

Local (“Arena”) Memory Allocators

John Lakos

Thursday, April 27, 2017

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Abstract

The runtime implications of the physical location of allocated memory are sometimes overlooked—even in the most performance-critical code. In this talk, we will examine how the performance of long-running systems can degrade when using just one global allocator (e.g., via `new/delete`). We will contrast the use of global allocators with various kinds of *local* allocators—allocators that allocate memory for a well-defined subset of objects in the system. We will also demonstrate how local allocators can reduce, if not entirely prevent, degradation seen in systems that rely solely on the global allocator. Six dimensions—*fragmentability*, *allocation density*, *variation*, *utilization*, *locality*, and *contention*—will be introduced to help characterize a given subsystem, assess the potential for accelerating its runtime performance, and—where appropriate—aid in determining the best local allocator to do so. **Empirical evidence** will be presented to demonstrate that introducing an appropriate local allocator can often result in substantial reductions in run times (compared with a similar system relying solely on just a single, global allocator).

Important Recurring Questions

Are memory allocators really worth the trouble?

- ❑ What situations merit their use?
- ❑ How are they applied effectively?
- ❑ What's the performance impact?

Outline

1. Introduction and Background

What are memory allocators, and why are they useful?

2. Understanding the Problem

What aspects of software affect allocation strategy?

3. Analyzing the Benchmark Data

When and how do you use which allocator, and why?

4. Conclusions

What must we remember about memory allocators?

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1. Introduction and Background

Important Questions

Why do we like the C++ language?

- ❑ It enables us to “fine-tune” at a low level when needed.
- ❑ It can deliver very high runtime performance.

1. Introduction and Background

Important Questions

Why do (should) we care about memory allocators?

- ❑ They enable us to “fine-tune” at a low level when needed.
- ❑ They can help to improve runtime performance.

1. Introduction and Background

Important Questions

What are the benefits?

- ❑ Not all memory is alike:
 - ✓ Fast, Shared, Protected, Mapped
- ❑ Other qualitative benefits:
 - ✓ Testing, Debugging, Measuring
- ❑ Enhanced runtime performance:
 - ✓ Better Locality, Less Contention

1. Introduction and Background
Important Questions

What are the benefits?

(anecdotal)

Bear Stearns (c. 1997)

System's (coalescing) allocator optimized for allocation, not deallocation.

1. Introduction and Background
Important Questions

What are the benefits?

(anecdotal)

Bloomberg (c. 2002)

Process (static) memory saved/restored
via memory-mapped IO.

1. Introduction and Background
Important Questions

What are the benefits?

(anecdotal)

Bloomberg (c. 2006)

User interfaces observed to be “zippier”
when using local allocator.

1. Introduction and Background

Important Questions

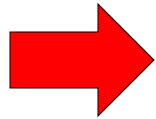
What are the common arguments against?

- ❖ Requires more up-front design effort
- ❖ Complicates user interfaces
- ❖ May actually degrade performance:
 - No special allocator needed
 - Poorly chosen allocator supplied

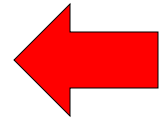
1. Introduction and Background

Addressing Allocator Concerns

These are valid concerns!



- ❖ Requires more up-front design effort
- ❖ Complicates user interfaces
- ❖ May actually degrade performance:
 - No special allocator needed
 - Poorly chosen allocator supplied



They can be addressed only with:

- Well-supported facts**
- Careful measurement**

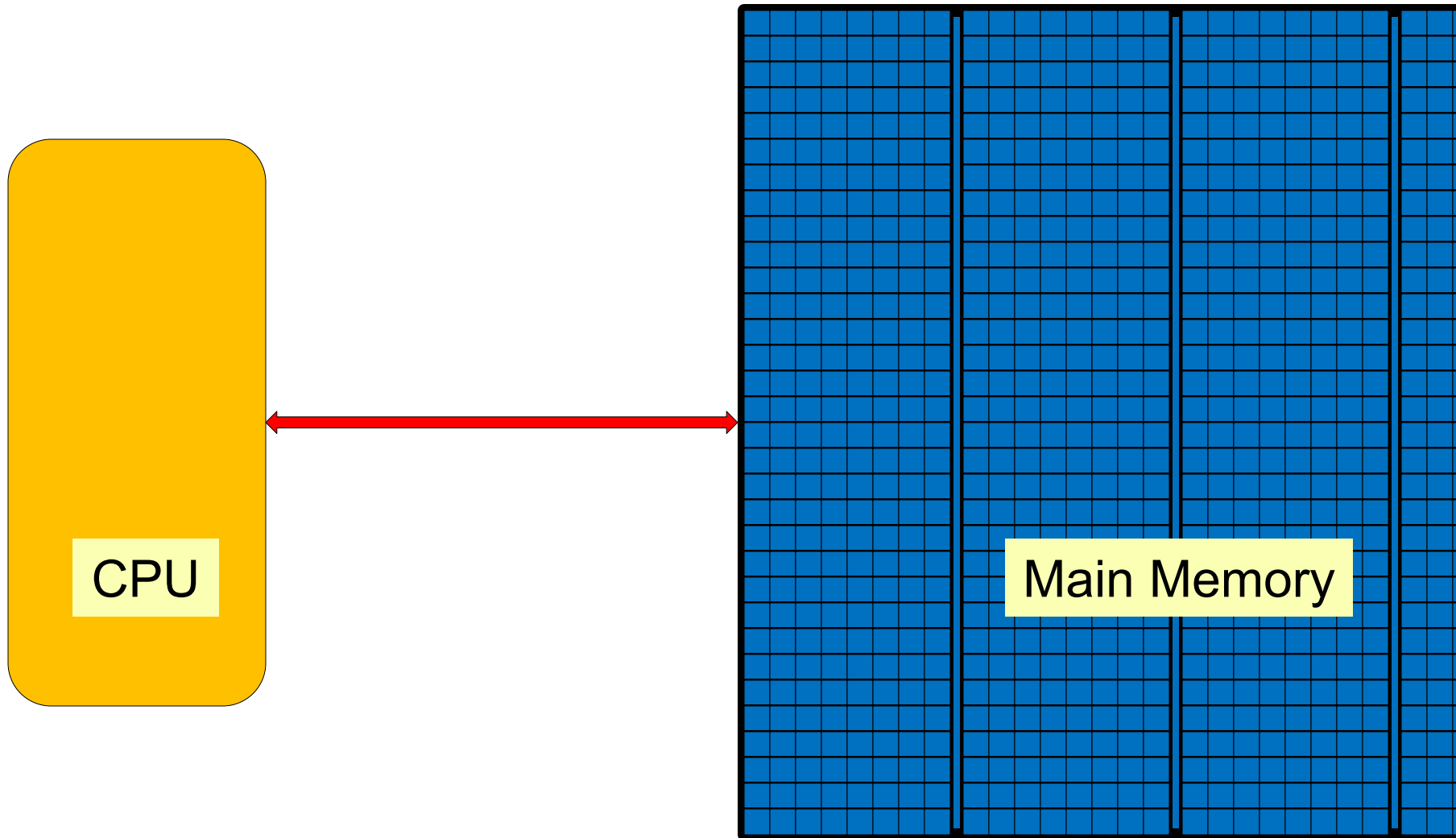
1. Introduction and Background

Review of Computer Memory

Main Memory

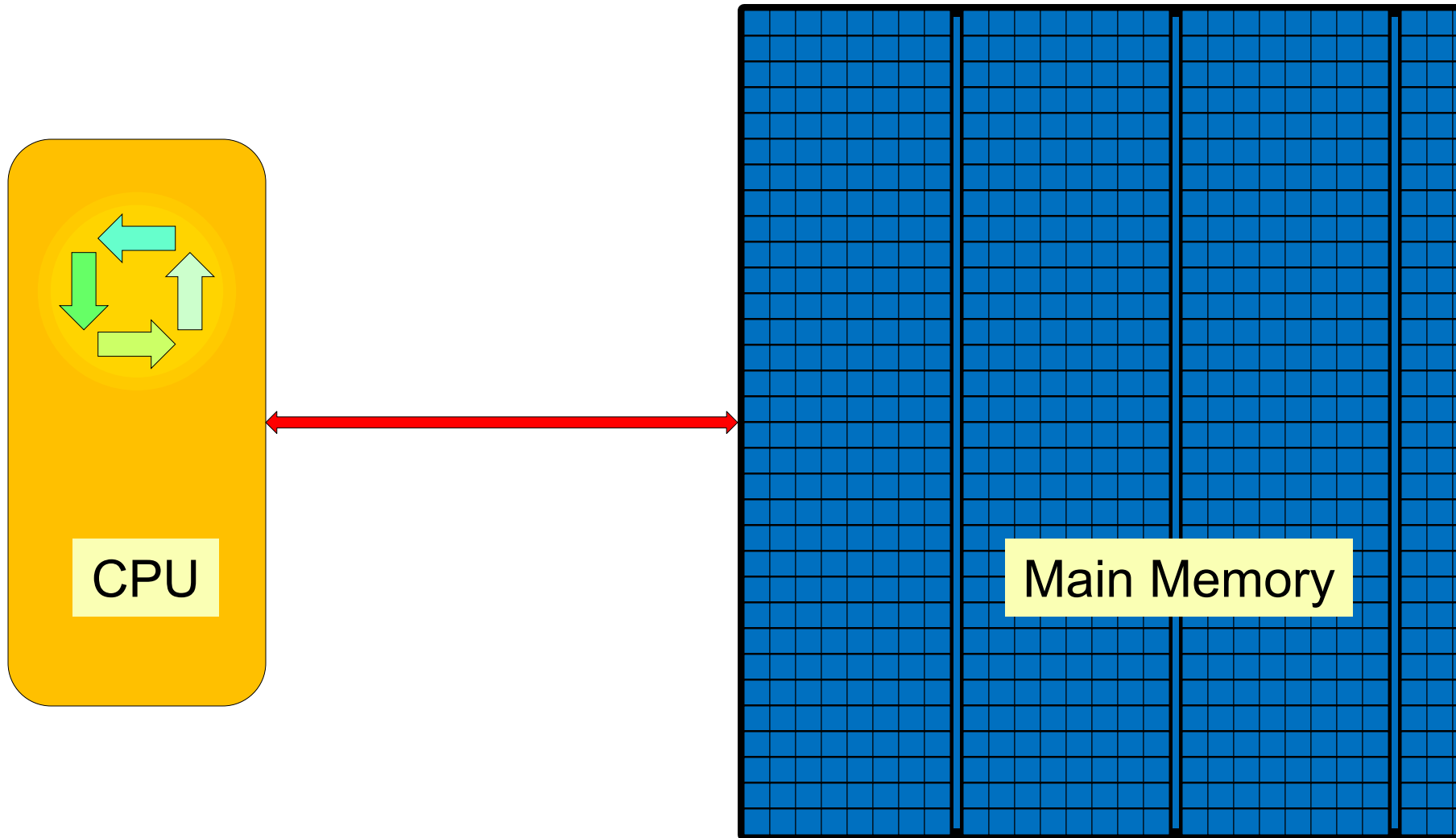
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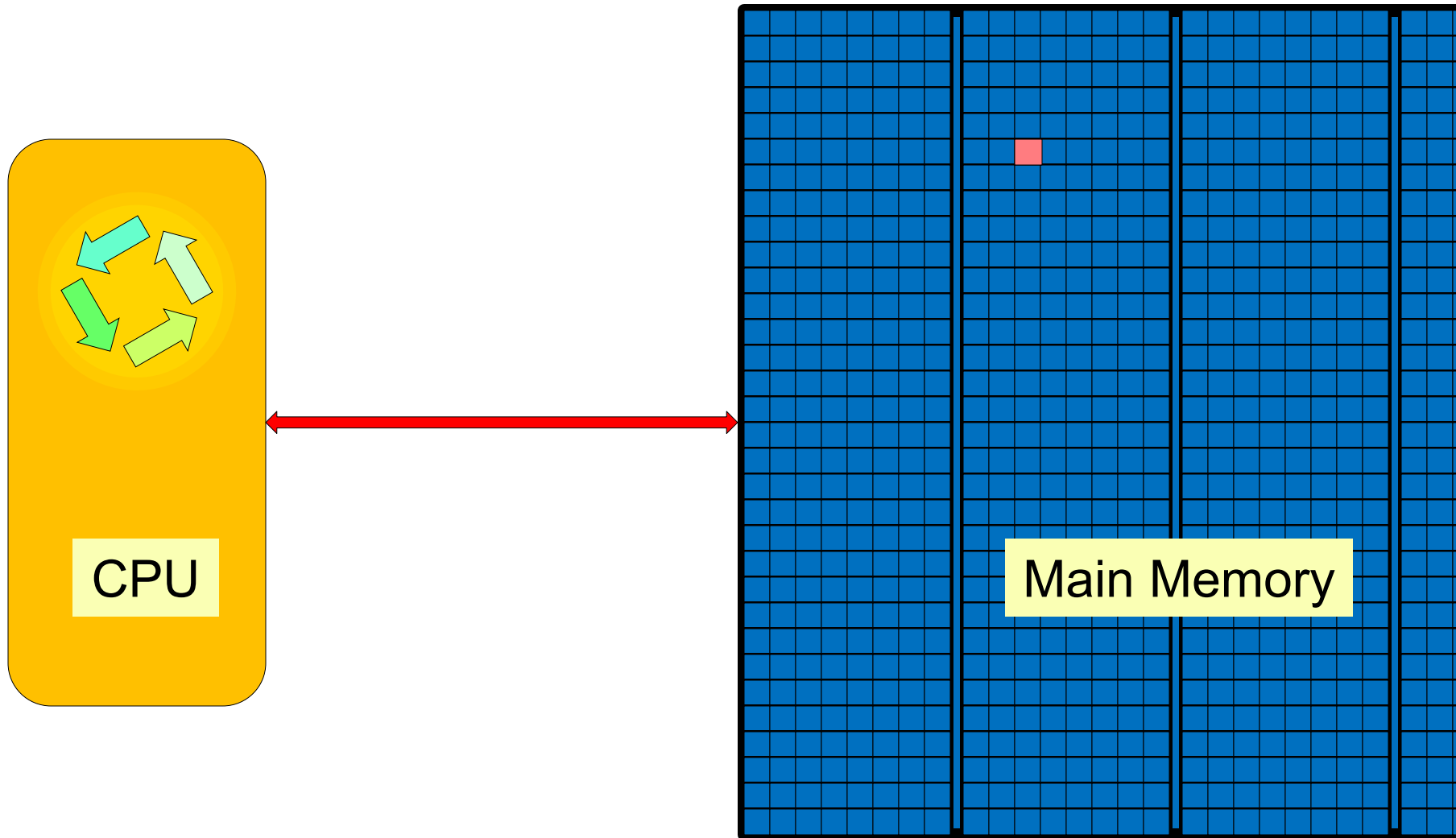
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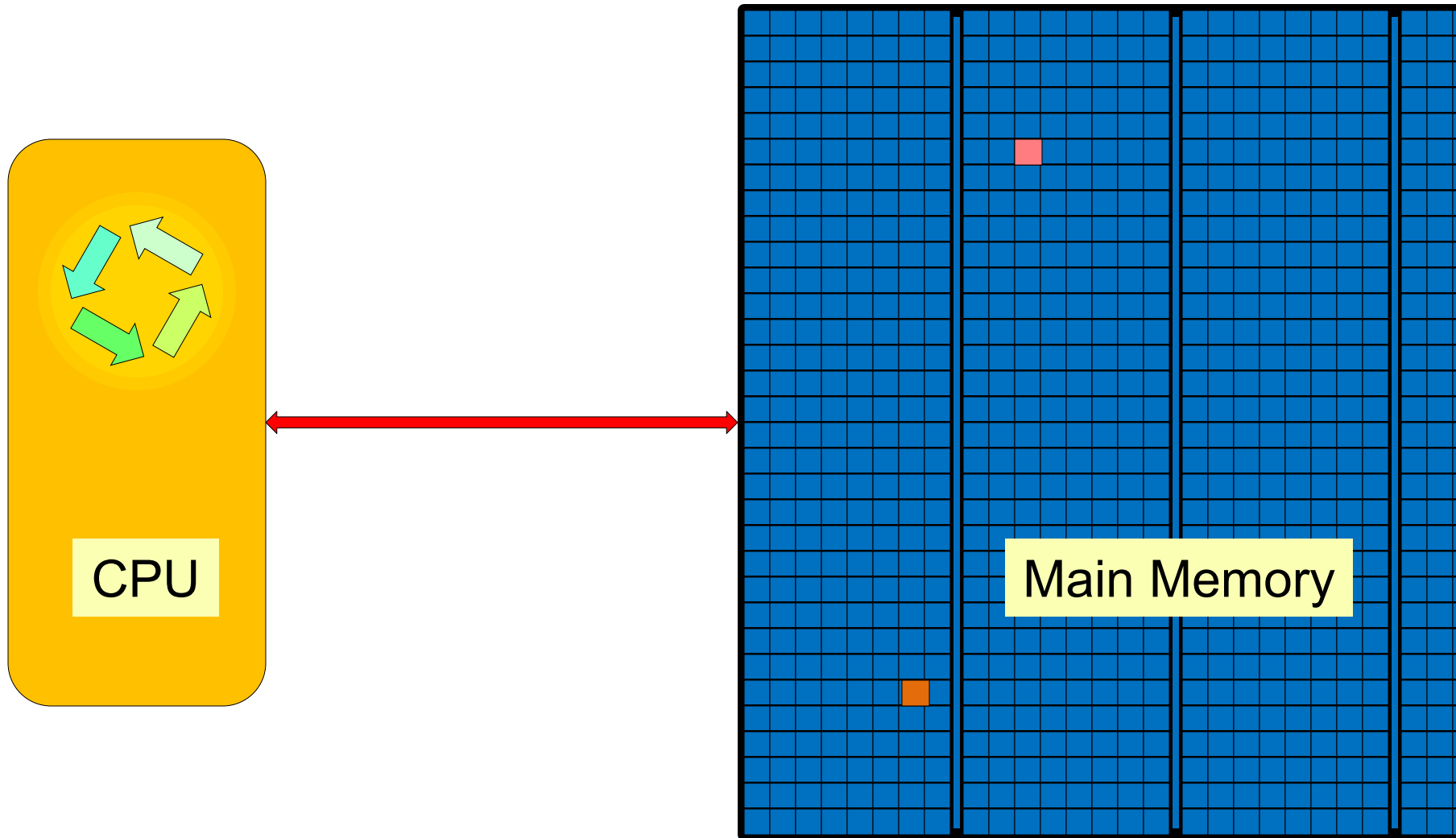
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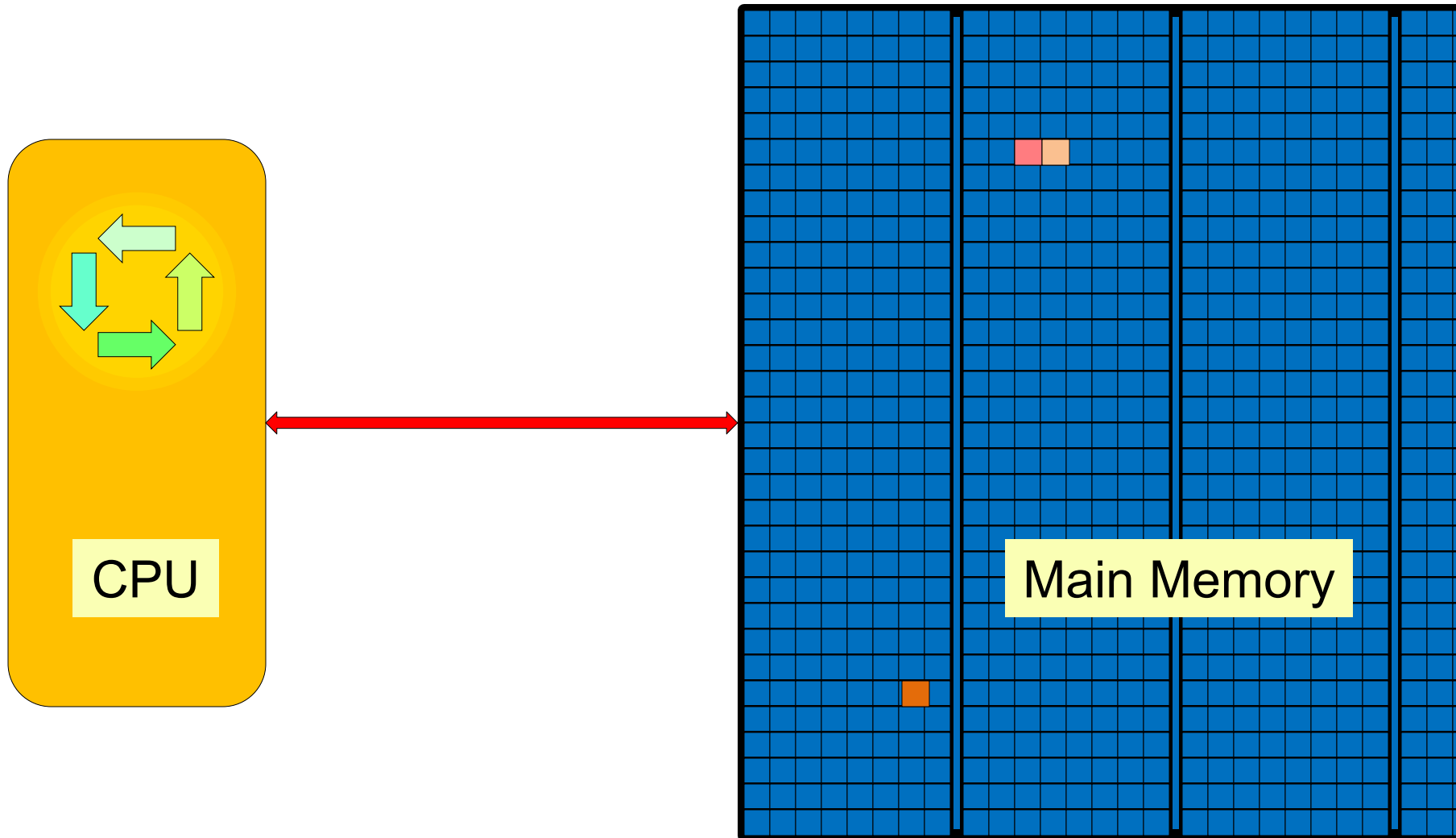
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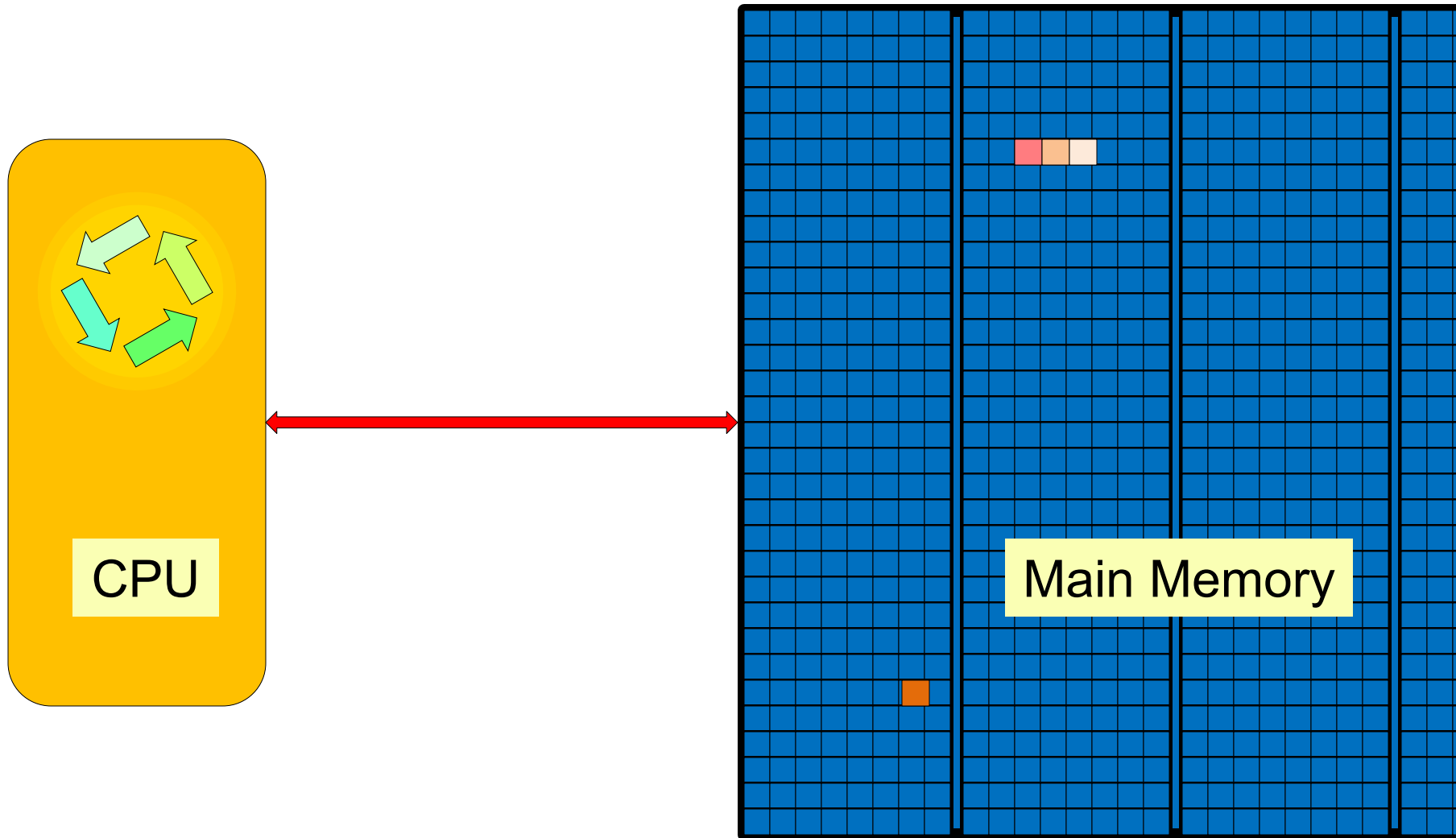
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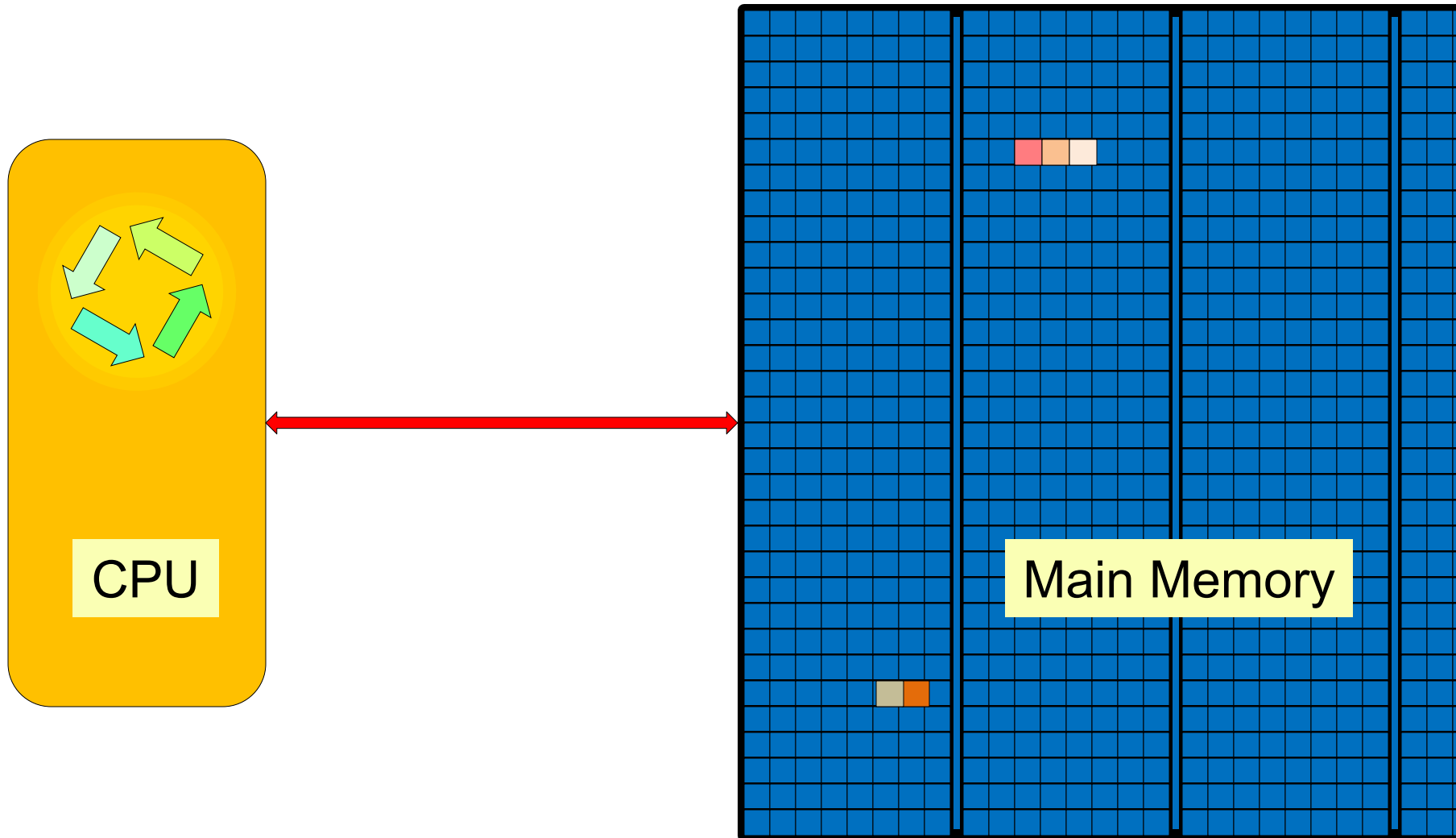
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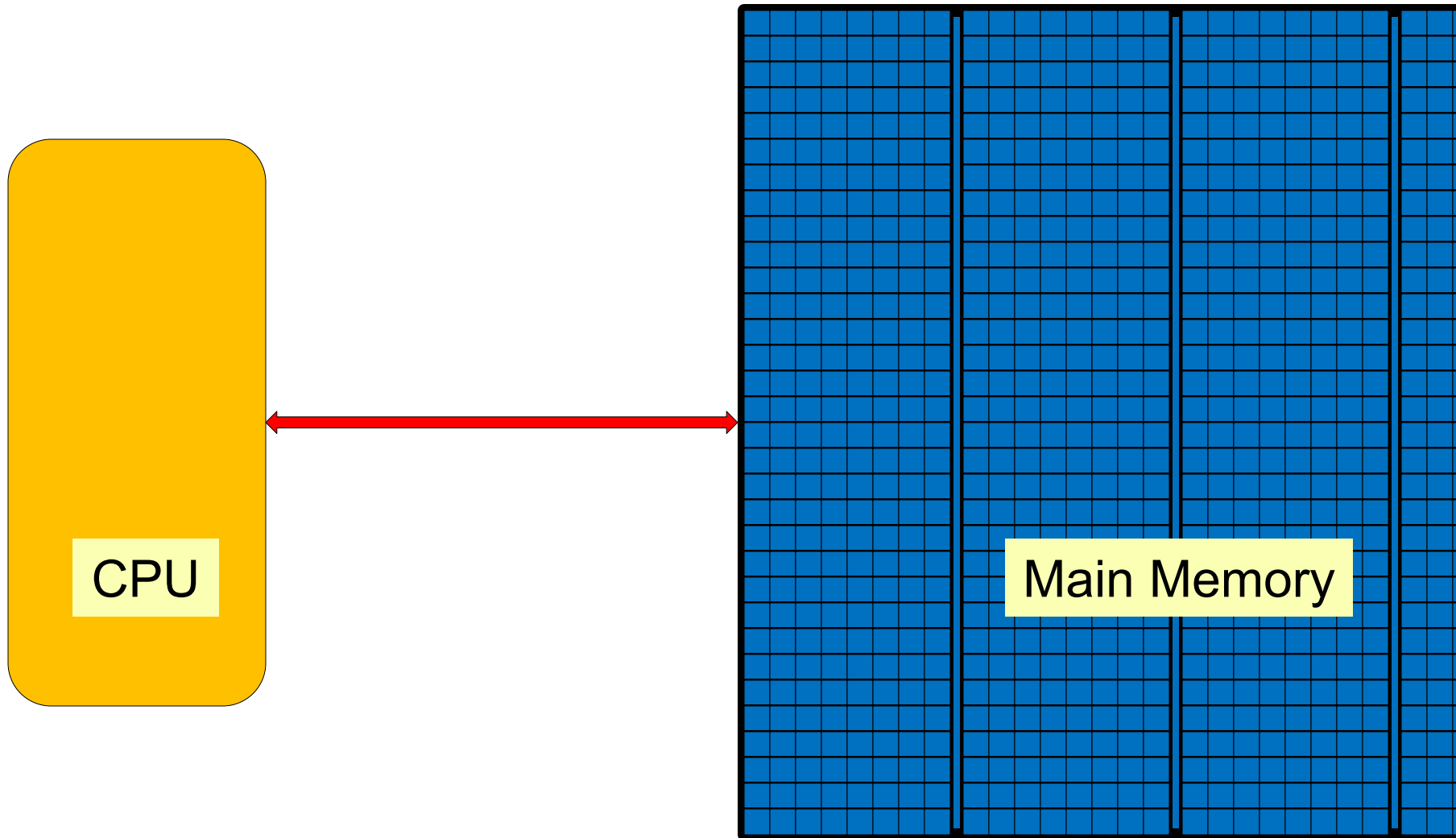
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Review of Computer Memory

