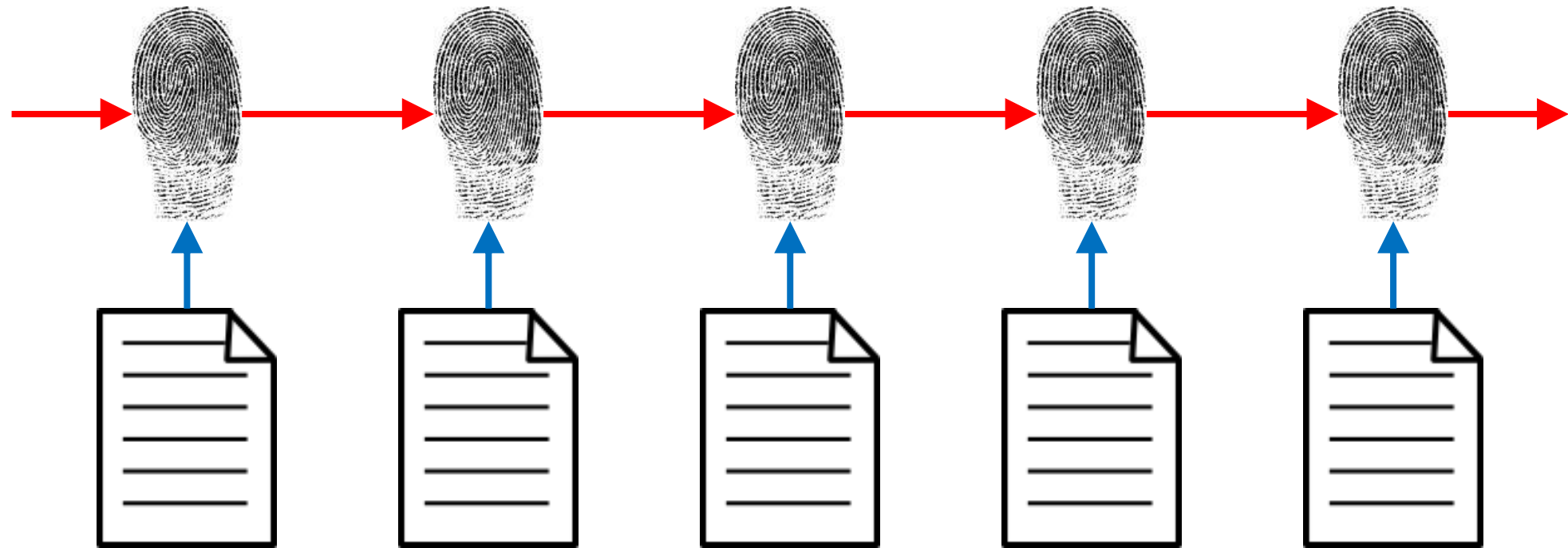


5/ TIME-STAMPING

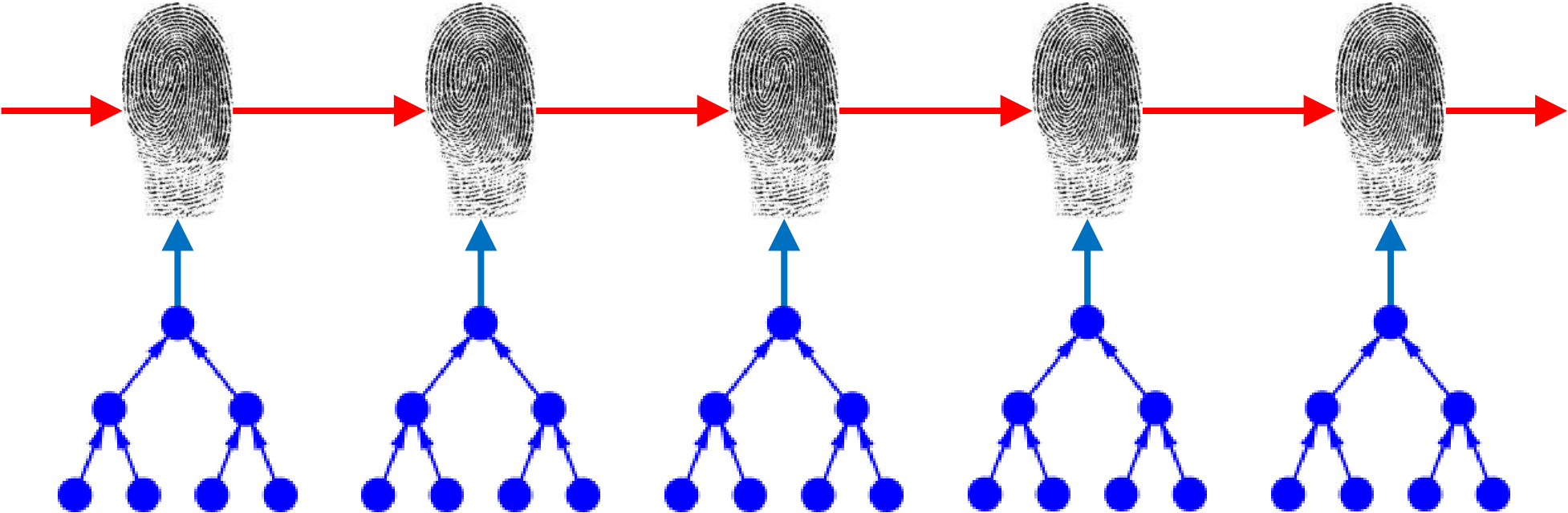
HASH-THEN-PUBLISH TIME-STAMPING

- + To prove the existence of some information: publish it
- + If the information is confidential: publish a hash instead
 - Can later reveal the information and show it matches the hash
- + Galileo, Hooke