Cache Memory

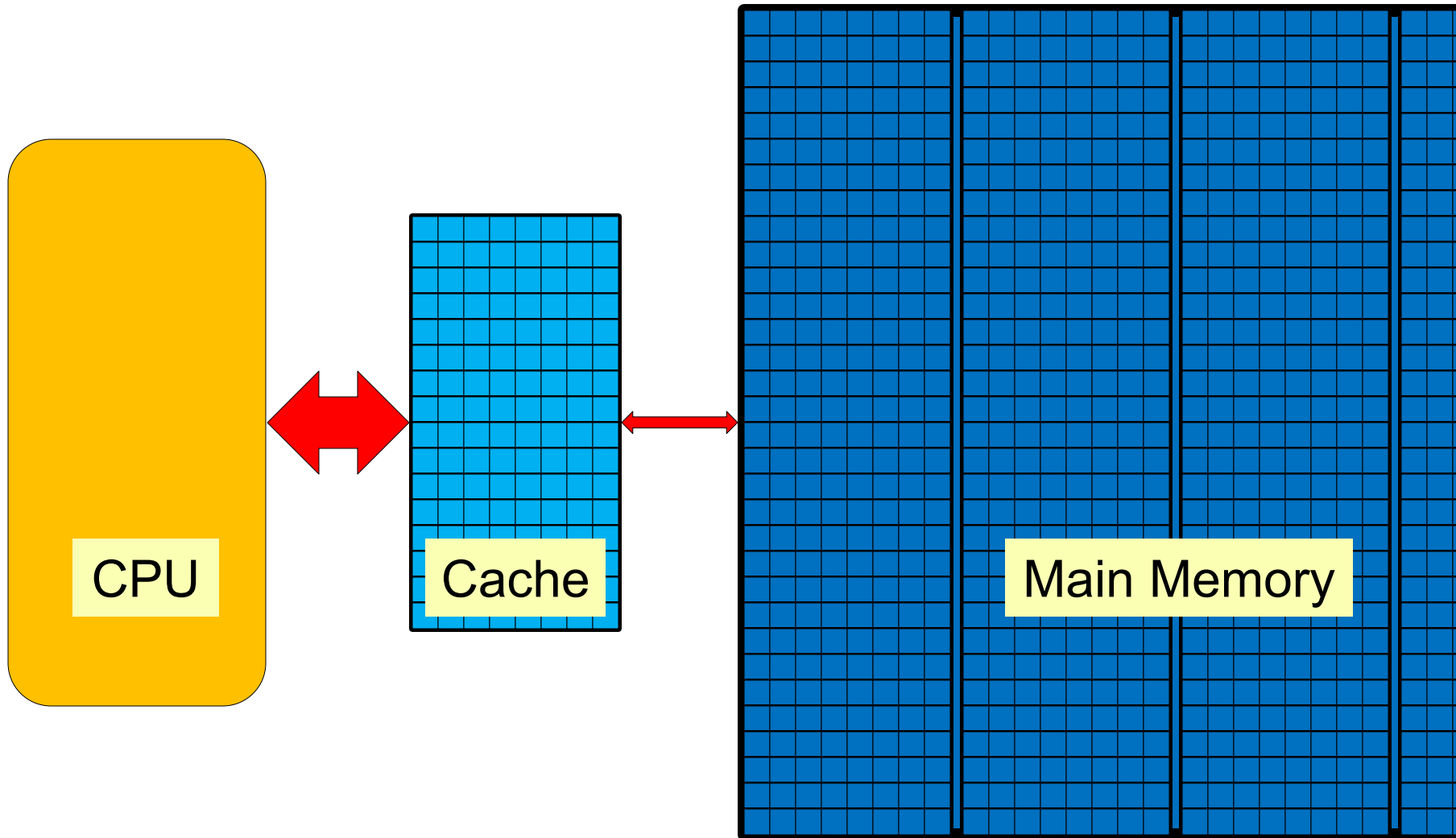
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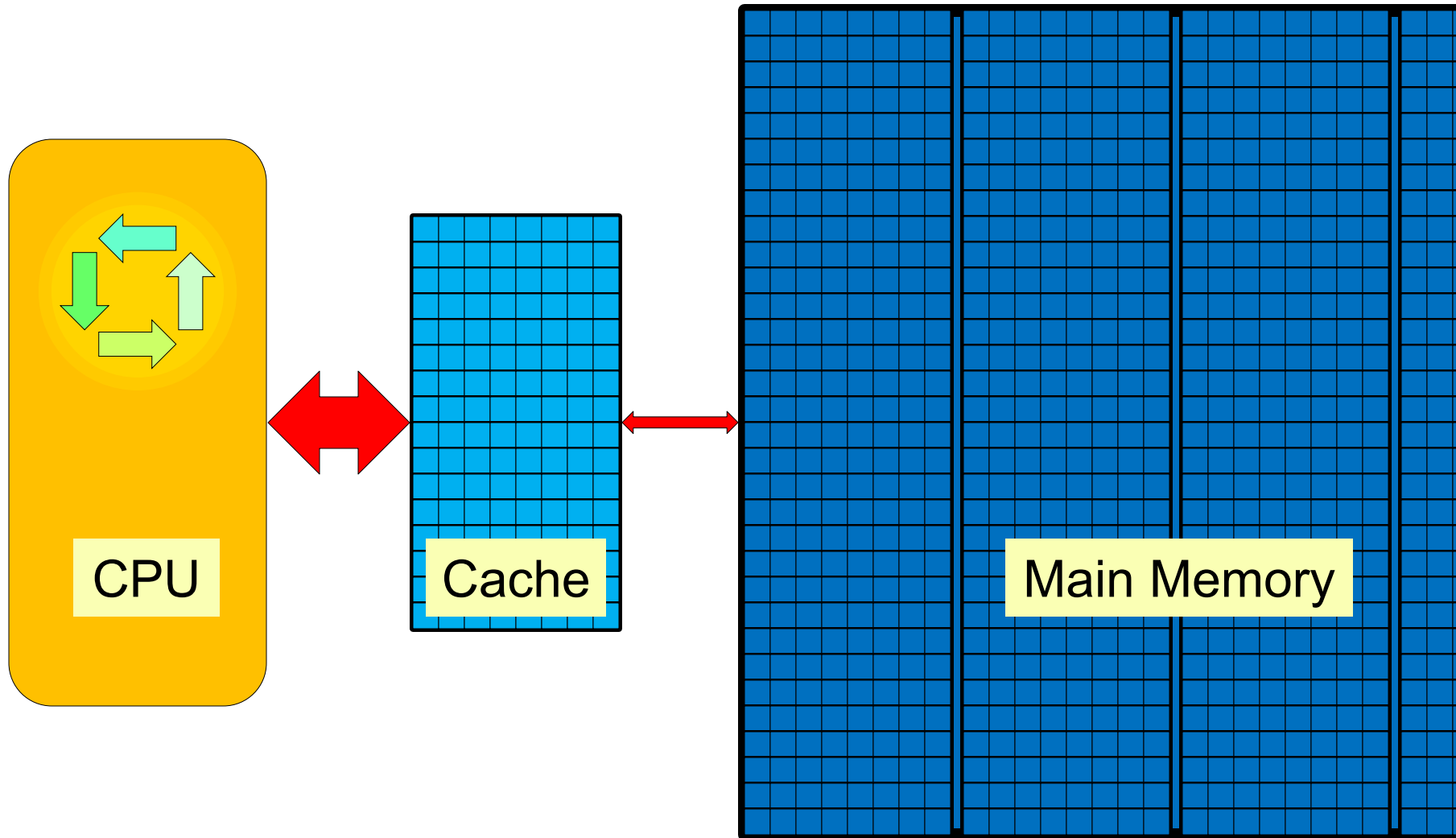
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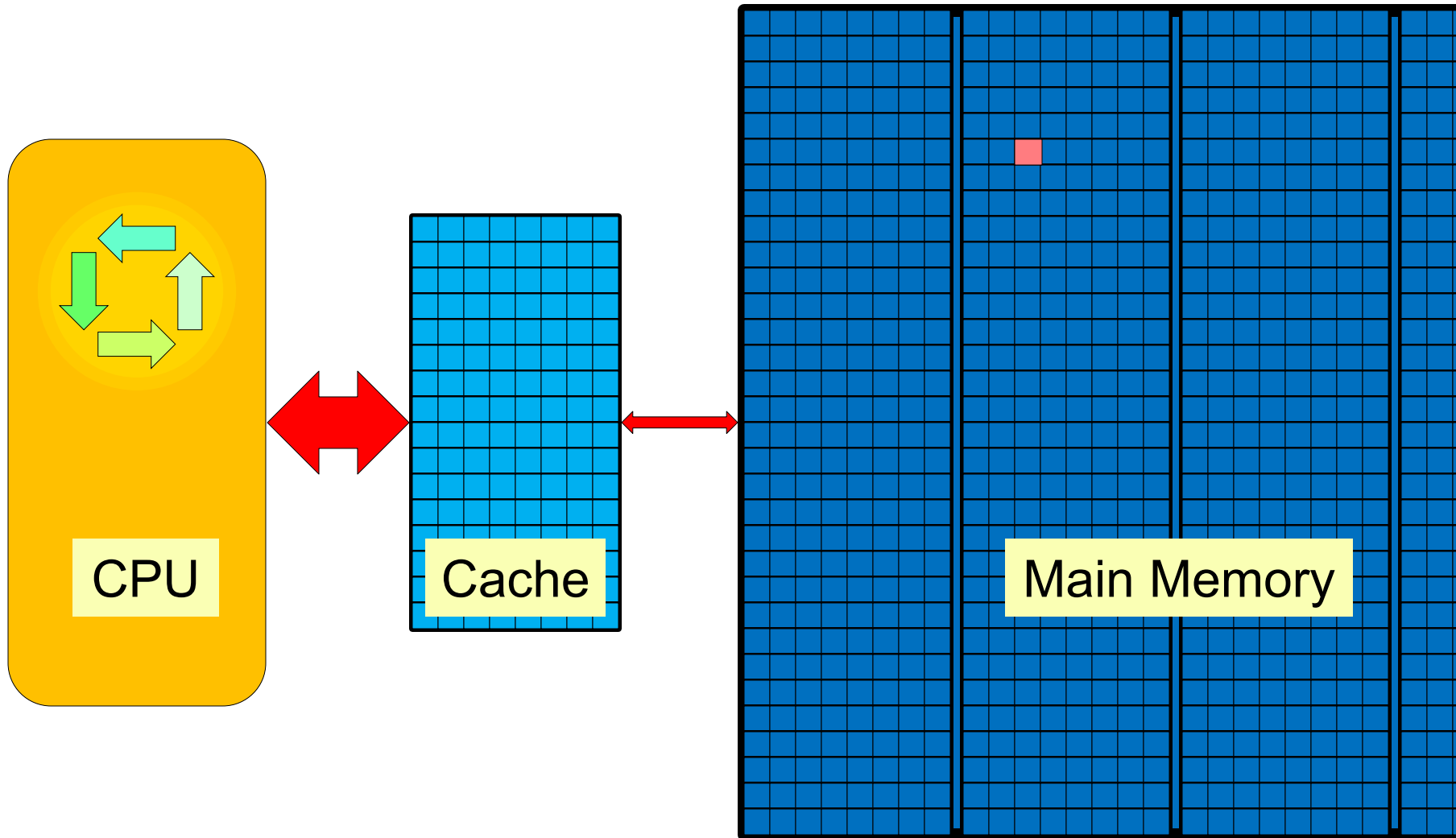
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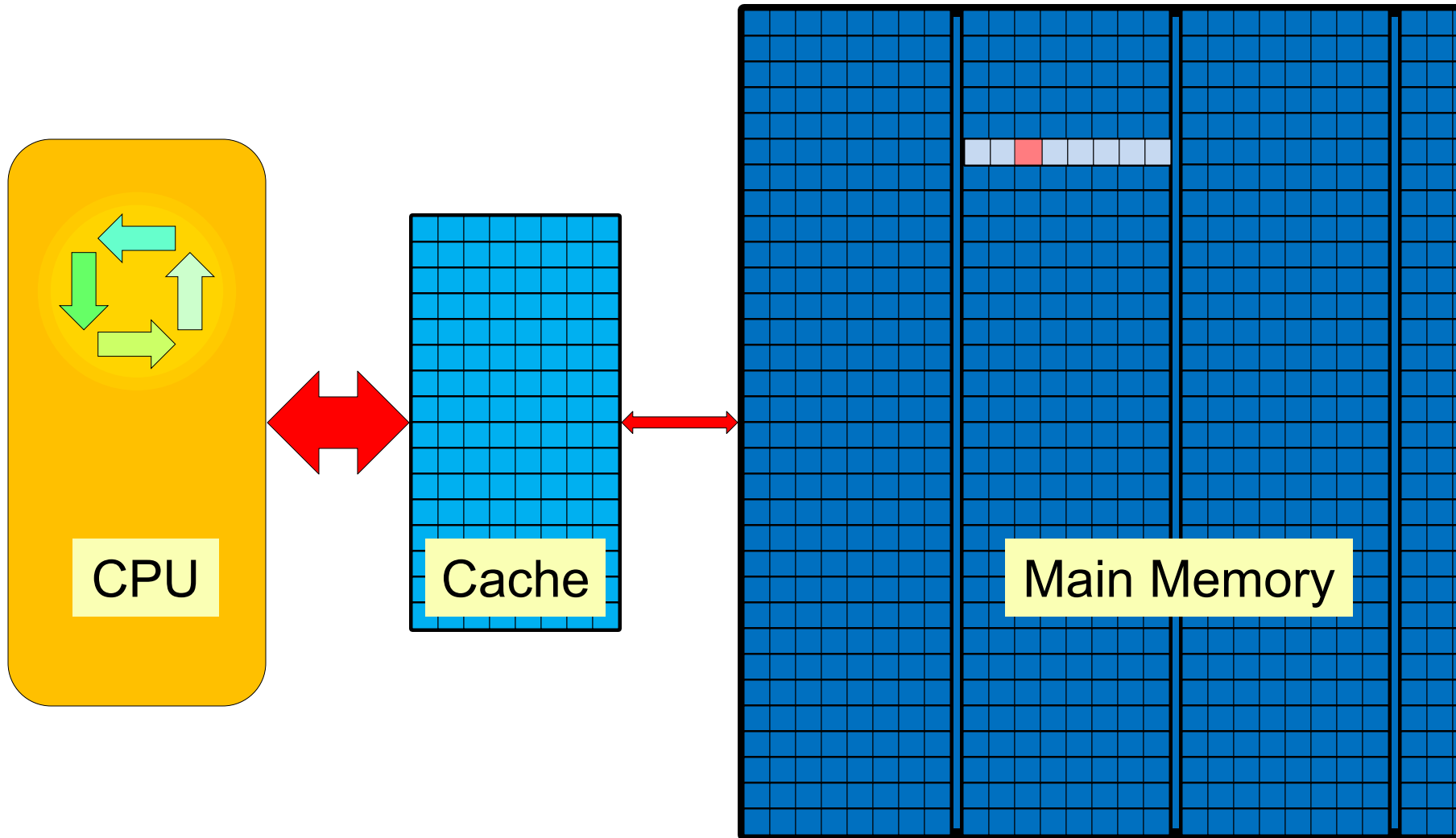
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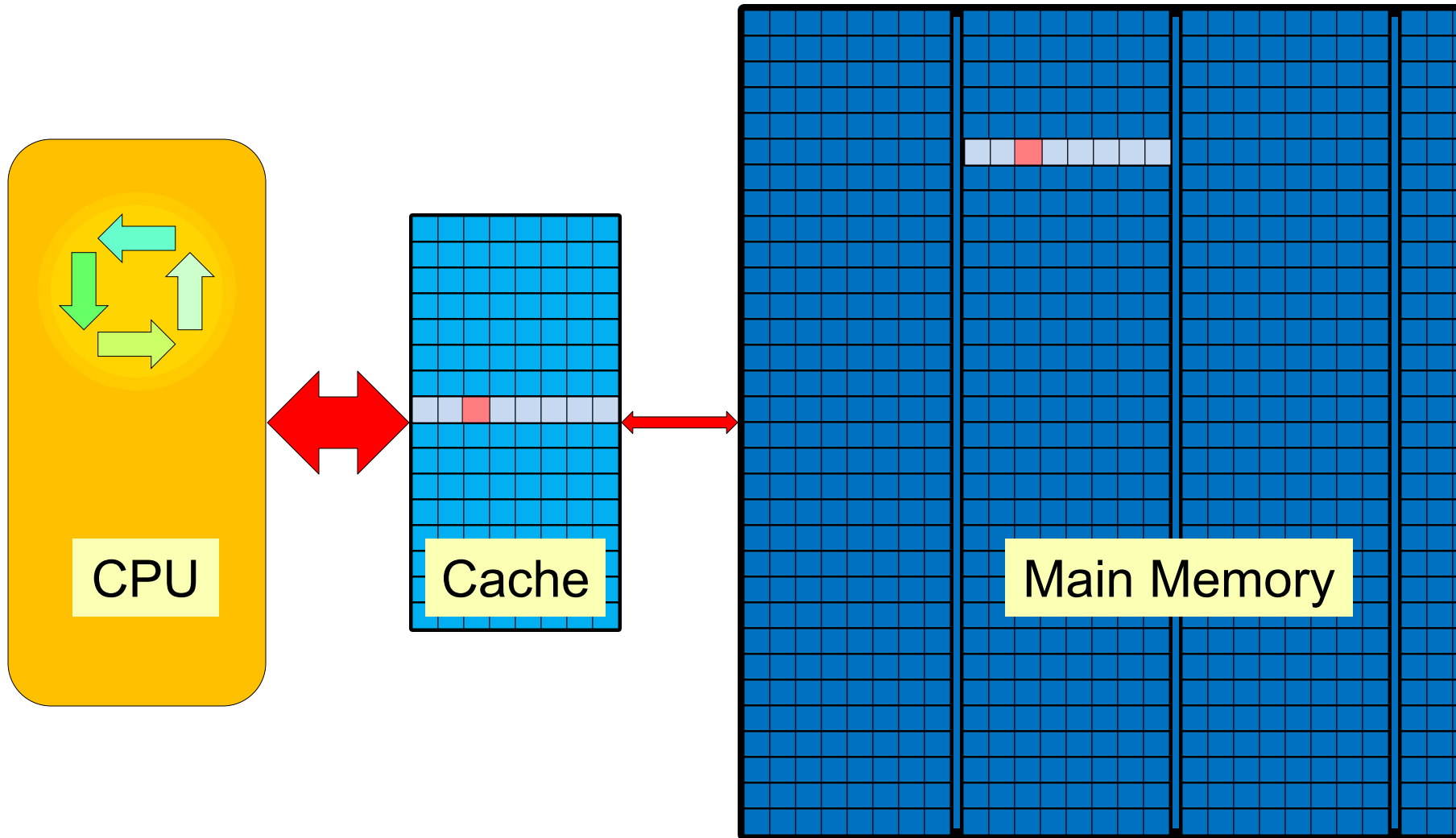
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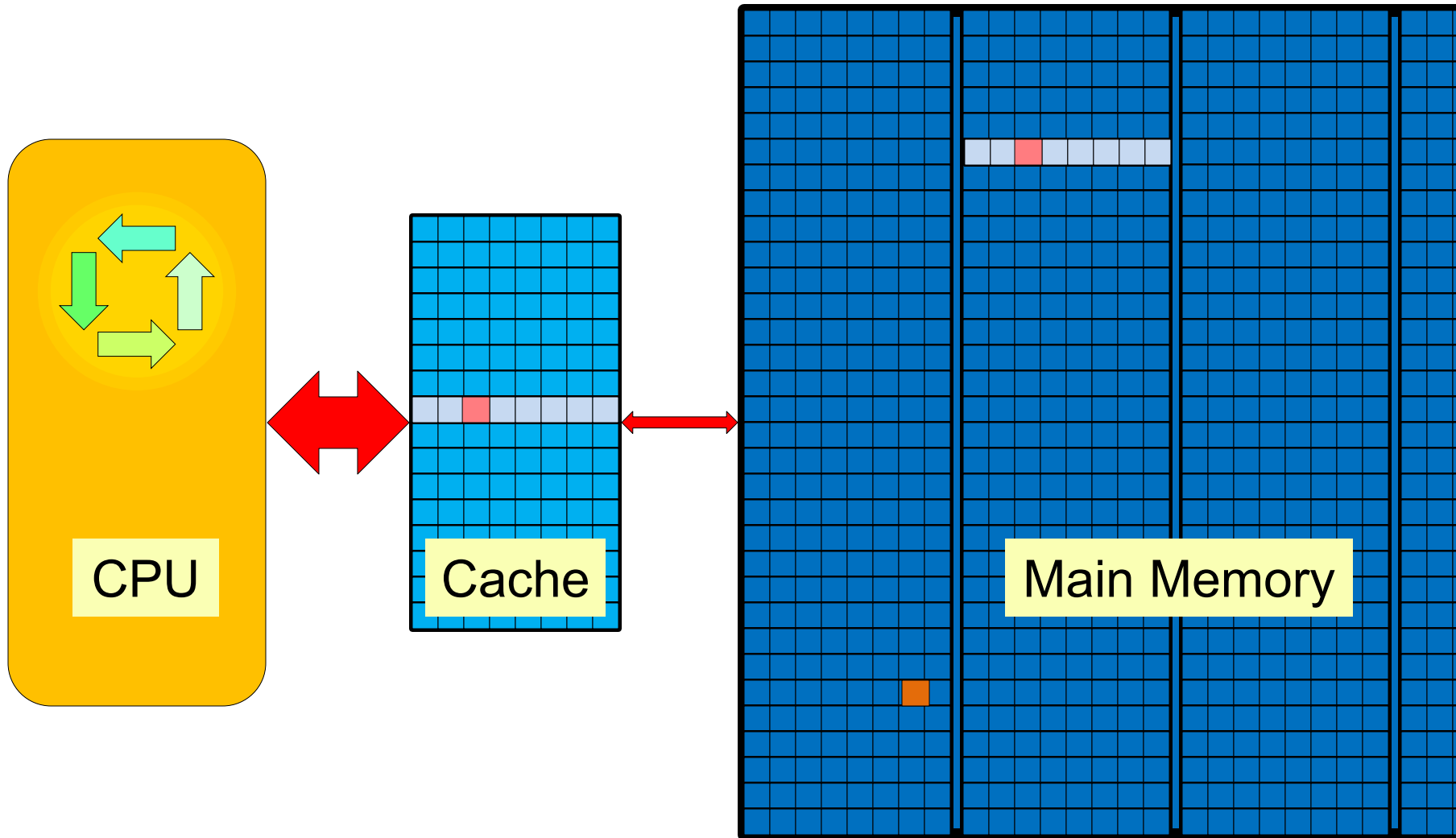
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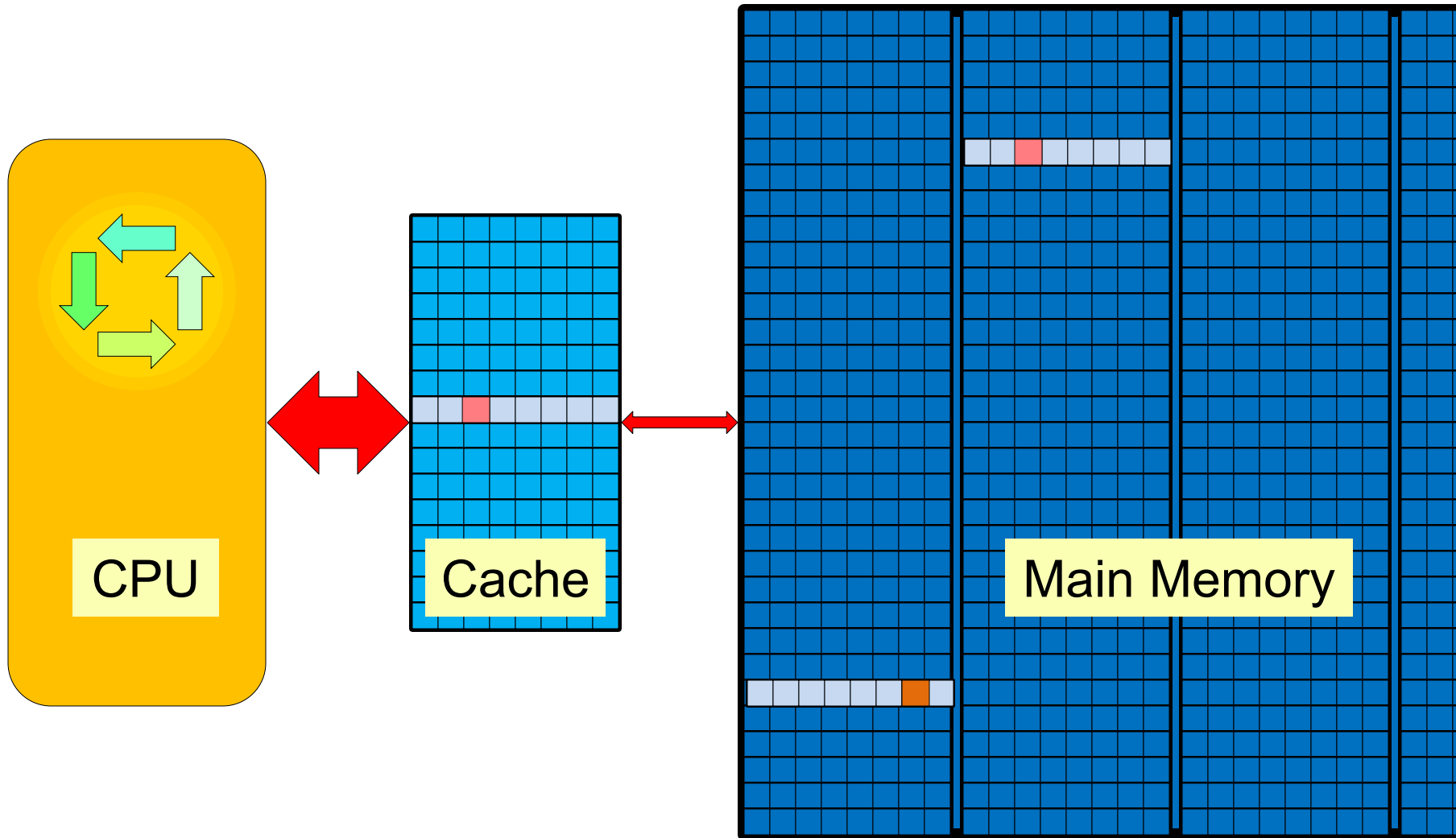
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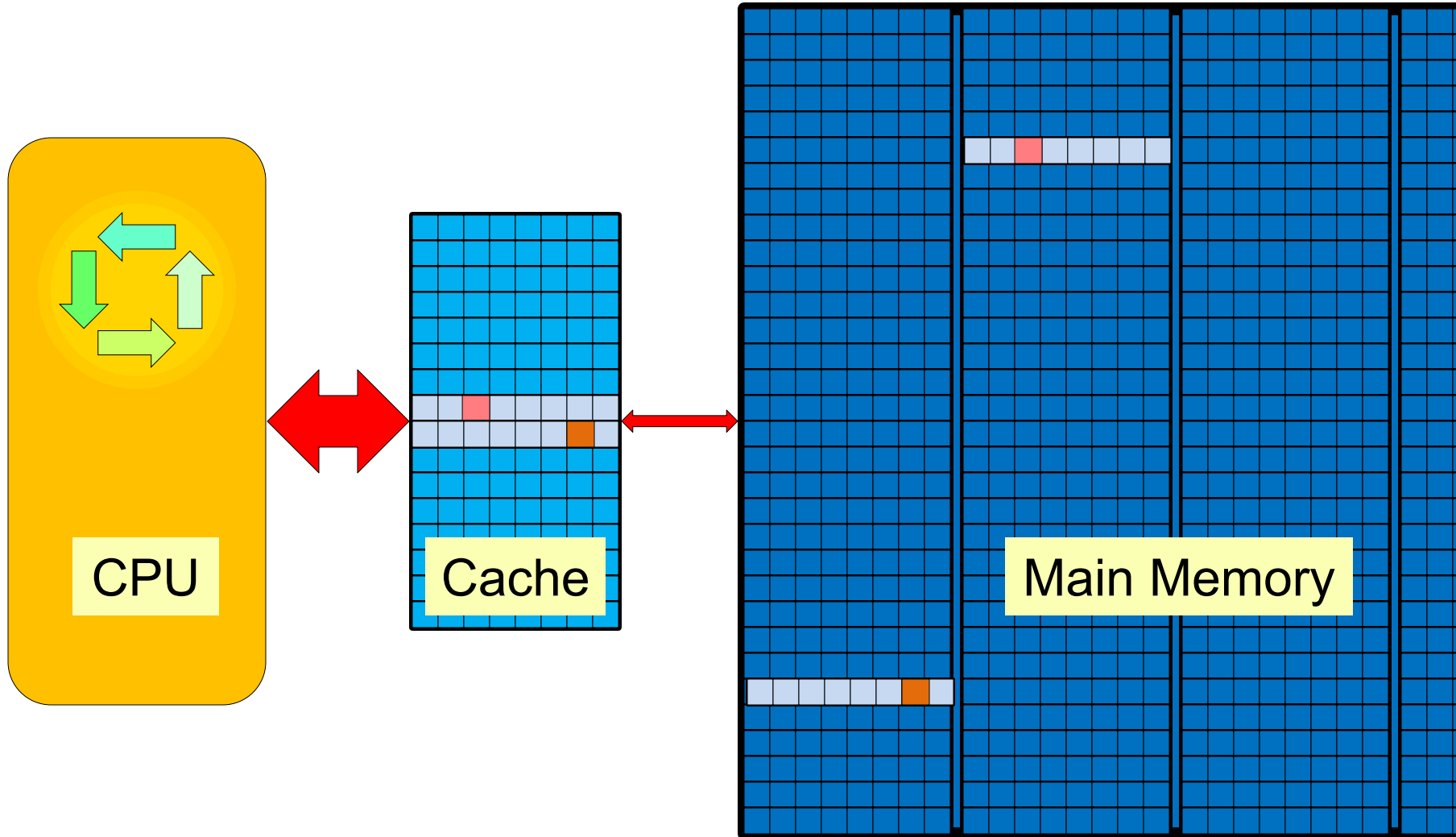
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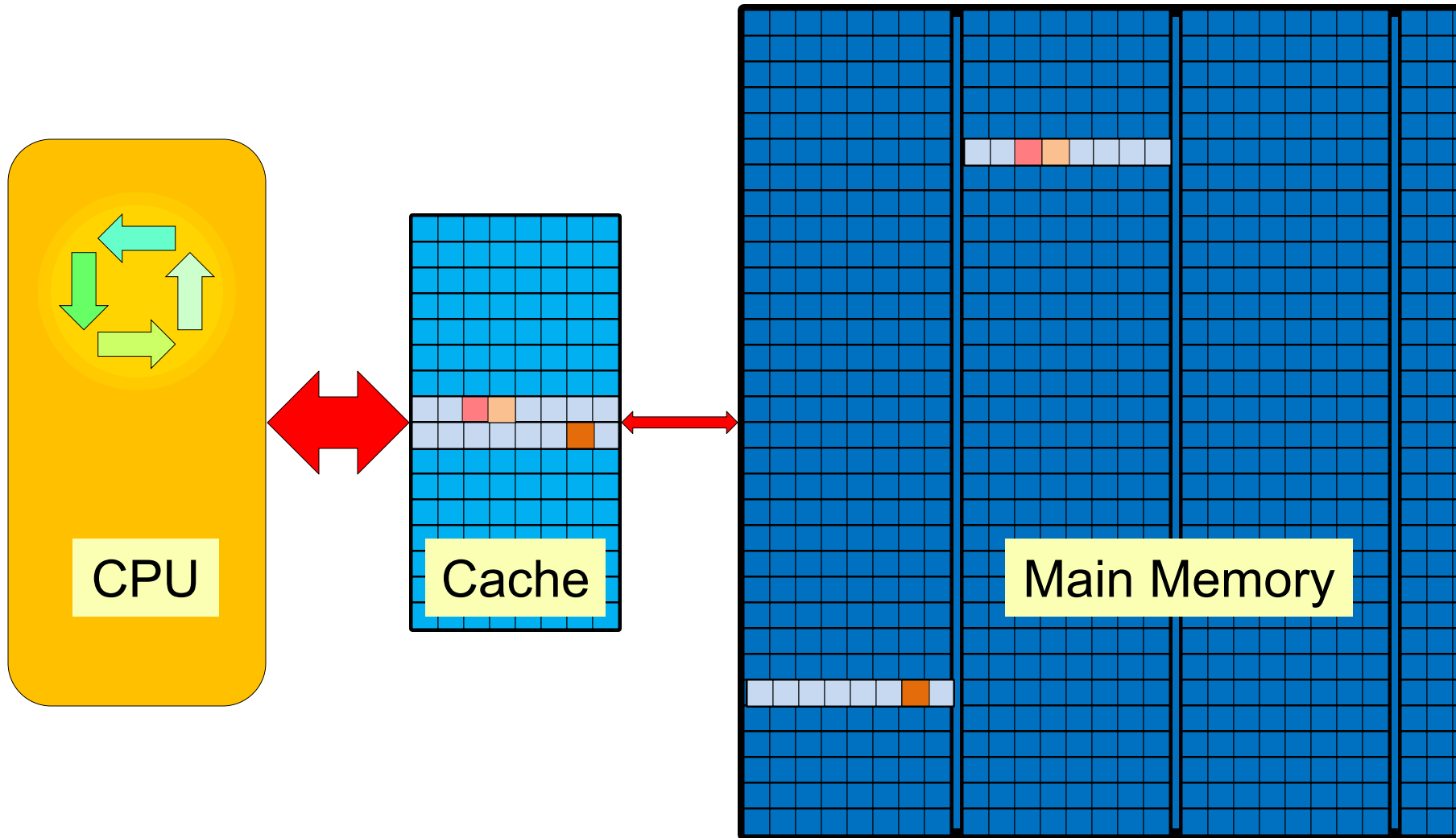
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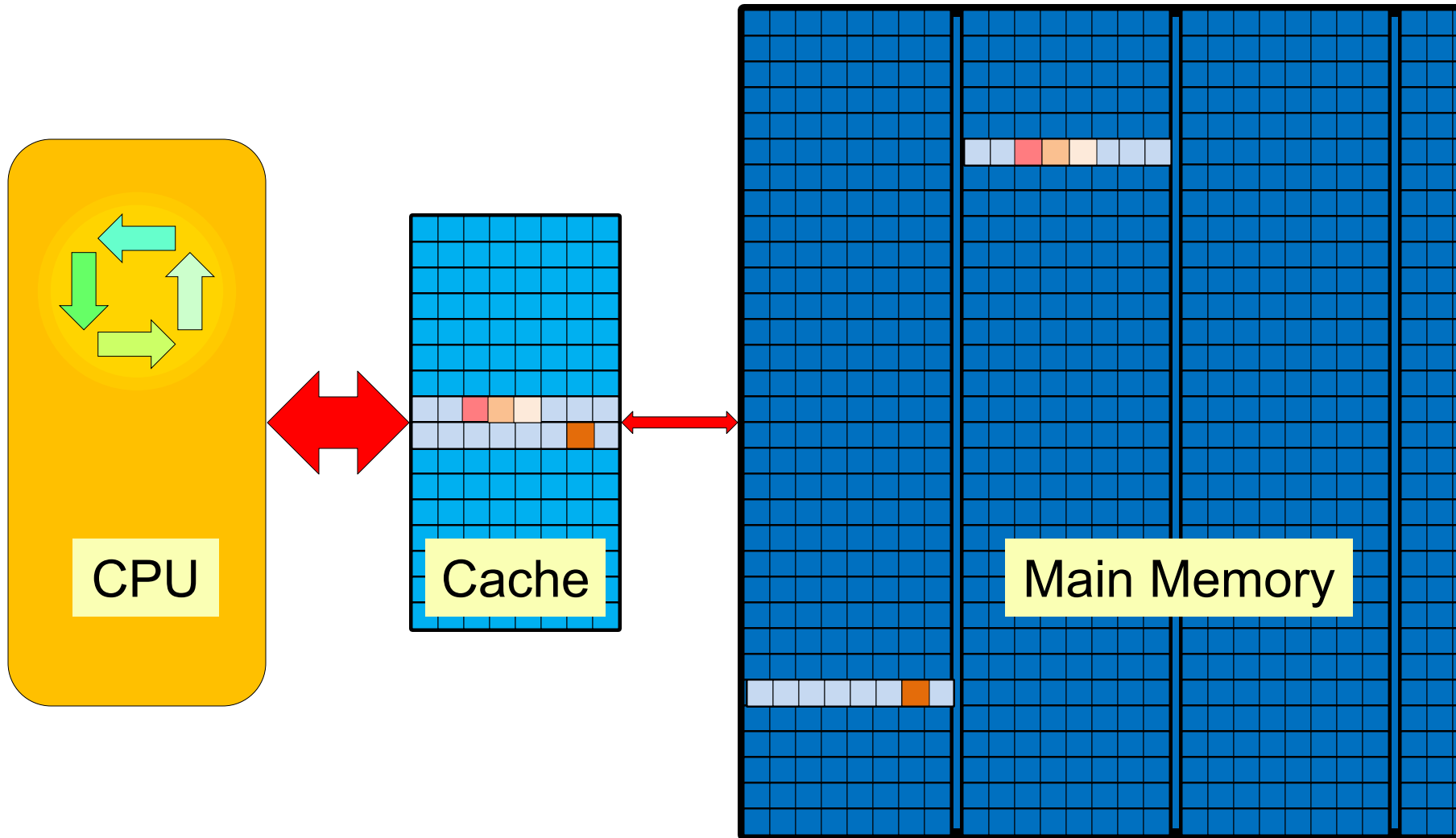
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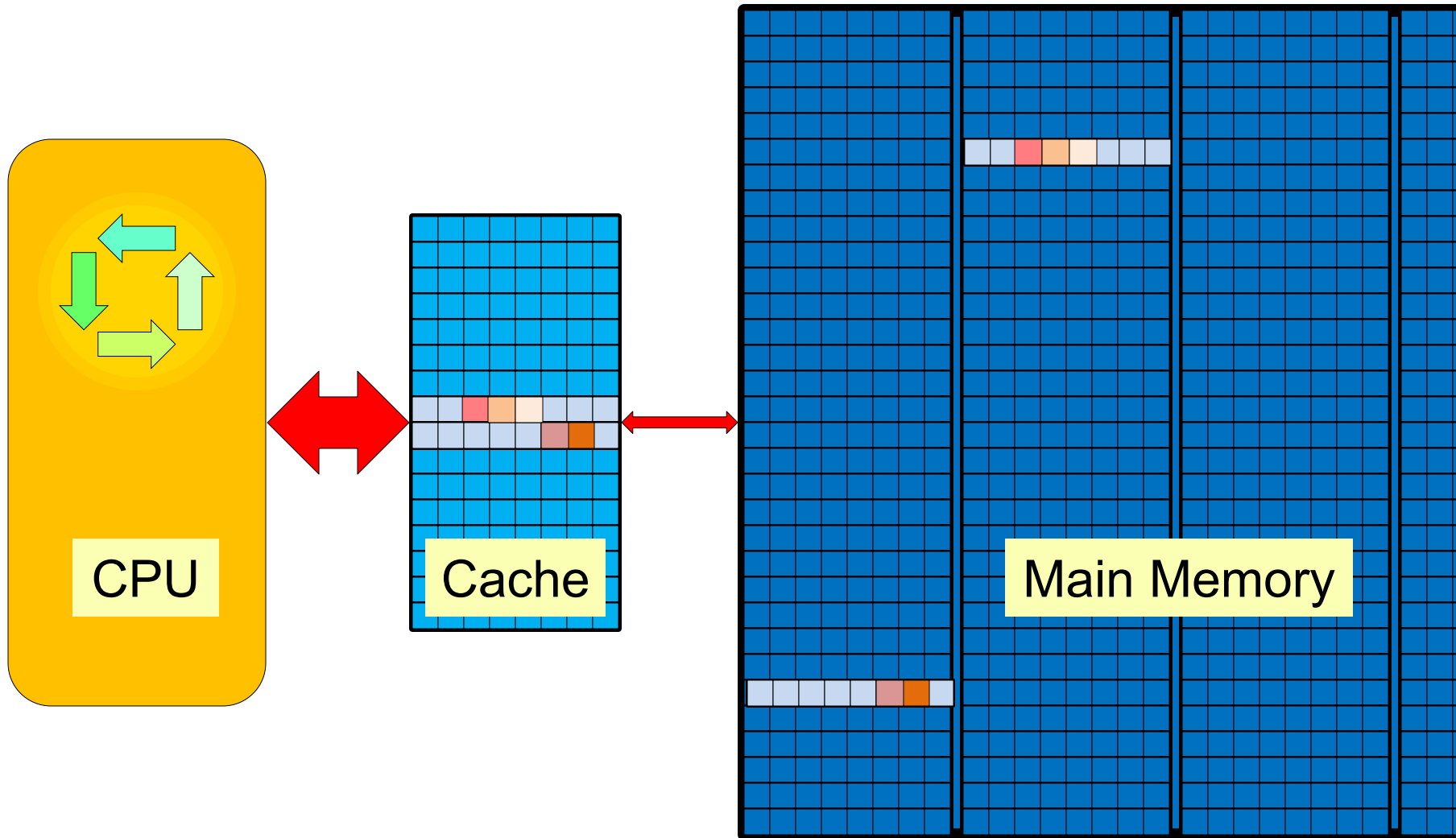
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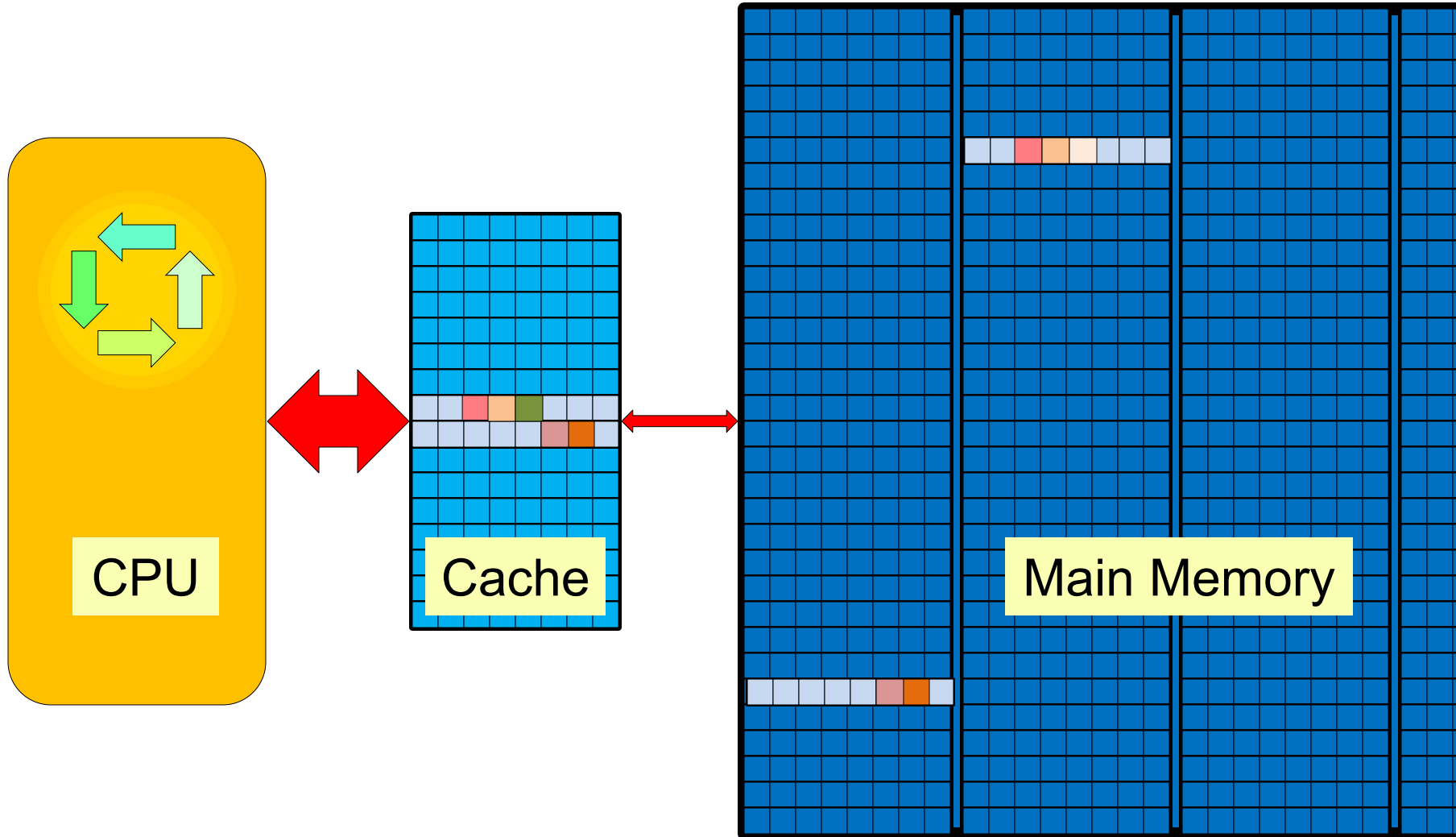