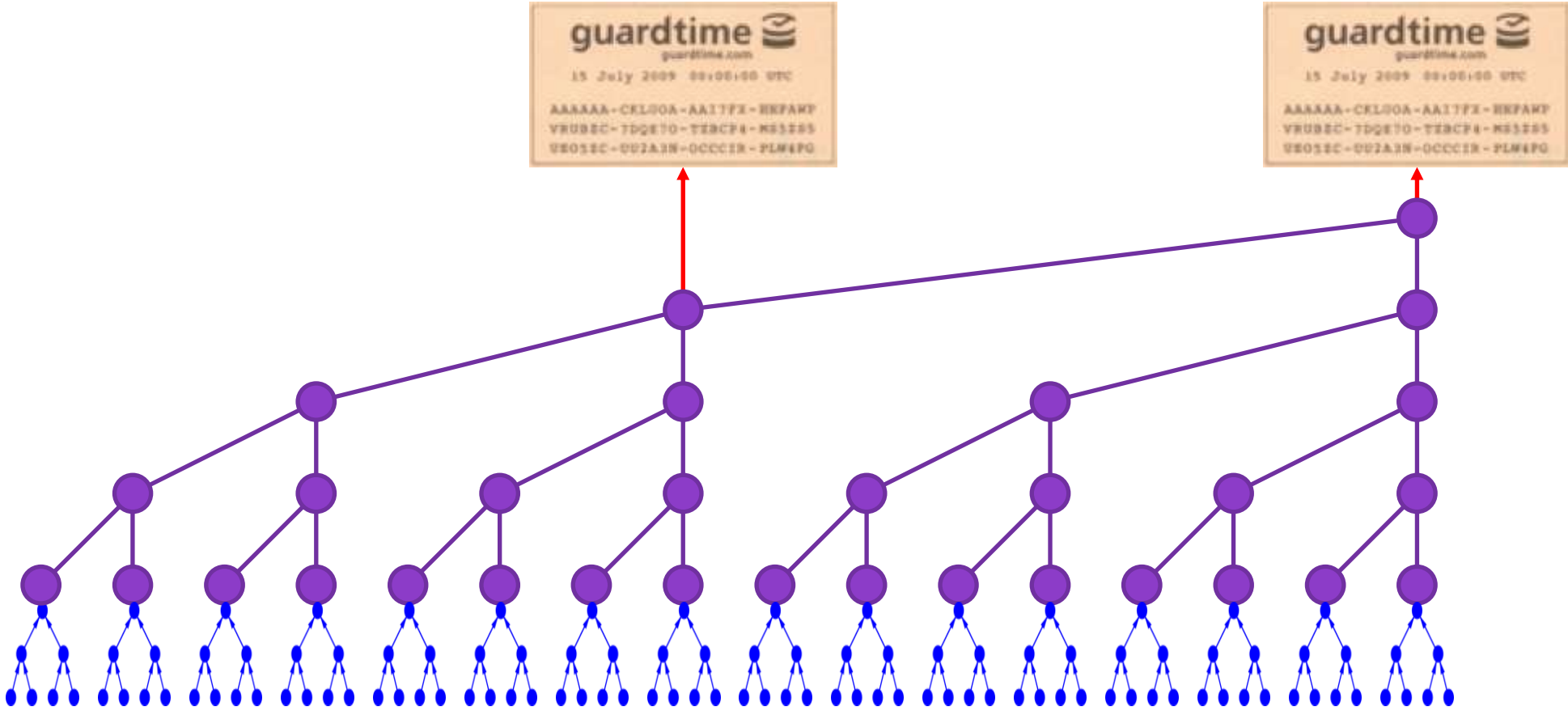
PUBLISHING TO HASH-LINKED LEDGER



HASH-TREE AGGREGATION OF INPUTS



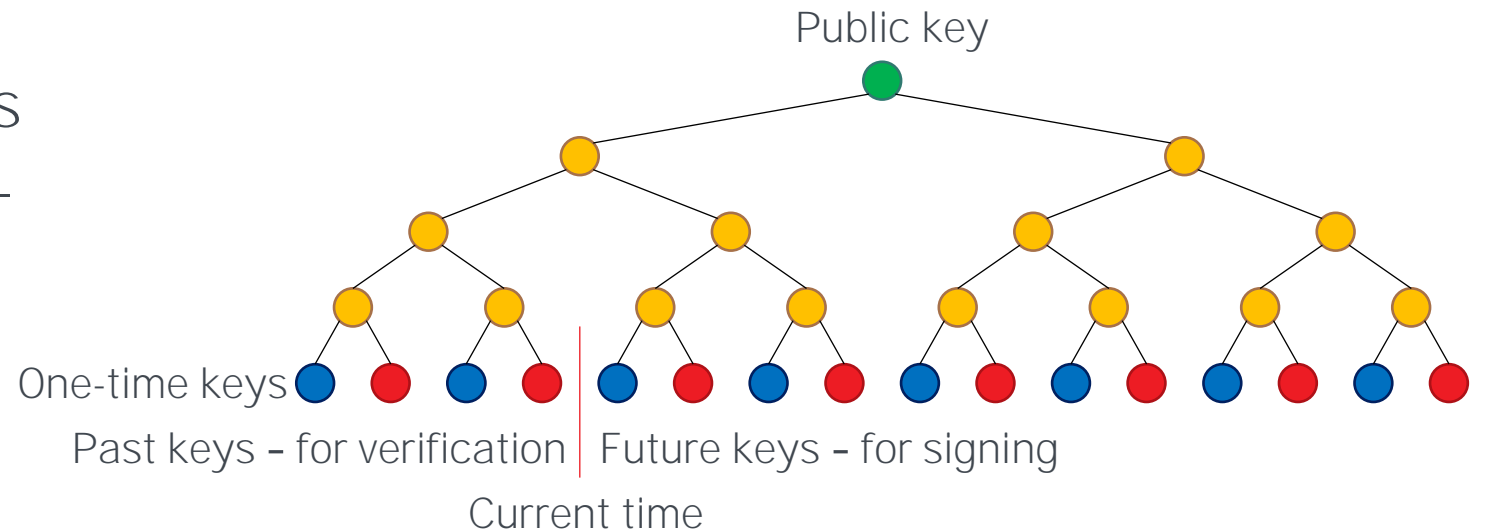
HASH-TREE AGGREGATION OF LEDGER



6/ BLT SIGNATURES

BLT-TB: TIME-BOUND KEYS

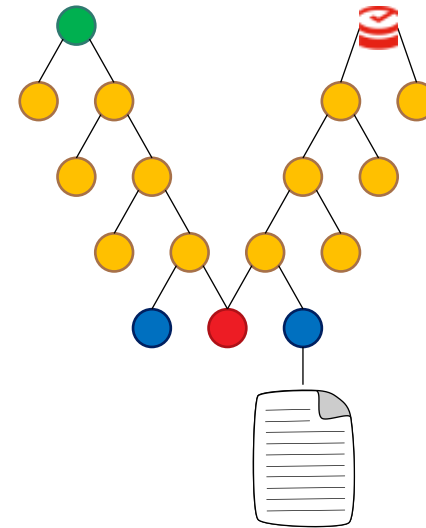
- + One-time keys for message authentication
- + Message authentication is symmetric and lacks non-repudiation
- + Use time to break the symmetry