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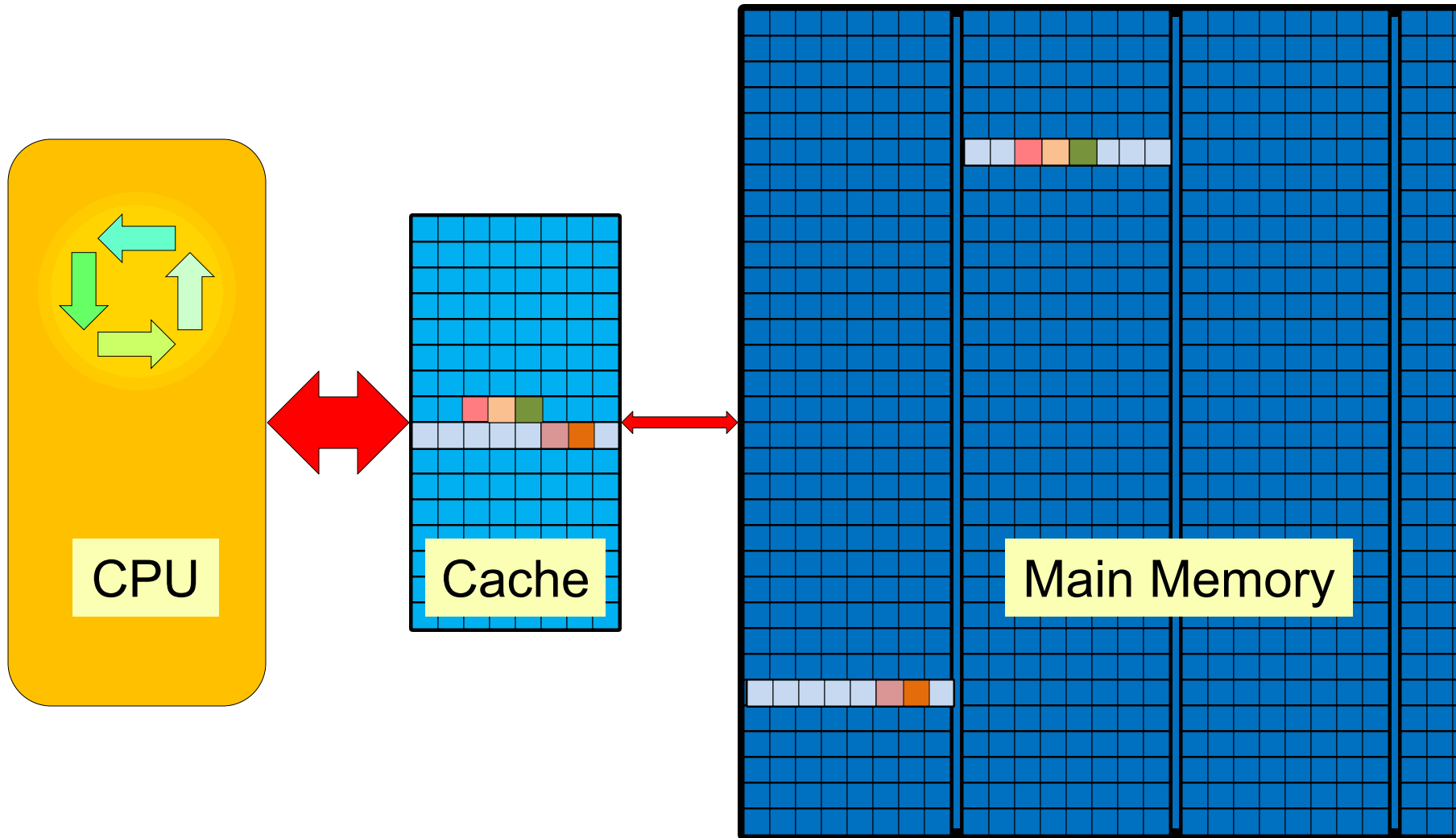
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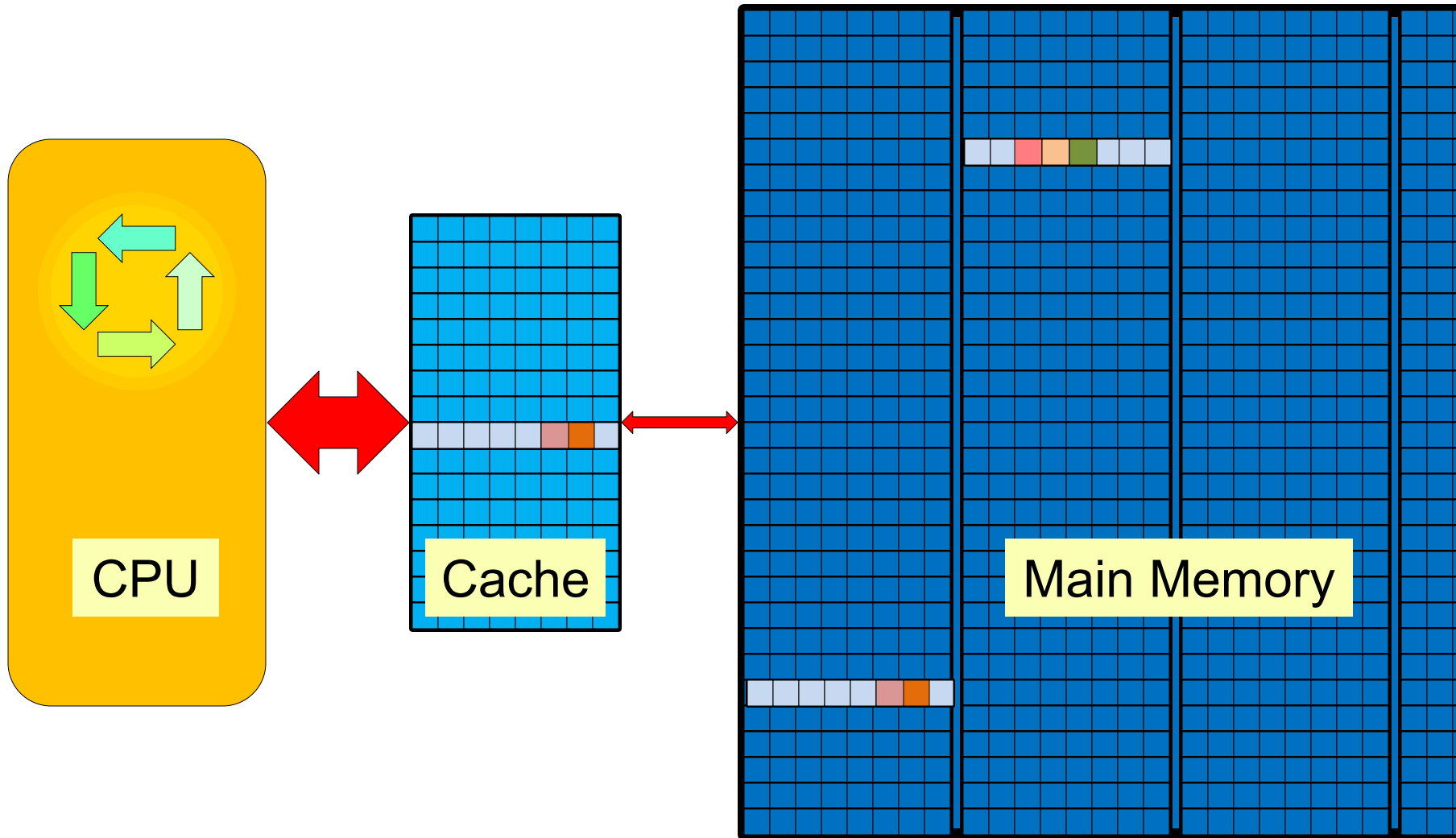
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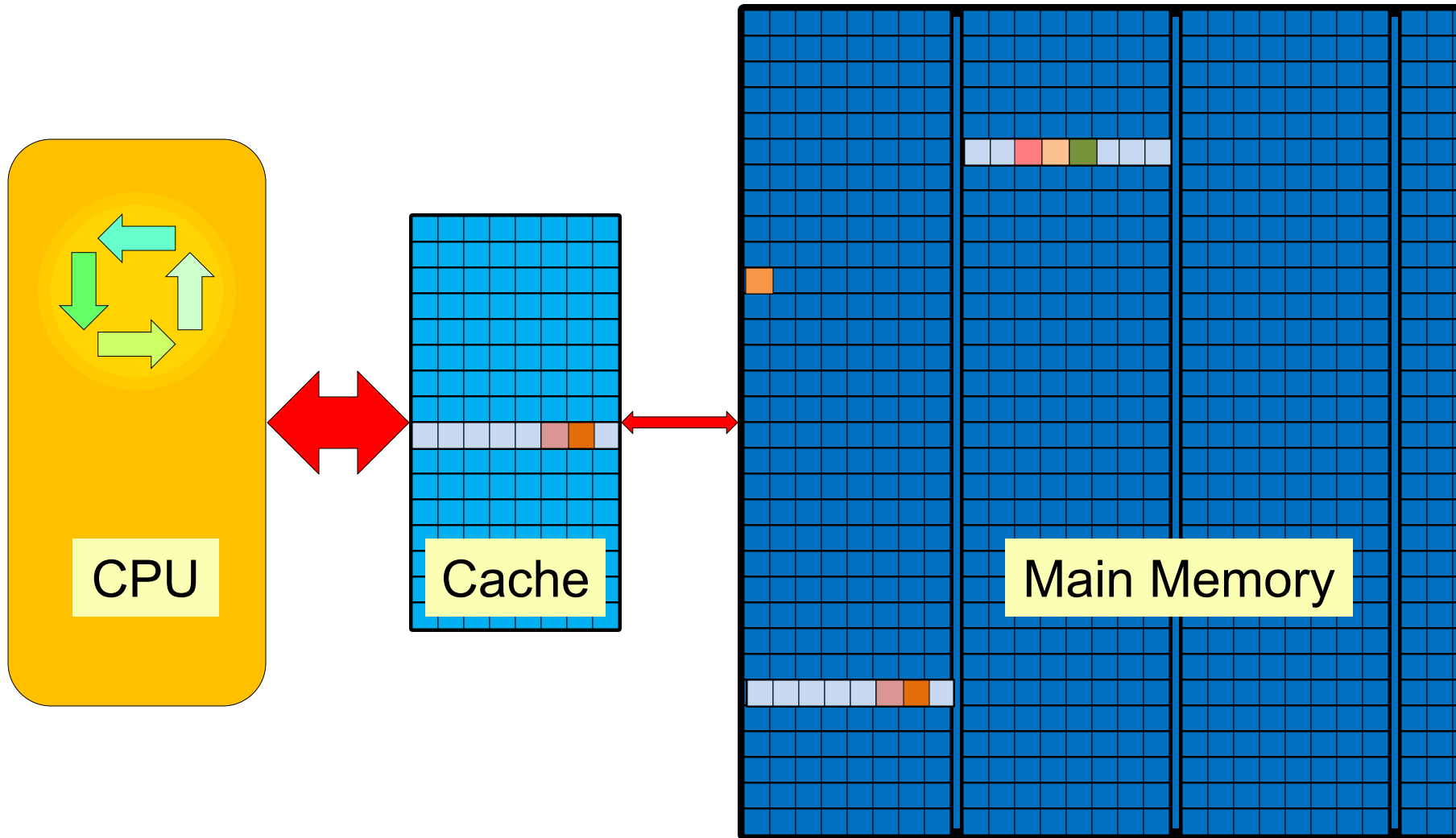
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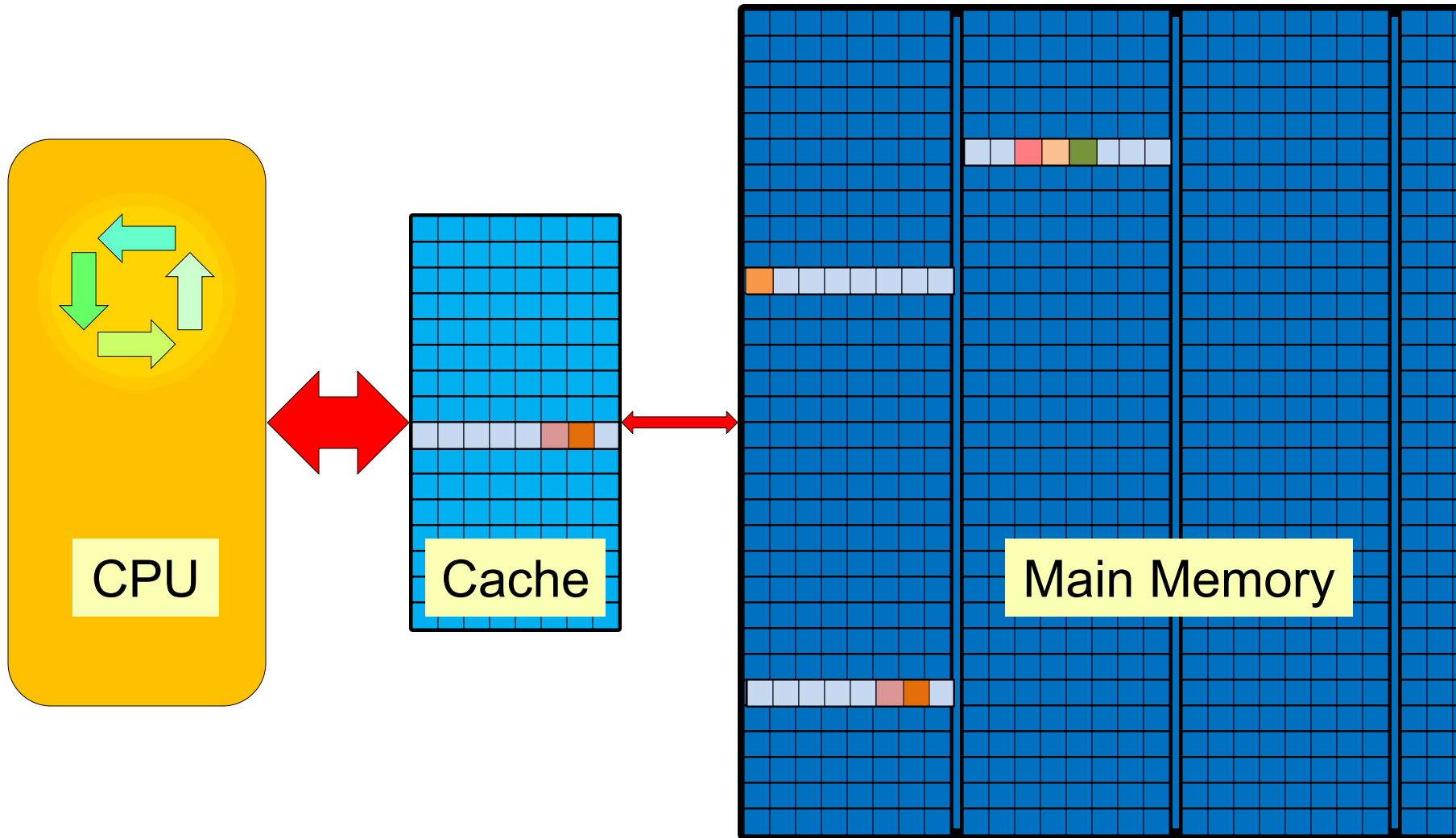
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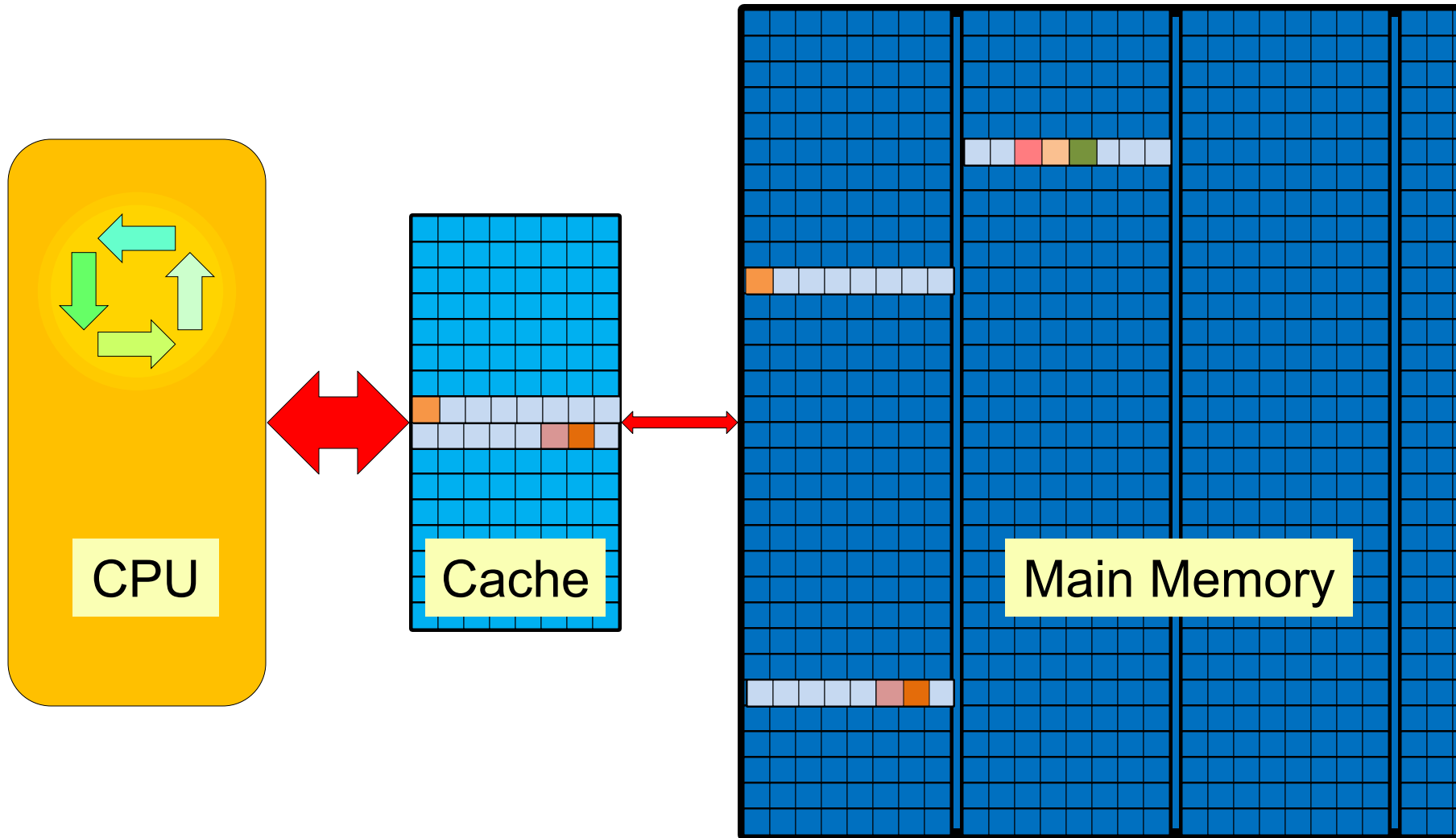
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Review of Computer Memory



1. Introduction and Background

Review of Computer Memory



1. Introduction and Background

Review of Computer Memory

(Main)

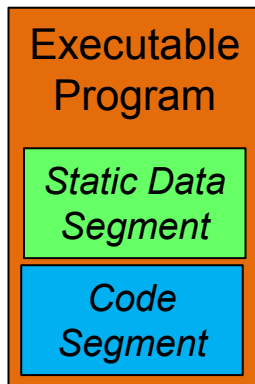
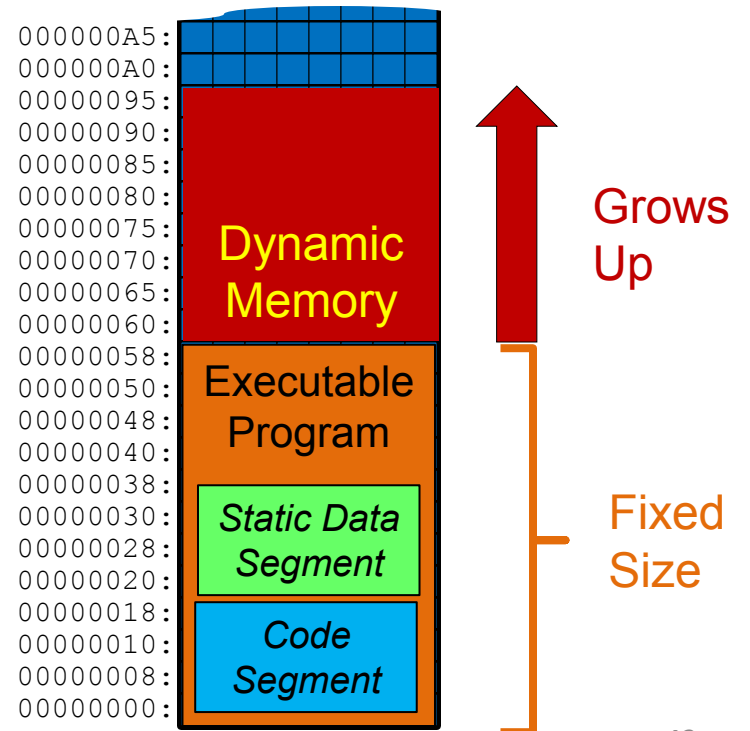
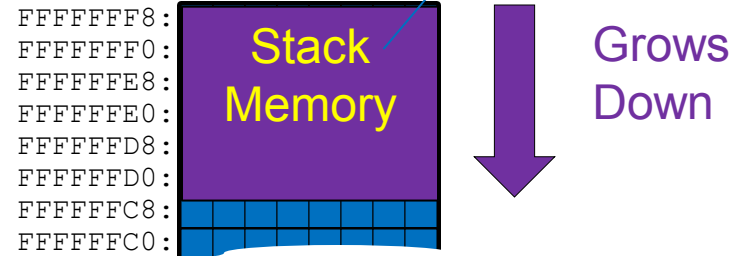
Memory

Segments

1. Introduction and Background

Review of Computer Memory

Main Memory



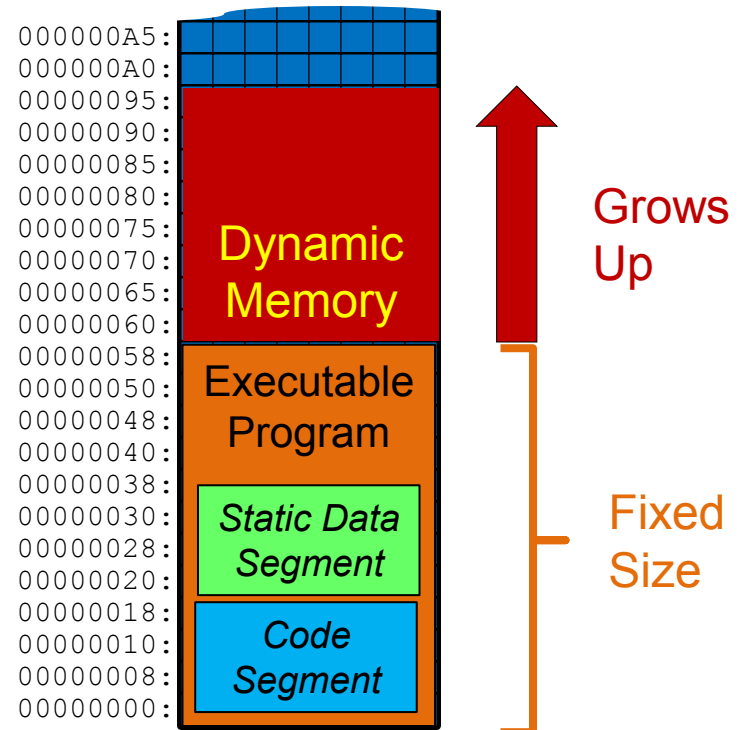
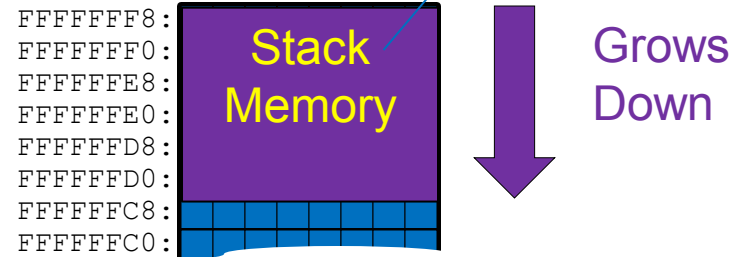
1. Introduction and Background
Important Questions

What is a
Memory Allocator?

1. Introduction and Background

Review of Computer Memory

Main
Memory



1. Introduction and Background

Review of Computer Memory

Main
Memory

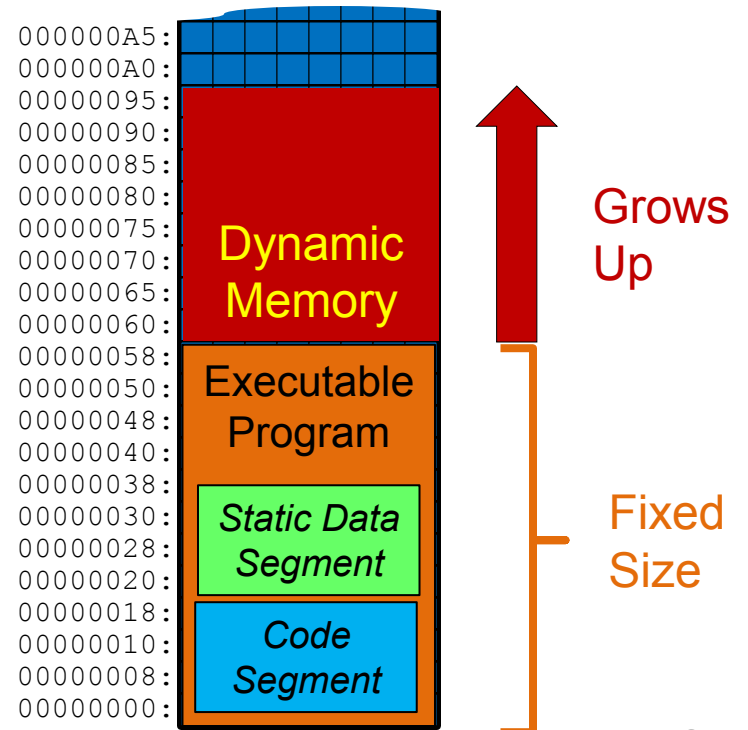
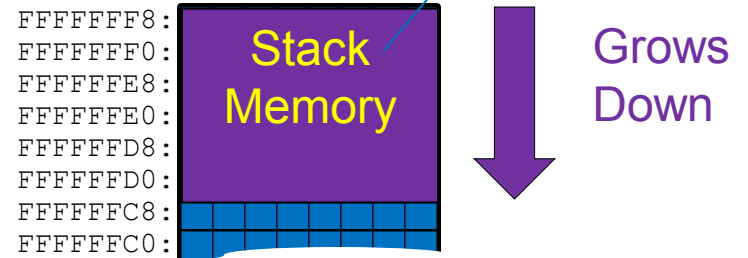
Special-Purpose Local Allocator:

```
// alloca.h  
void *alloca(size_t nBytes);
```

General-Purpose Global Allocator:

```
// malloc.h  
void *malloc(size_t nBytes);  
void free(void *address);
```

C-Language Memory-Allocation Utilities



1. Introduction and Background

Memory Allocator Definition (take 1)

A memory allocator organizes a* region of computer memory, dispensing and reclaiming authorized access to suitable sub-regions on demand.

*possibly non-contiguous

1. Introduction and Background

General versus Special Allocator

A General-Purpose Allocator

- Is designed to work reasonably well for *all* use cases.
- Satisfies *all* requirements for memory allocators.

A Special-Purpose Allocator

- (Typically) works especially well for *some* use cases.
- Need not satisfy *all* requirements for allocators - E.g.:
 - May not be safe to use in a multi-threaded program.
 - May not reuse individually freed memory.
- Requires specific knowledge of the context of use.

1. Introduction and Background

Global versus Local Allocator

A Global Allocator

- Operates on a single ubiquitous region of memory.
- Exists throughout the lifetime of a program.
- Is inherently accessible from all parts of a program.

A Local Allocator

- Operates on a local sub-region (“arena”) of memory.
- May exist for less than the lifetime of a program.
- Is (typically) supplied for client use via a “reference”.
- Can (typically) be used to free memory unilaterally.

1. Introduction and Background

Global, General Allocator Utility

C:

```
// <malloc.h>
void *malloc(size_t nbytes);
void free(void *address);
```

C++:

```
// <new>
namespace std {
void *operator new(size_t nbytes);
void operator delete(void *address);
...
}
```

1. Introduction and Background

General/Special × Global/Local

| | Global | Local |
|---------|--|--|
| General | <code>malloc/free</code> <code>new/delete</code> <i><code>tcmalloc</code></i> <i><code>jemalloc</code></i> | <code>multipool_allocator</code> Any general algorithm applied to a physically (and temporally) local region of memory. |
| Special | An unsynchronized <i><code>tcmalloc</code></i> allocator “plugged into” (i.e., used to implement) <code>malloc/free</code> | <code>alloca</code> <code>monotonic_allocator</code> An unsynchronized version of a <code>multipool_allocator</code> |

1. Introduction and Background

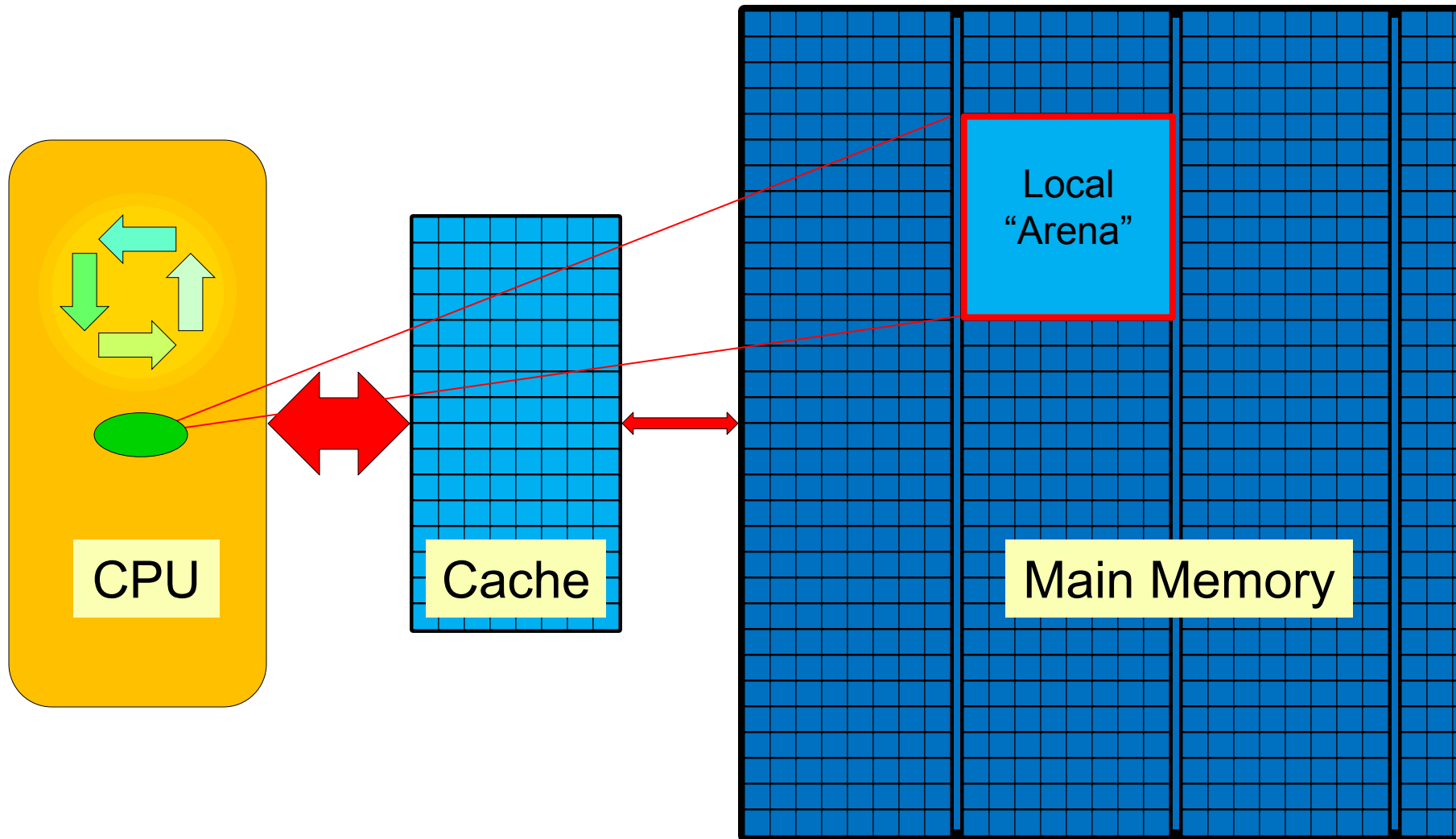
Memory Allocator Definition (take 2)

*A memory allocator is a stateful utility or **mechanism** that organizes a* region of computer memory, dispensing and reclaiming authorized access to suitable sub-regions on demand.*

*possibly non-contiguous

1. Introduction and Background

What is a local memory allocator?



1. Introduction and Background

Local Allocator Mechanism

```
class LocalAllocator {
    // internal data structure
public:
    LocalAllocator(const LocalAllocator&) = delete;
    LocalAllocator& operator=(const LocalAllocator&)
        = delete;

    // CREATORS
    LocalAllocator(/* ... */);

    // MANIPULATORS
    void *allocate(std::size_t nBytes);
    void deallocate(void *address);
};
```

1. Introduction and Background

Local Allocator Mechanism

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class LocalAllocator {
    // internal data structure
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1. Introduction and Background

Local Allocator Mechanism

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    // CREATORS
    LocalAllocator(void *begin, void *end);
    // MANIPULATORS
    void *allocate(std::size_t nBytes);
    void deallocate(void *address);
};
```


1. Introduction and Background

Local Allocator Mechanism

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1. Introduction and Background

Local Allocator Mechanism

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class LocalAllocator {
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        = delete;

    // CREATORS
    LocalAllocator(void *begin, void *end);

    // MANIPULATORS
    void *allocate(std::size_t nBytes);
    void deallocate(void *address);
    void release(); // local allocators only
};
```

1. Introduction and Background

Memory Allocator Definition (take 3)

A memory allocator is (the client-facing interface for) a stateful utility or *mechanism* that organizes a* region of computer memory, dispensing and reclaiming authorized access to suitable sub-regions on demand.

*possibly non-contiguous

1. Introduction and Background

Memory Allocator Interfaces

Allocators can be supplied for use in multiple ways:

1. As (stateful) utility functions.

- ❖ Doesn't support allocator objects.

2. As a “reference wrapper” template parameter.

- ✓ Concrete allocator type is available for use by client's compiler.
- ❖ Forces a client to be a template in order to hold the allocator reference.
- ❖ Allocator type affects the C++ type of the client object.

3. As the address of a pure abstract base class.

- ✓ Allocator can be held via a base-class reference by a non-template class.
- ✓ The choice of allocator does not affect the C++ type of the client object.
- ❖ Allocator must be accessed via its virtual-function interface.
- ❖ Object must somehow hold an extra address – even for the default case.

Outline

1. Introduction and Background

What are memory allocators, and why are they useful?

2. Understanding the Problem

What aspects of software affect allocation strategy?

3. Analyzing the Benchmark Data

When and how do you use which allocator, and why?

4. Conclusions

What must we remember about memory allocators?

Outline

1. Introduction and Background

What are memory allocators, and why are they useful?

2. Understanding the Problem

What aspects of software affect allocation strategy?

3. Analyzing the Benchmark Data

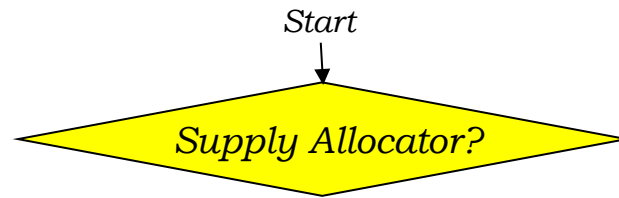
When and how do you use which allocator, and why?

4. Conclusions

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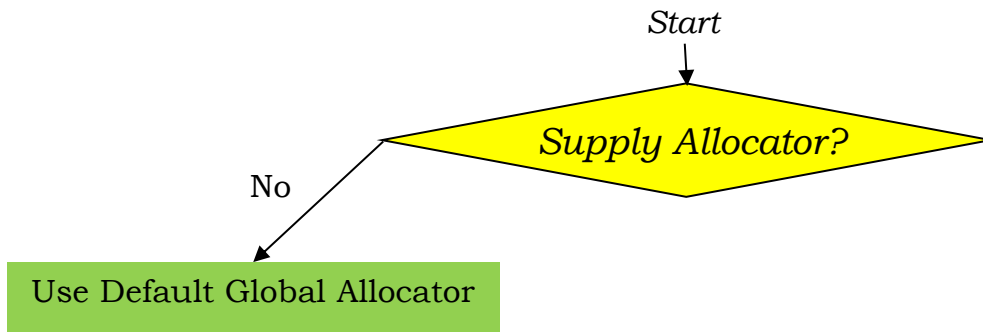
2. Understanding the Problem

Supply a local allocator? Which one?