BLT-TB: SIGNING

To sign a document at a given time:

- Authenticate the document with the corresponding one-time key
- Time-stamp the authenticator to prove the signing time
- Include proof of the key-time binding in the signature

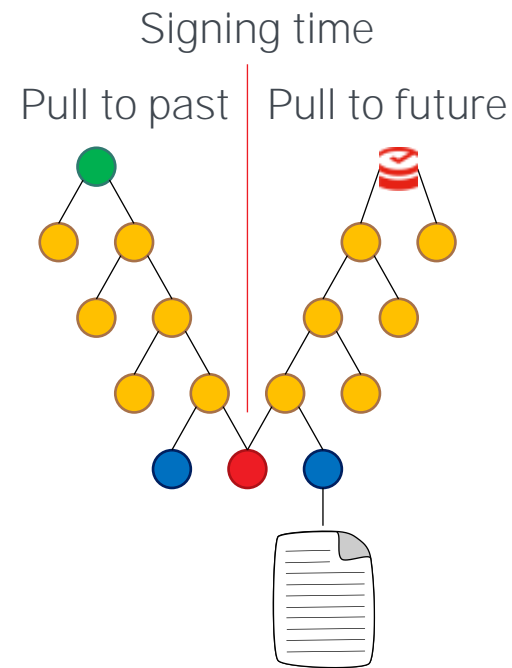


BLT-TB PROPERTIES

- Keys pre-generated for each possible signing time
- Suitable for full-size computers that have
 - Reasonable computing power
 - Reliable clocks
 - Direct network access
- Suitable for applications that need to sign often
 - Ideal for server applications used by many clients

NEW CONCEPT: FORWARD-RESISTANT TAGS

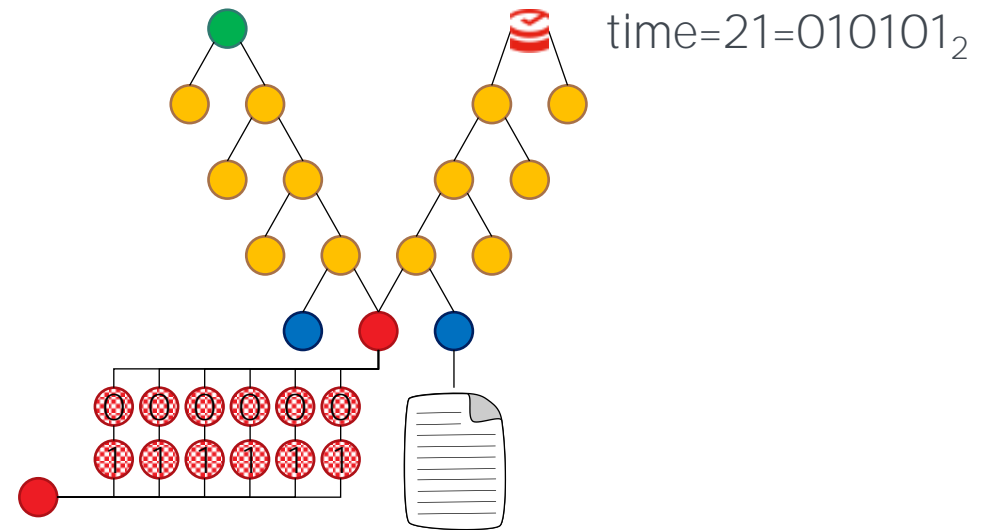
- Pre-binding keys to time slots is wasteful
- Time-stamp already prevents moving the signing event to past
- So, the key binding only needs to prevent moving to future
- So, we can relax the requirement on the key binding



BLT-OT: ONE-TIME KEYS

Inspired by **Lamport's** signatures

- Generate a multi-component private key
- Bind it to time after time-stamping
- The time value is shorter than a hash value, so less components are needed
- Extra optimization: generate all the key components from a single seed
- Can pre-generate several such keys and use them in sequence



REFERENCES

- + BLT-TB scheme in more detail
<https://eprint.iacr.org/2019/671>
- + BLT-OT scheme in more detail
<https://eprint.iacr.org/2019/673>



THANK YOU
QUESTIONS?

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