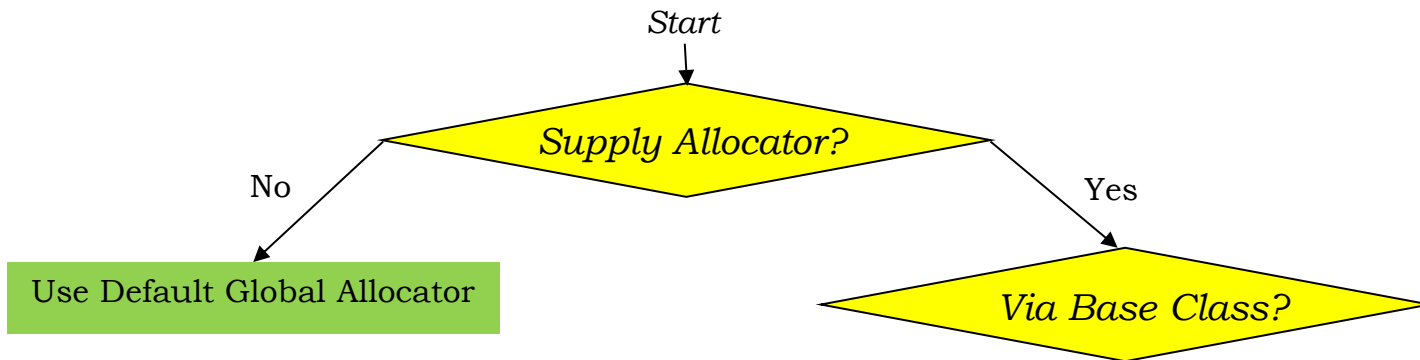
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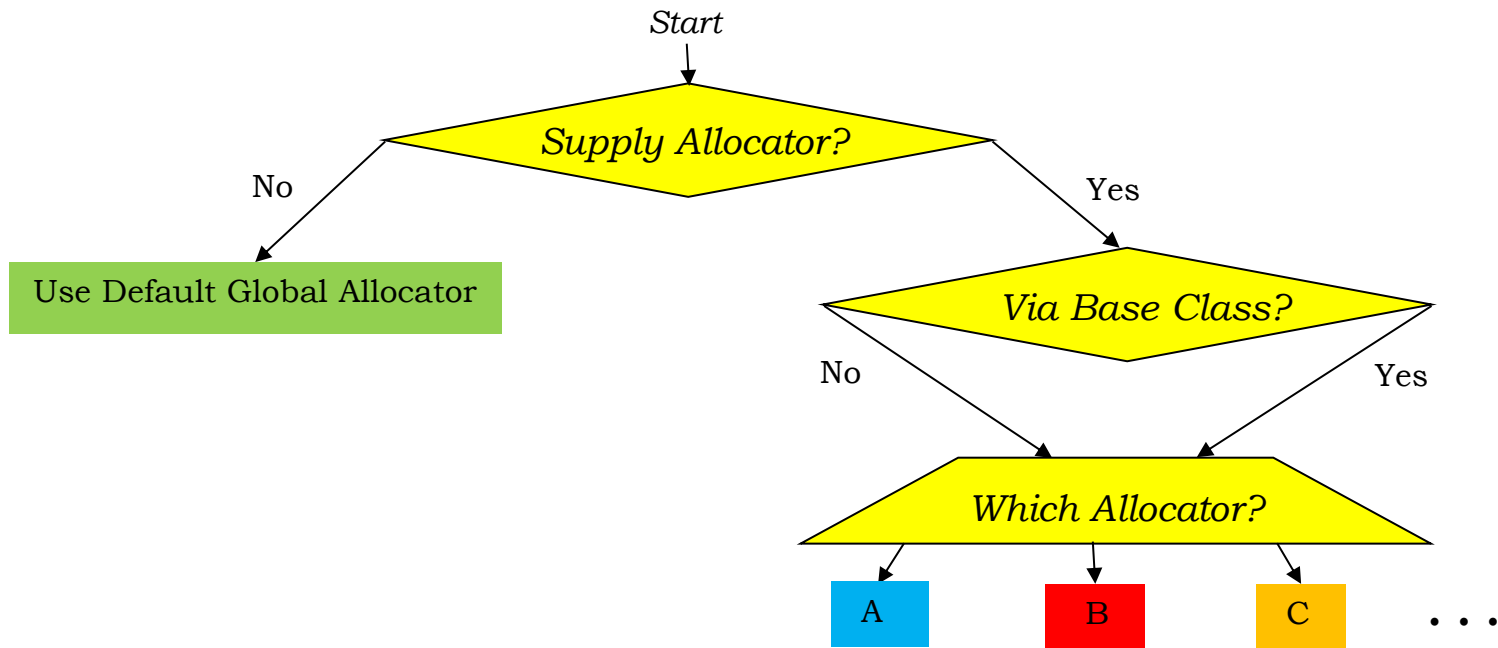
2. Understanding the Problem

Supply a local allocator? Which one?



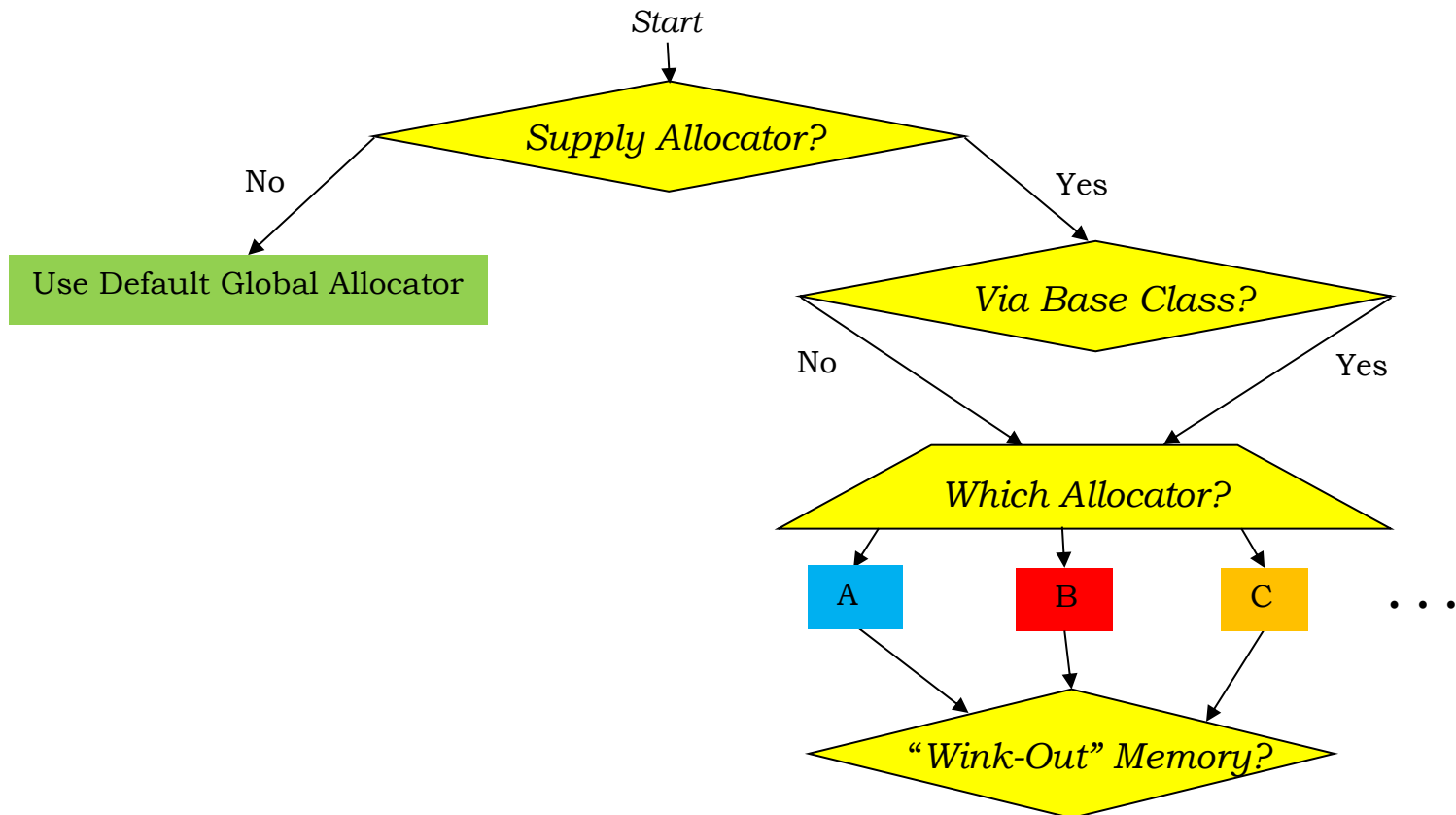
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Supply a local allocator? Which one?



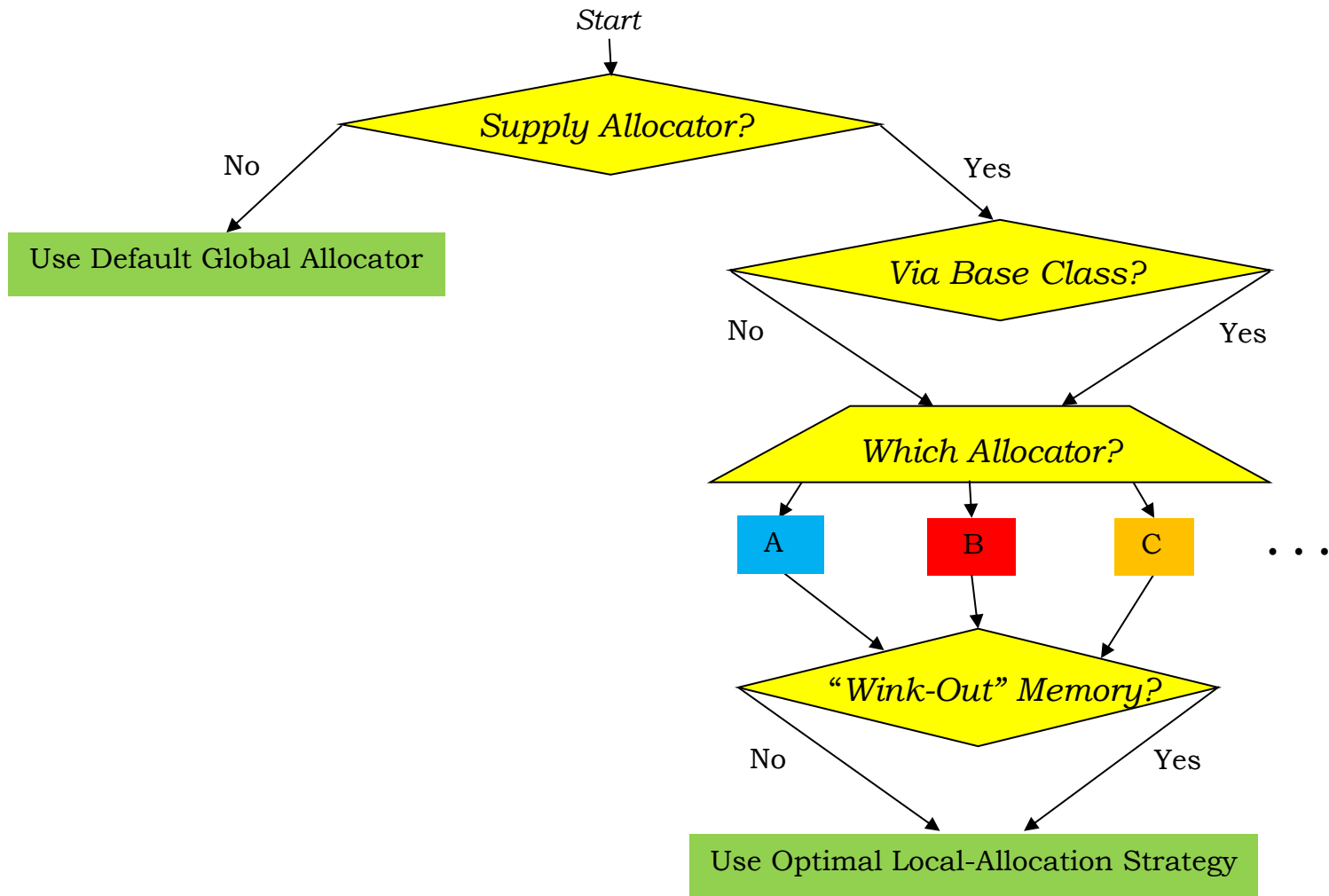
2. Understanding the Problem

Supply a local allocator? Which one?



2. Understanding the Problem

Supply a local allocator? Which one?



2. Understanding the Problem

Our Tool Chest of Allocation Strategies

2. Understanding the Problem

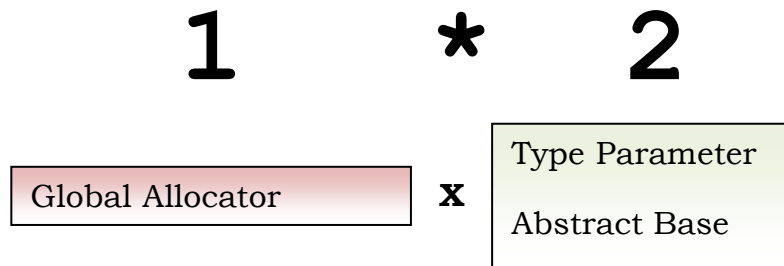
Our Tool Chest of Allocation Strategies

1

Global Allocator

2. Understanding the Problem

Our Tool Chest of Allocation Strategies



2. Understanding the Problem

Our Tool Chest of Allocation Strategies

2 =

1

*

2

Global Allocator

x

Type Parameter
Abstract Base

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

2 =

1

*

2

Global Allocator

x

Type Parameter
Abstract Base

3

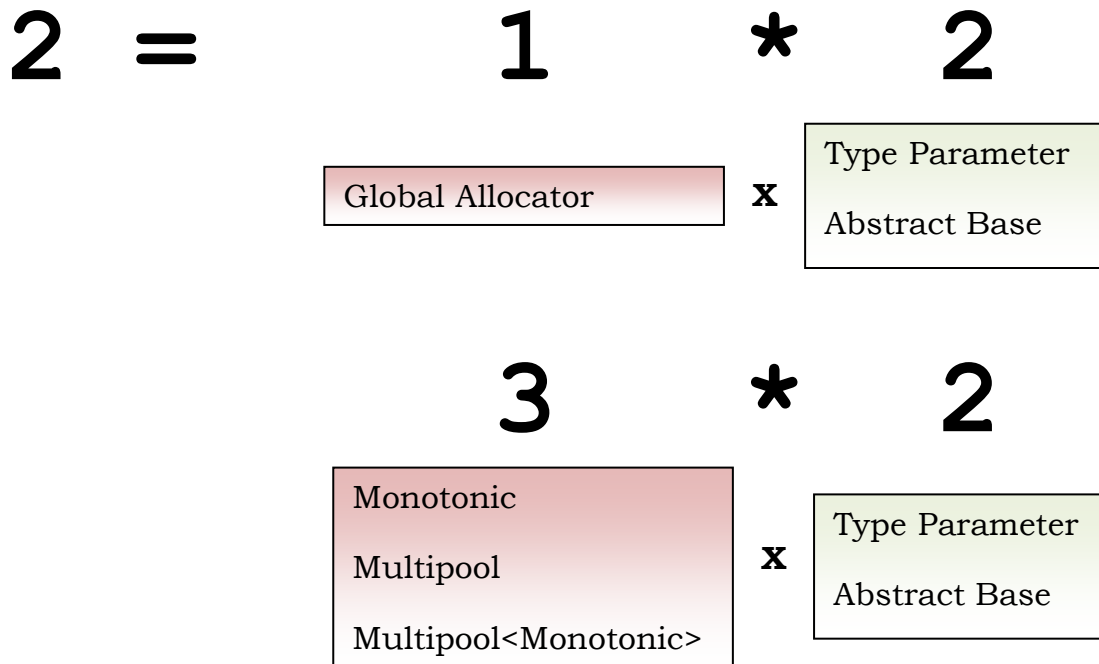
Monotonic

Multipool

Multipool<Monotonic>

2. Understanding the Problem

Our Tool Chest of Allocation Strategies



2. Understanding the Problem

Our Tool Chest of Allocation Strategies

2 =

1

*

2

Global Allocator

x

Type Parameter
Abstract Base

3

*

2

*

2

Monotonic
Multipool
Multipool<Monotonic>

x

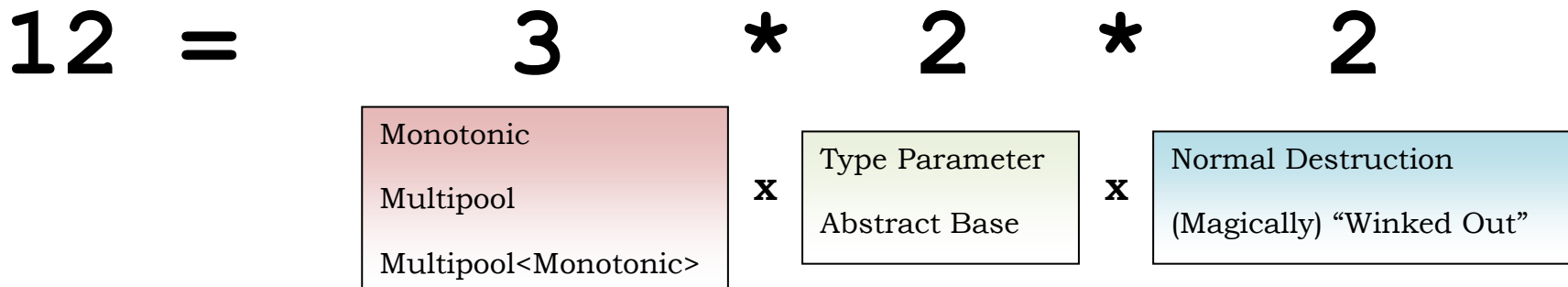
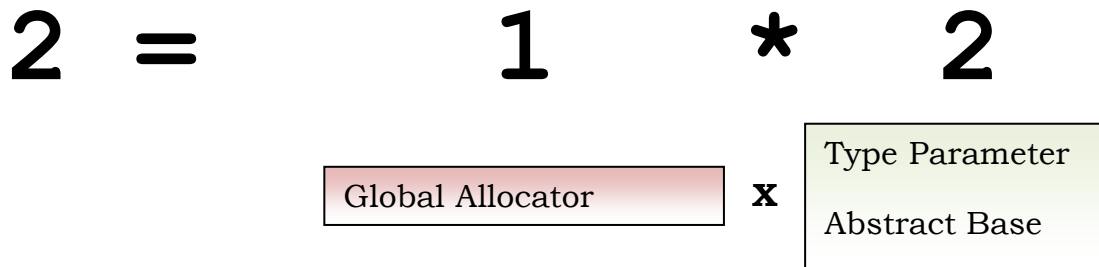
Type Parameter
Abstract Base

x

Normal Destruction
(Magically) “Winked Out”

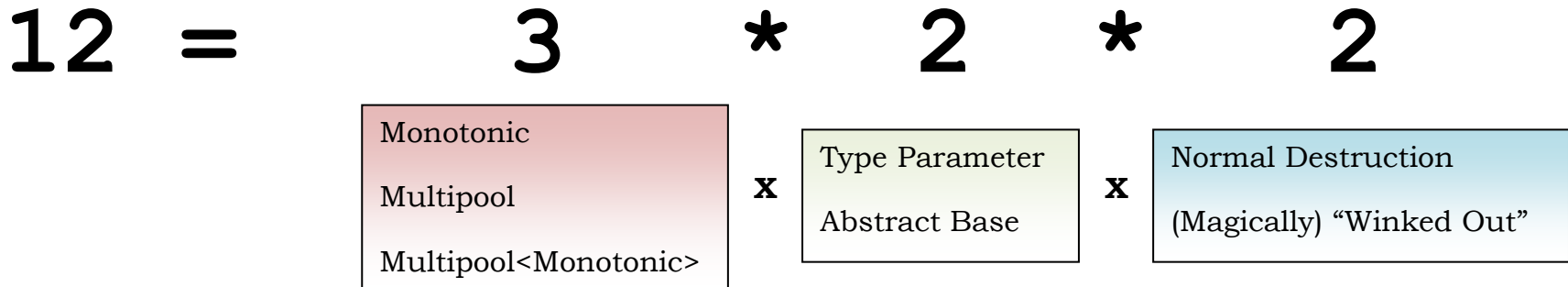
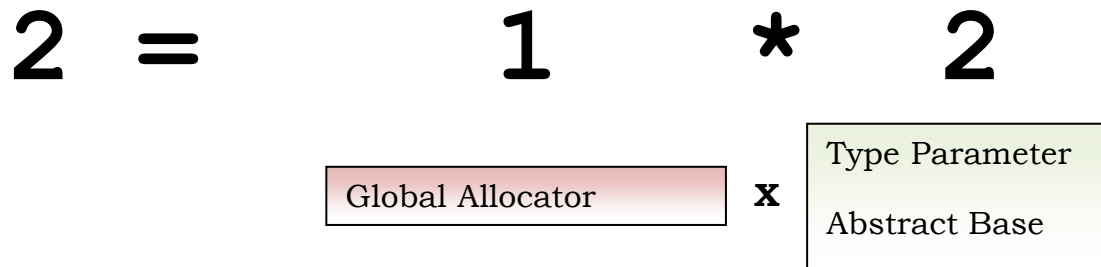
2. Understanding the Problem

Our Tool Chest of Allocation Strategies



2. Understanding the Problem

Our Tool Chest of Allocation Strategies



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Allocation Strategies (AS)

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

| Label | Allocator Type | Allocator Binding | Destruction of Allocated Objects |
|-------|--------------------------|-------------------|----------------------------------|
| AS1 | Default Global Allocator | Type Parameter | Normal Destruction |
| AS2 | New/Delete Allocator | Abstract Base | Normal Destruction |
| | | | |
| AS3 | Monotonic | Type Parameter | Normal Destruction |
| AS4 | Monotonic | Type Parameter | (magically) “Winked Out” |
| AS5 | Monotonic | Abstract Base | Normal Destruction |
| AS6 | Monotonic | Abstract Base | (magically) “Winked Out” |
| | | | |
| AS7 | Multipool | Type Parameter | Normal Destruction |
| AS8 | Multipool | Type Parameter | (magically) “Winked Out” |
| AS9 | Multipool | Abstract Base | Normal Destruction |
| AS10 | Multipool | Abstract Base | (magically) “Winked Out” |
| | | | |
| AS11 | Multipool<Monotonic> | Type Parameter | Normal Destruction |
| AS12 | Multipool<Monotonic> | Type Parameter | (magically) “Winked Out” |
| AS13 | Multipool<Monotonic> | Abstract Base | Normal Destruction |
| AS14 | Multipool<Monotonic> | Abstract Base | (magically) “Winked Out” |

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

| Label | Allocator Type | Allocator Binding | Destruction of Allocated Objects |
|-------------|--------------------------|-------------------|----------------------------------|
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| AS6 | Monotonic | Abstract Base | (magically) “Winked Out” |
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| AS7 | Multipool | Type Parameter | Normal Destruction |
| AS8 | Multipool | Type Parameter | (magically) “Winked Out” |
| AS9 | Multipool | Abstract Base | Normal Destruction |
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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

Allocation Strategies: AS1-AS2



Global Allocator

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

Standard Allocator

```
class allocator {
    // no data members
public:
    // CREATORS
    allocator() { }
    allocator(const allocator& ) { }
    ~allocator() { }

    // MANIPULATORS
    allocator operator=( ) = delete;
    void *allocate(std::size_t nBytes) {
        return ::operator new(nBytes); }
    void deallocate(void *address) {
        ::operator delete(address); }
};

// FREE OPERATORS
bool operator==(const allocator&, const allocator&) {
    return true; }
```

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

Standard Allocator

```
class allocator {
    // no data members
public:
    // CREATORS
    allocator() { }
    allocator(const allocator& ) { }
    ~allocator() { }

    // MANIPULATORS
    allocator operator=() = delete;
    void *allocate(std::size_t nBytes) {
        return ::operator new(nBytes); }
    void deallocate(void *address) {
        ::operator delete(address); }
};

// FREE OPERATORS
bool operator==(const allocator&, const allocator&) {
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```

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
class allocator {
    // no data members
public:
    // CREATORS
    allocator() { }
    allocator(const allocator& ) { }
    ~allocator() { }

    // MANIPULATORS
    allocator operator=( ) = delete;
    void *allocate(std::size_t nBytes) {
        return ::operator new(nBytes); }
    void deallocate(void *address) {
        ::operator delete(address); }
};

// FREE OPERATORS
bool operator==(const allocator&, const allocator&) {
    return true; }
```

AS1: Standard Allocator Default Global Allocator

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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| AS5 | Monotonic | Abstract Base | Normal Destruction |
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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myFunction()  
{  
    std::vector<int> v;  
}
```

Same object code generated as

```
myFunction()  
{  
    std::vector<int, allocator> v;  
}
```

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myFunction ()  
{  
    std::vector<int> v;  
}
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Same object code generated as

```
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Type Parameter



2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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Our Tool Chest of Allocation Strategies

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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myBenchmark()  
{  
    const int N = 1000;  
    std::vector<std::list<int> *> system(N);
```

```
} // 'system' goes out of scope (and is destroyed).
```

Same object code generated as

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myBenchmark()  
{  
    const int N = 1000;  
  
    std::vector<std::list<int> *> system(N) ;
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} // 'system' goes out of scope (and is destroyed).
```

Same object code generated as

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myBenchmark()  
{  
    const int N = 1000;  
    std::vector<std::list<int> *> system(N);  
  
    for (int i = 0; i < N; ++i) {  
        system[i] = new std::list<int>;  
        // build up list of elements  
    }  
  
} // 'system' goes out of scope (and is destroyed).
```

Same object code generated as

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myBenchmark()  
{  
    const int N = 1000;  
    std::vector<std::list<int> *> system(N);  
  
    for (int i = 0; i < N; ++i) {  
        system[i] = new std::list<int>;  
        // build up list of elements  
    }  
  
    // Do benchmark (e.g., access links).  
  
} // 'system' goes out of scope (and is destroyed).
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Same object code generated as

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myBenchmark()  
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    const int N = 1000;  
    std::vector<std::list<int> *> system(N);  
  
    for (int i = 0; i < N; ++i) {  
        system[i] = new std::list<int>;  
        // build up list of elements  
    }  
  
    // Do benchmark (e.g., access links).  
    for (int i = 0; i < N; ++i) {  
        delete system[i];  
    }  
} // 'system' goes out of scope (and is destroyed).
```

Normal Destruction

Same object code generated as

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
class Allocator {  
    // no data members  
public:  
    // CREATORS  
    virtual ~allocator(); // Defined empty in '.cpp' file.  
  
    // MANIPULATORS  
    virtual void *allocate(std::size_t nBytes) = 0;  
    virtual void deallocate(void *address) = 0;  
};
```

Protocol:
Pure Abstract Base Class

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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class Allocator {  
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public:  
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    virtual void *allocate(std::size_t nBytes) = 0;  
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};
```

Protocol:
Pure Abstract Base Class

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
class NewDeleteAllocator : public Allocator {
    // no data members
public:
    // CREATORS
    NewDeleteAllocator() = default;
    ~NewDeleteAllocator() = default;
    NewDeleteAllocator(const NewDeleteAllocator&) = delete;

    // MANIPULATORS
    NewDeleteAllocator& operator=(const NewDeleteAllocator&)

    inline void *allocate(std::size_t nBytes) override {
        return ::operator new(nBytes); }

    inline void deallocate(void *address) override {
        ::operator delete(address); }
};
```

Concrete Derived Class

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
class NewDeleteAllocator : public Allocator {  
    // no data members  
public:  
    // CREATORS  
    NewDeleteAllocator() = default;  
    ~NewDeleteAllocator() = default;  
    NewDeleteAllocator(const NewDeleteAllocator&) = delete;  
    // MANIPULATORS  
    NewDeleteAllocator& operator=(const NewDeleteAllocator&)  
  
    inline void *allocate(std::size_t nBytes) override {  
        return ::operator new(nBytes); }  
  
    inline void deallocate(void *address) override {  
        ::operator delete(address); }  
};
```

AS2

Concrete Derived Class

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
class NewDeleteAllocator : public Allocator {  
    // no data members  
public:  
    // CREATORS  
    NewDeleteAllocator() = default;  
    ~NewDeleteAllocator() = default;  
    NewDeleteAllocator(const NewDeleteAllocator&) = delete;  
    // MANIPULATORS  
    NewDeleteAllocator& operator=(const NewDeleteAllocator&)  
  
    inline void *allocate(std::size_t nBytes) override {  
        return ::operator new(nBytes); }  
  
    inline void deallocate(void *address) override {  
        ::operator delete(address); }  
};
```

AS2

Concrete Derived Class

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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| AS6 | Monotonic | Abstract Base | (magically) “Winked Out” |
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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myFunction ()
```

```
{
```

```
    NewDeleteAllocator a;
```

```
    std::pmr::vector<int> v (&a);
```

```
    // ...
```

```
}
```

Via Protocol



2. Understanding the Problem

Our Tool Chest of Allocation Strategies

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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
myBenchmark()  
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    const int N = 1000;  
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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

Allocation Strategies: AS3-AS6

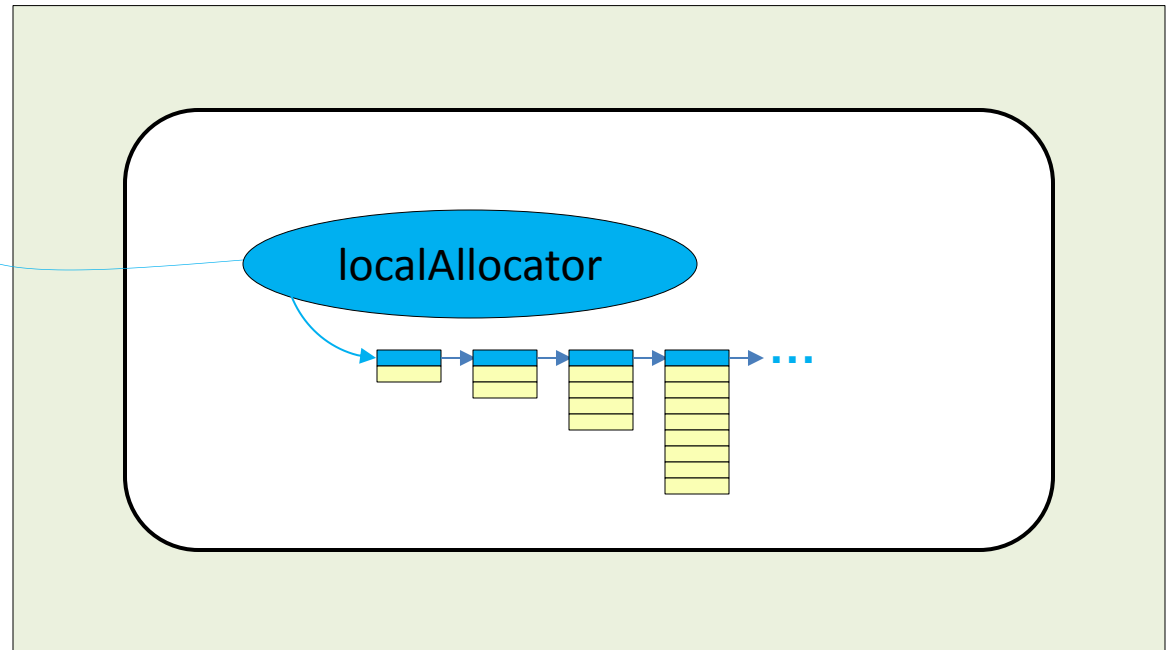
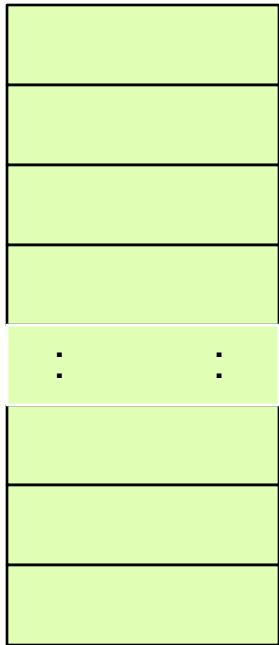
Monotonic Allocator

Global Allocator

2. Understanding the Problem

Our Tool Chest of Allocation Strategies

```
void myFunction(...) {  
    char buffer[1024];
```



`bdlma_bufferedsequentialallocator`

```
bdlma::BufferedSequentialAllocator local Allocator(buffer, sizeof buffer);  
bsl::vector(&local Allocator);  
// ...  
}
```

Note that deallocate is a No-Op!

2. Understanding the Problem

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2. Understanding the Problem

Our Tool Chest of Allocation Strategies

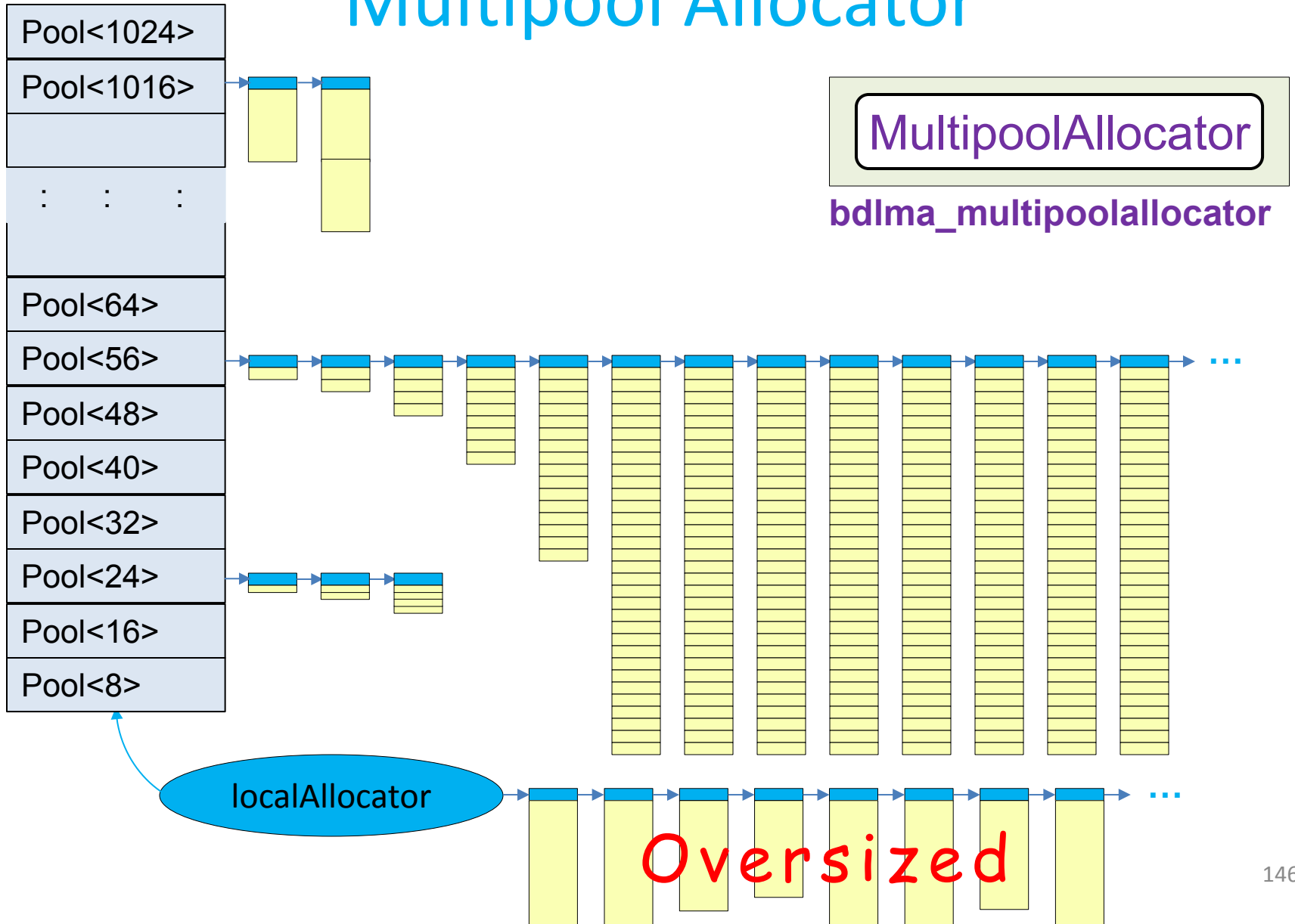
Allocation Strategies: AS7-AS10

Multipool Allocator

Global Allocator

4. Bloomberg Development Environment

Multipool Allocator



2. Understanding the Problem

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Our Tool Chest of Allocation Strategies

Allocation Strategies: AS11-AS14

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2. Understanding the Problem

Characterizing Usage Scenarios

What basic
“size” parameters
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2. Understanding the Problem

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Characterizing Usage Scenarios

Two fundamental (architectural*)
“*size*” *parameters* spring to mind:

N: number of **instructions**
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W: number of active **threads**

*Note that these parameters are deliberately
chosen to be platform independent.

2. Understanding the Problem

Characterizing Usage Scenarios

What “*aspects*”
of software
affect optimal
allocation strategy?

2. Understanding the Problem

Characterizing Usage Scenarios

We initially proposed five “*dimensions*” to help us characterize *aspects* software usage:

D

1

V

2

L

3

U

4

C

5

2. Understanding the Problem

Characterizing Usage Scenarios

We initially proposed five “*dimensions*” to help us characterize *aspects* software usage:

D DENSITY of *allocation operations*

V VARIATION of *allocated sizes*

L LOCALITY of *accessed memory*

U UTILIZATION of *allocated memory*

C CONTENTION of *concurrent allocations*

2. Understanding the Problem

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- They are intended to be scaled (somehow) to fit the range [0 .. 1].
- 0 implies the *minimum* for the *aspect*, whereas 1 implies the *maximum*.
- Note that these “*dimensions*” are far from independent.

2. Understanding the Problem

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DENSITY of *allocation operations*

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Consider: `std::vector<int>`

2. Understanding the Problem

Characterizing Usage Scenarios

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Consider: `std::set<int>`
`std::string`

2. Understanding the Problem

Characterizing Usage Scenarios

LOCALITY of *accessed memory*

I = num access instructions on subregion over duration

M = num bytes of memory in subregion

T = num transitions out of subregion over duration

2. Understanding the Problem

Characterizing Usage Scenarios

*Note that **LOCALITY (L)** can play a critical role in long-running programs even when the allocation **DENSITY (D)** is negligible!*

M = number of memory units
T = number of memory units accessed over duration

$$\mathbf{L}_{physical} = \frac{\mathbf{I}}{\mathbf{M} * \mathbf{T}} \quad \mathbf{L} = \frac{\mathbf{I}}{\mathbf{M} * \mathbf{T}} \quad \mathbf{L}_{temporal} = \frac{\mathbf{I}}{\mathbf{M} * \mathbf{T}}$$

0.0: Subregion is large or not accessed repeatedly.

1.0: Subregion is small and accessed repeatedly.

2. Understanding the Problem

Characterizing Usage Scenarios

UTILIZATION of *allocated memory*

$$\mathbf{U} = \frac{\mathit{maxMemoryInUse}}{\mathit{totalMemoryAllocated}}$$

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2. Understanding the Problem

Characterizing Usage Scenarios

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$$C = \frac{\textit{expectedNumConcurrentAllocations}}{W}$$

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0.0: At most one thread has non-zero (**D**).

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CONTENTION of *concurrent allocations*

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0.0: At most one thread has non-zero (**D**).

1.0: The allocation **DENSITY** (**D**) per thread is 1.

*Note that thread **CONTENTION** (**C**) is strongly correlated with allocation **DENSITY** (**D**).*

2. Understanding the Problem

Characterizing Usage Scenarios

Summary

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Mnemonic:

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Mnemonic: **D.V.L.U.C.** the **DUCK**

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Outline

1. Introduction and Background

What are memory allocators, and why are they useful?

2. Understanding the Problem

What aspects of software affect allocation strategy?

3. Analyzing the Benchmark Data

When and how do you use which allocator, and why?

4. Conclusions

What must we remember about memory allocators?

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3. Analyzing the Benchmark Data

Roadmapping the Benchmarks

Considerations:

- We wanted to explore each dimension to observe its effects on optimal memory allocation.
- Our first thought was to create a single benchmark that spanned all five dimensions.
 - Find the centroid.
 - Vary the arguments along each dimension separately
 - Such a single benchmark is not at all easy.
- We finally settled on four separate benchmarks.
 - Benchmark I addresses the first two dimensions.

3. Analyzing the Benchmark Data

Tested Across Many Problem Sizes

Considerations:

- We tried not to assume the answers we expected.
 - Explored a wide range of problem sizes, **N**.
- Used successive *powers of two*.
 - We often show just the exponent in tables: 5 versus 2^5 .
- Contrasted results across disparate physical sizes.
 - E.g., by holding overall problem size **N** constant.
- Traded-off comparable parameters – E.g.,
 - *Subsystem size* versus *number of subsystems*
 - *Subsystem iterations* versus *experiment repetitions*

3. Analyzing the Benchmark Data

Platforms Used For These Benchmarks

All of results presented here are from a server having *dual* Intel Xeon E5-2620v2 processors.

Each processor:

- Ivy Bridge EP – “Sandy Bridge” architecture (c. 2013)
- 6 cores (for a total of 12 cores)
- 15 MB of L3 cache
- running at a fixed clock rate of 2.1 GHz
- 16GB of DDR3-1600 RAM (13G available to processes)

See: <http://ark.intel.com/products/75789>

3. Analyzing the Benchmark Data

Platforms Used For These Benchmarks

All benchmark programs were

- compiled using gcc-5.1,
- using optimizing “-O3 -march=native”,
- and run under Linux 3.18.

All experiments used only one core at a time

Except, that is, for Benchmark IV, which measures

CONTENTION (**C**) and used more of the available cores.

3. Analyzing the Benchmark Data

Alternative Global Allocators

We investigate alternative global allocators:

➤ *tcmalloc*

➤ *jemalloc*

“We determined that the **native allocators** (e.g., the one currently shipped with GCC on Linux) **performed as well or better.**”

3. Analyzing the Benchmark Data

Benchmark Road Map

I. **Short Running:** Build Up, Use, Tear Down

- Allocation **D**ENSITY and **V**ARIATION in Allocated Sizes

II. **Long Running:** Time-Multiplexed Subsystems

- Access **L**OCALITY – both *Physical* and *Temporal*

III. **Short Running:** Varying Memory Reusability

- Memory **U**TILIZATION

IV. **Multithreaded:** Varying Numbers of Threads

- Allocator **C**ONTENTION

3. Analyzing the Benchmark Data

Benchmark I: **D**ENSITY, **V**ARIATION

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- Memory **U**TILIZATION

IV. **Multithreaded:** Varying Numbers of Threads

- Allocator **C**ONTENTION

3. Analyzing the Benchmark Data

Benchmark I: **DENSITY**, **VARIATION**

Considerations:

- Initially we wanted to investigate allocation **DENSITY**.
 - Focused on allocation/deallocation costs themselves.
- Chose a variety of common data structures.
 - Used `int`, `string`, `vector`, and `unordered_set`.
- Didn't want access **LOCALITY** to dominate results.
 - Wrote to just the first byte of each newly allocated element.
- Later Incorporated **VARIATION** into allocated memory.
 - `vector` objects' capacities were reserved up front.
 - `string` lengths were 33-1000 (uniformly distributed).

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Simple Data Structures

| Label | Data Structure |
|-------|--|
| DS1 | <code>vector<int></code> |
| DS2 | <code>vector<string></code> |
| DS3 | <code>unordered_set<int></code> |
| DS4 | <code>unordered_set<string></code> |

3. Analyzing the Benchmark Data

Benchmark I: **D**ENSITY, **V**ARIATION

Plan:

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Plan:

- For each data structure in a thoughtfully chosen set:
 - Create the data structure.
 - Access it lightly.
 - Destroy it.
 - Repeat (until the problem size N is reached).

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Plan:

- For each data structure in a thoughtfully chosen set:
 - Create the data structure.
 - Access it lightly.
 - Destroy it.
 - Repeat (until the problem size N is reached).
- We chose the overall problem size to be $N = 2^{27}$.
 - The container *size* (S) varies from 2^8 to 2^{16} .
 - The number of experiment repetitions (R) = N/S .

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Contrasting access times across system sizes

Overall Problem Size = 2^{27}

$$\log_2 \mathbf{N} = 27$$

These
are all
exponents
of 2.

| Container Size (S) | Experiment Repititions (R) |
|--------------------|----------------------------|
| 8 | 19 |
| 9 | 18 |
| 10 | 17 |
| 11 | 16 |
| 12 | 15 |
| 13 | 14 |
| 14 | 13 |
| 15 | 12 |
| 16 | 11 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Plan:

- For each data structure in a thoughtfully chosen set:
 - Create the data structure.
 - Access it lightly.
 - Destroy it.
 - Repeat (until the problem size N is reached).
- We chose the overall problem size to be $N = 2^{27}$.
 - The container *size* (S) varies from 2^8 to 2^{16} .
 - The number of repetitions (R) = N/S .
- Each result entry is absolute **RUNTIME** (in seconds).

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS1

Each result entry represents absolute runtime in seconds.

`vector<int>`



| Size | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
|----------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 2^6 | 1.20 | 1.90 | 0.30 | 0.40 | 0.40 | 0.40 | 0.80 | 1.00 | 0.90 | 1.10 | 0.60 | 0.70 | 0.80 | 0.70 |
| 2^7 | 0.90 | 1.60 | 0.30 | 0.40 | 0.40 | 0.40 | 0.50 | 0.70 | 0.60 | 0.70 | 0.50 | 0.50 | 0.60 | 0.50 |
| 2^8 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.30 | 0.40 | 0.60 | 0.50 | 0.60 | 0.30 | 0.50 | 0.50 | 0.50 |
| 2^9 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.40 | 0.30 | 0.50 | 0.50 | 0.50 | 0.30 | 0.40 | 0.40 | 0.40 |
| 2^{10} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{11} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.30 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{12} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{13} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{14} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{15} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{16} | 0.80 | 0.90 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS1

```
vector<int>
```

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|------|-----------|--------|--------|--------|-----------|--------|--------|--------|-----------------|--------|--------|--------|
| | Virtual | | Virtual | | | | Virtual | | | | Virtual | | | |
| | | | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) | (wink) |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 1.20 | 1.90 | 0.30 | 0.40 | 0.40 | 0.40 | 0.80 | 1.00 | 0.90 | 1.10 | 0.60 | 0.70 | 0.80 | 0.70 |
| 2^7 | 0.90 | 1.60 | 0.30 | 0.40 | 0.40 | 0.40 | 0.50 | 0.70 | 0.60 | 0.70 | 0.50 | 0.50 | 0.60 | 0.50 |
| 2^8 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.30 | 0.40 | 0.60 | 0.50 | 0.60 | 0.30 | 0.50 | 0.50 | 0.50 |
| 2^9 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.40 | 0.30 | 0.50 | 0.50 | 0.50 | 0.30 | 0.40 | 0.40 | 0.40 |
| 2^{10} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{11} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.30 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{12} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{13} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{14} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{15} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{16} | 0.80 | 0.90 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS1

`vector<int>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|--------|---------|-----------|------------|------------|------|-----------|------------|------------|------|-----------------|------|-------------|------|
| | | Virtual | | | Virtual | | | Virtual | | | Virtual | | | |
| | AS1 | AS2 | AS3 | (wink) AS4 | (wink) AS5 | AS6 | AS7 | (wink) AS8 | (wink) AS9 | AS10 | (wink) AS11 | AS12 | (wink) AS13 | AS14 |
| 2^6 | 1.20 | 1.90 | 0.30 | 0.40 | 0.40 | 0.40 | 0.80 | 1.00 | 0.90 | 1.10 | 0.60 | 0.70 | 0.80 | 0.70 |
| 2^7 | 0.90 | 1.60 | 0.30 | 0.40 | 0.40 | 0.40 | 0.50 | 0.70 | 0.60 | 0.70 | 0.50 | 0.50 | 0.60 | 0.50 |
| 2^8 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.30 | 0.40 | 0.60 | 0.50 | 0.60 | 0.30 | 0.50 | 0.50 | 0.50 |
| 2^9 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.40 | 0.30 | 0.50 | 0.50 | 0.50 | 0.30 | 0.40 | 0.40 | 0.40 |
| 2^{10} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{11} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.30 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{12} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{13} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{14} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{15} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{16} | 0.80 | 0.90 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS1

`vector<int>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|------|-----------|------|----------------|------|-----------|------|----------------|------|-----------------|------|----------------|------|
| | Virtual | | (wink) | | Virtual (wink) | | (wink) | | Virtual (wink) | | (wink) | | Virtual (wink) | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 1.20 | 1.90 | 0.30 | 0.40 | 0.40 | 0.40 | 0.80 | 1.00 | 0.90 | 1.10 | 0.60 | 0.70 | 0.80 | 0.70 |
| 2^7 | 0.90 | 1.60 | 0.30 | 0.40 | 0.40 | 0.40 | 0.50 | 0.70 | 0.60 | 0.70 | 0.50 | 0.50 | 0.60 | 0.50 |
| 2^8 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.30 | 0.40 | 0.60 | 0.50 | 0.60 | 0.30 | 0.50 | 0.50 | 0.50 |
| 2^9 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.40 | 0.30 | 0.50 | 0.50 | 0.50 | 0.30 | 0.40 | 0.40 | 0.40 |
| 2^{10} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{11} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.30 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{12} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{13} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{14} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{15} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{16} | 0.80 | 0.90 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS1

`vector<int>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 1.20 | 1.90 | 0.30 | 0.40 | 0.40 | 0.40 | 0.80 | 1.00 | 0.90 | 1.10 | 0.60 | 0.70 | 0.80 | 0.70 |
| 2^7 | 0.90 | 1.60 | 0.30 | 0.40 | 0.40 | 0.40 | 0.50 | 0.70 | 0.60 | 0.70 | 0.50 | 0.50 | 0.60 | 0.50 |
| 2^8 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.30 | 0.40 | 0.60 | 0.50 | 0.60 | 0.30 | 0.50 | 0.50 | 0.50 |
| 2^9 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.40 | 0.30 | 0.50 | 0.50 | 0.50 | 0.30 | 0.40 | 0.40 | 0.40 |
| 2^{10} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{11} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.30 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{12} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{13} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{14} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{15} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{16} | 0.80 | 0.90 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS1

`vector<int>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 1.20 | 1.90 | 0.30 | 0.40 | 0.40 | 0.40 | 0.80 | 1.00 | 0.90 | 1.10 | 0.60 | 0.70 | 0.80 | 0.70 |
| 2^7 | 0.90 | 1.60 | 0.30 | 0.40 | 0.40 | 0.40 | 0.50 | 0.70 | 0.60 | 0.70 | 0.50 | 0.50 | 0.60 | 0.50 |
| 2^8 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.30 | 0.40 | 0.60 | 0.50 | 0.60 | 0.30 | 0.50 | 0.50 | 0.50 |
| 2^9 | 0.80 | 1.00 | 0.20 | 0.40 | 0.40 | 0.40 | 0.30 | 0.50 | 0.50 | 0.50 | 0.30 | 0.40 | 0.40 | 0.40 |
| 2^{10} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{11} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.30 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{12} | 0.70 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{13} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{14} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{15} | 0.80 | 0.90 | 0.20 | 0.30 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |
| 2^{16} | 0.80 | 0.90 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 | 0.20 | 0.40 | 0.40 | 0.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS2

`vector<string>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|-------|---------|-------|-----------|-------|---------|-------|-----------------|-------|---------|-------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 68.90 | 67.30 | 12.90 | 12.80 | 13.30 | 12.90 | 18.10 | 17.80 | 18.20 | 17.70 | 15.50 | 14.80 | 15.60 | 14.80 |
| 2^7 | 68.80 | 68.20 | 12.80 | 12.90 | 13.20 | 12.90 | 20.60 | 20.20 | 20.60 | 20.40 | 15.10 | 14.30 | 15.00 | 14.40 |
| 2^8 | 70.80 | 68.90 | 13.20 | 12.80 | 13.60 | 12.90 | 30.80 | 30.40 | 30.70 | 30.30 | 15.30 | 14.60 | 15.40 | 14.70 |
| 2^9 | 73.10 | 71.20 | 13.50 | 13.50 | 13.90 | 13.50 | 38.20 | 37.60 | 38.00 | 37.30 | 15.90 | 15.10 | 15.90 | 15.10 |
| 2^{10} | 75.40 | 74.30 | 13.60 | 13.50 | 14.00 | 13.70 | 41.10 | 40.30 | 41.60 | 40.90 | 16.00 | 15.10 | 15.90 | 15.00 |
| 2^{11} | 76.90 | 74.50 | 13.60 | 13.50 | 14.10 | 13.60 | 43.90 | 43.20 | 43.70 | 42.60 | 16.00 | 15.00 | 16.00 | 15.10 |
| 2^{12} | 76.10 | 74.80 | 13.70 | 13.50 | 14.00 | 13.60 | 41.20 | 38.80 | 40.60 | 39.40 | 15.90 | 14.90 | 15.80 | 15.00 |
| 2^{13} | 76.10 | 74.80 | 13.60 | 13.60 | 14.00 | 13.60 | 41.40 | 39.20 | 41.30 | 39.90 | 15.90 | 15.00 | 15.80 | 14.90 |
| 2^{14} | 78.30 | 76.50 | 13.60 | 13.60 | 14.00 | 13.60 | 45.80 | 42.30 | 44.80 | 44.00 | 16.10 | 15.20 | 16.20 | 15.40 |
| 2^{15} | 90.40 | 91.00 | 20.20 | 20.10 | 20.50 | 20.10 | 62.20 | 58.70 | 62.20 | 58.20 | 26.00 | 25.00 | 26.00 | 24.90 |
| 2^{16} | 103.0 | 103.0 | 21.50 | 21.30 | 21.80 | 21.30 | 66.50 | 59.20 | 65.10 | 59.90 | 27.00 | 25.30 | 27.10 | 25.20 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS3

`unordered_set<int>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 10.20 | 11.00 | 5.08 | 4.88 | 5.62 | 5.34 | 7.16 | 7.12 | 7.50 | 7.20 | 6.19 | 5.73 | 6.40 | 5.81 |
| 2^7 | 12.50 | 13.30 | 5.04 | 4.81 | 5.68 | 5.24 | 6.37 | 6.22 | 6.71 | 6.31 | 5.80 | 5.46 | 6.08 | 5.50 |
| 2^8 | 15.80 | 16.40 | 4.99 | 4.79 | 5.54 | 5.22 | 5.95 | 5.81 | 6.21 | 5.92 | 5.65 | 5.32 | 5.82 | 5.40 |
| 2^9 | 18.30 | 19.00 | 5.01 | 4.80 | 5.53 | 5.18 | 5.78 | 5.56 | 6.01 | 5.70 | 5.56 | 5.20 | 5.76 | 5.21 |
| 2^{10} | 21.40 | 22.30 | 4.99 | 4.83 | 5.55 | 5.20 | 5.72 | 5.46 | 5.95 | 5.55 | 5.52 | 5.27 | 5.68 | 5.24 |
| 2^{11} | 25.50 | 26.10 | 4.98 | 4.81 | 5.56 | 5.16 | 5.67 | 5.44 | 5.86 | 5.65 | 5.53 | 5.23 | 5.69 | 5.26 |
| 2^{12} | 27.10 | 28.00 | 5.02 | 4.81 | 5.55 | 5.20 | 6.42 | 6.10 | 6.57 | 6.25 | 5.51 | 5.12 | 5.68 | 5.27 |
| 2^{13} | 27.90 | 28.80 | 5.03 | 4.81 | 5.59 | 5.21 | 7.34 | 6.91 | 7.46 | 7.03 | 5.61 | 5.16 | 5.71 | 5.24 |
| 2^{14} | 28.50 | 29.00 | 5.03 | 4.80 | 5.58 | 5.26 | 7.03 | 6.59 | 7.18 | 6.68 | 5.64 | 5.19 | 5.80 | 5.34 |
| 2^{15} | 28.30 | 29.20 | 5.03 | 4.78 | 5.56 | 5.28 | 7.11 | 6.65 | 7.20 | 6.83 | 5.68 | 5.17 | 5.78 | 5.24 |
| 2^{16} | 31.60 | 31.80 | 5.02 | 4.76 | 5.60 | 5.22 | 6.79 | 6.37 | 6.93 | 6.46 | 5.68 | 5.17 | 5.79 | 5.24 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS4 unordered_set<string>

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|-------|---------|-------|-----------|-------|---------|-------|-----------------|-------|---------|-------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 103.0 | 120.0 | 52.20 | 51.90 | 52.40 | 51.20 | 58.40 | 57.60 | 59.70 | 58.90 | 55.10 | 54.10 | 56.90 | 55.30 |
| 2^7 | 103.0 | 122.0 | 52.50 | 52.10 | 52.90 | 51.80 | 63.30 | 61.90 | 64.40 | 63.80 | 55.30 | 54.00 | 56.80 | 55.70 |
| 2^8 | 109.0 | 128.0 | 53.60 | 53.00 | 53.70 | 52.60 | 76.30 | 74.70 | 77.40 | 75.90 | 56.50 | 54.90 | 57.90 | 56.70 |
| 2^9 | 113.0 | 134.0 | 54.50 | 53.40 | 54.90 | 53.00 | 83.10 | 81.70 | 82.80 | 81.40 | 57.30 | 56.70 | 58.00 | 56.40 |
| 2^{10} | 119.0 | 143.0 | 56.60 | 54.90 | 56.90 | 54.60 | 87.60 | 85.90 | 88.10 | 86.50 | 58.80 | 56.90 | 59.20 | 57.30 |
| 2^{11} | 122.0 | 144.0 | 57.00 | 55.30 | 57.70 | 54.90 | 90.70 | 89.20 | 90.70 | 88.40 | 59.40 | 57.60 | 60.00 | 57.80 |
| 2^{12} | 122.0 | 146.0 | 57.90 | 55.90 | 58.40 | 55.70 | 93.20 | 90.70 | 93.20 | 90.70 | 60.50 | 58.30 | 60.70 | 58.40 |
| 2^{13} | 124.0 | 148.0 | 58.20 | 56.30 | 58.50 | 55.90 | 95.10 | 91.50 | 94.30 | 92.00 | 60.50 | 58.20 | 60.70 | 58.70 |
| 2^{14} | 139.0 | 166.0 | 59.10 | 57.30 | 59.60 | 56.80 | 98.50 | 94.10 | 97.80 | 95.80 | 61.80 | 59.60 | 62.20 | 60.00 |
| 2^{15} | 176.0 | 211.0 | 66.00 | 62.70 | 66.20 | 62.40 | 121.0 | 115.0 | 122.0 | 115.0 | 76.50 | 73.30 | 76.80 | 74.00 |
| 2^{16} | 196.0 | 232.0 | 78.50 | 72.00 | 79.10 | 71.00 | 137.0 | 127.0 | 136.0 | 127.0 | 87.10 | 82.40 | 87.80 | 82.90 |

3. Analyzing the Benchmark Data

Benchmark I: **D**ENSITY, **V**ARIATION

Questions
and/or
Discussion?

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Composite Data Structures

| Label | Data Structure |
|-------|---|
| DS5 | <code>vector<vector<int>></code> |
| DS6 | <code>vector<vector<string>></code> |
| DS7 | <code>vector<unordered_set<int>></code> |
| DS8 | <code>vector<unordered_set<string>></code> |
| DS9 | <code>unordered_set<vector<int>></code> |
| DS10 | <code>unordered_set<vector<string>></code> |
| DS11 | <code>unordered_set<unordered_set<int>></code> |
| DS12 | <code>unordered_set<unordered_set<string>></code> |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Composite Data Structures:

- The composite data elements were much larger.
- We wanted runtimes to be roughly comparable.
- We kept the overall problem size $N = 2^{27}$.
 - The outer container *size* (S) *still* varies from 2^8 to 2^{16} .
 - The inner container size (K) was fixed at 2^7 .
 - Now, the number of repetitions (R) = $N/(K \cdot S)$.

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Contrasting access times across system sizes

Overall Problem Size = 2^{27}

These are all
exponents of 2.

$$\log_2 \mathbf{N} = 27$$

| Outer Container Size (S) | Inner Container Size (fixed) | Experiment Repetitions (R) |
|--------------------------|------------------------------|----------------------------|
| 8 | 7 | 12 |
| 9 | 7 | 11 |
| 10 | 7 | 10 |
| 11 | 7 | 9 |
| 12 | 7 | 8 |
| 13 | 7 | 7 |
| 14 | 7 | 6 |
| 15 | 7 | 5 |
| 16 | 7 | 4 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

Composite Data Structures:

- The composite data elements were much larger.
- We wanted runtimes to be roughly comparable.
- We kept the overall problem size $N = 2^{27}$.
 - The outer container *size* (S) *still* varies from 2^8 to 2^{16} .
 - The inner container size (K) was fixed at 2^7 .
 - Now, the number of repetitions (R) = $N/(K \cdot S)$.
- These adjustment kept runtimes manageable.
 - The number of leaf elements remained comparable.

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS5

vector<vector<int>>

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 0.97 | 1.00 | 0.19 | 0.13 | 0.20 | 0.17 | 0.24 | 0.20 | 0.20 | 0.21 | 0.21 | 0.19 | 0.20 | 0.21 |
| 2^7 | 0.96 | 0.96 | 0.22 | 0.16 | 0.18 | 0.14 | 0.21 | 0.20 | 0.19 | 0.20 | 0.16 | 0.20 | 0.21 | 0.19 |
| 2^8 | 0.99 | 1.00 | 0.19 | 0.13 | 0.18 | 0.17 | 0.27 | 0.30 | 0.27 | 0.29 | 0.19 | 0.19 | 0.20 | 0.21 |
| 2^9 | 0.99 | 1.02 | 0.19 | 0.13 | 0.18 | 0.14 | 0.36 | 0.33 | 0.33 | 0.36 | 0.19 | 0.15 | 0.20 | 0.20 |
| 2^{10} | 1.01 | 1.04 | 0.19 | 0.18 | 0.19 | 0.14 | 0.37 | 0.36 | 0.36 | 0.38 | 0.22 | 0.19 | 0.20 | 0.22 |
| 2^{11} | 1.02 | 1.05 | 0.19 | 0.13 | 0.19 | 0.14 | 0.36 | 0.35 | 0.36 | 0.36 | 0.20 | 0.15 | 0.20 | 0.22 |
| 2^{12} | 1.03 | 1.05 | 0.19 | 0.19 | 0.22 | 0.18 | 0.33 | 0.36 | 0.32 | 0.32 | 0.20 | 0.21 | 0.20 | 0.19 |
| 2^{13} | 1.02 | 1.05 | 0.19 | 0.13 | 0.22 | 0.19 | 0.35 | 0.35 | 0.34 | 0.33 | 0.20 | 0.21 | 0.22 | 0.19 |
| 2^{14} | 1.05 | 1.10 | 0.19 | 0.17 | 0.19 | 0.16 | 0.38 | 0.36 | 0.38 | 0.37 | 0.17 | 0.19 | 0.20 | 0.19 |
| 2^{15} | 1.13 | 1.18 | 0.22 | 0.19 | 0.19 | 0.16 | 0.50 | 0.45 | 0.47 | 0.45 | 0.21 | 0.21 | 0.17 | 0.18 |
| 2^{16} | 1.29 | 1.32 | 0.22 | 0.19 | 0.20 | 0.17 | 0.54 | 0.47 | 0.52 | 0.50 | 0.22 | 0.21 | 0.22 | 0.21 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS6

vector<vector<string>>

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|-------|---------|-------|-----------|-------|---------|-------|-----------------|-------|---------|-------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 72.60 | 72.70 | 9.06 | 9.06 | 9.36 | 8.98 | 41.70 | 40.00 | 41.20 | 39.20 | 11.20 | 10.30 | 11.20 | 10.30 |
| 2^7 | 74.90 | 76.00 | 8.92 | 8.98 | 9.29 | 8.89 | 46.50 | 44.80 | 46.00 | 43.00 | 11.40 | 11.00 | 12.70 | 10.30 |
| 2^8 | 85.50 | 85.20 | 17.10 | 17.40 | 17.30 | 16.90 | 62.90 | 58.40 | 61.30 | 58.40 | 22.80 | 22.50 | 23.30 | 22.00 |
| 2^9 | 96.40 | 96.30 | 18.40 | 18.70 | 19.00 | 18.40 | 66.20 | 59.00 | 64.70 | 59.30 | 24.20 | 22.70 | 24.50 | 22.30 |
| 2^{10} | 102.0 | 102.0 | 18.70 | 18.60 | 19.10 | 18.60 | 67.00 | 59.60 | 65.90 | 59.00 | 24.80 | 22.50 | 24.80 | 22.50 |
| 2^{11} | 102.0 | 101.0 | 18.40 | 18.70 | 19.20 | 18.20 | 62.40 | 55.00 | 61.30 | 54.20 | 24.80 | 22.60 | 25.10 | 22.30 |
| 2^{12} | 104.0 | 103.0 | 18.50 | 18.70 | 19.40 | 18.30 | 61.60 | 54.20 | 60.50 | 53.40 | 24.90 | 22.70 | 25.10 | 22.30 |
| 2^{13} | 103.0 | 104.0 | 18.80 | 18.40 | 19.00 | 18.60 | 61.80 | 53.40 | 59.90 | 53.50 | 25.30 | 22.60 | 25.10 | 22.60 |
| 2^{14} | 97.10 | 96.30 | 19.20 | 19.60 | 20.10 | 19.20 | 60.60 | 53.70 | 60.20 | 52.90 | 29.00 | 26.70 | 29.20 | 26.30 |
| 2^{15} | 88.10 | 88.70 | 23.40 | 23.20 | 23.70 | 23.40 | 62.60 | 54.40 | 60.90 | 53.90 | 33.40 | 30.60 | 33.20 | 30.70 |
| 2^{16} | 76.70 | 76.70 | 25.00 | 25.30 | 25.80 | 25.00 | 63.40 | 54.80 | 62.90 | 54.30 | 35.00 | 32.80 | 35.50 | 32.40 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS7

`vector<unordered_set<int>>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 28.80 | 28.70 | 2.97 | 2.69 | 3.43 | 2.98 | 4.89 | 4.37 | 5.33 | 4.73 | 3.21 | 2.65 | 3.64 | 3.05 |
| 2^7 | 28.30 | 28.50 | 2.97 | 2.66 | 3.36 | 2.95 | 4.99 | 4.44 | 5.43 | 4.91 | 3.20 | 2.62 | 3.61 | 2.97 |
| 2^8 | 28.20 | 28.10 | 2.94 | 2.62 | 3.33 | 2.92 | 5.02 | 4.53 | 5.53 | 4.97 | 3.23 | 2.60 | 3.60 | 3.01 |
| 2^9 | 31.80 | 31.70 | 2.92 | 2.61 | 3.33 | 2.93 | 5.08 | 4.54 | 5.52 | 4.92 | 3.16 | 2.58 | 3.58 | 2.96 |
| 2^{10} | 46.60 | 47.20 | 2.92 | 2.61 | 3.33 | 2.89 | 5.07 | 4.49 | 5.48 | 4.93 | 3.15 | 2.58 | 3.57 | 2.98 |
| 2^{11} | 54.30 | 54.10 | 2.92 | 2.61 | 3.33 | 2.89 | 5.63 | 4.75 | 5.88 | 5.37 | 3.16 | 2.60 | 3.61 | 2.98 |
| 2^{12} | 54.70 | 54.80 | 2.96 | 2.66 | 3.34 | 2.91 | 6.90 | 5.79 | 7.28 | 6.23 | 4.15 | 3.05 | 4.58 | 3.40 |
| 2^{13} | 55.10 | 56.00 | 3.51 | 2.95 | 3.77 | 3.21 | 7.01 | 6.03 | 7.47 | 6.35 | 4.27 | 3.08 | 4.65 | 3.48 |
| 2^{14} | 51.00 | 50.90 | 3.53 | 2.99 | 3.81 | 3.25 | 7.08 | 6.00 | 7.47 | 6.46 | 4.29 | 3.14 | 4.71 | 3.47 |
| 2^{15} | 44.80 | 45.40 | 3.58 | 3.01 | 3.83 | 3.26 | 7.07 | 6.04 | 7.55 | 6.52 | 4.35 | 3.14 | 4.75 | 3.53 |
| 2^{16} | 38.20 | 38.20 | 3.58 | 3.06 | 3.86 | 3.30 | 7.14 | 6.11 | 7.58 | 6.47 | 4.37 | 3.18 | 4.80 | 3.54 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS8

`vector<unordered_set<string>>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|-------|---------|-------|-----------|-------|---------|-------|-----------------|-------|---------|-------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 114.0 | 116.0 | 26.00 | 23.80 | 26.30 | 24.00 | 56.20 | 54.70 | 56.90 | 54.60 | 27.50 | 25.80 | 27.90 | 26.00 |
| 2^7 | 123.0 | 130.0 | 26.50 | 24.40 | 25.70 | 23.50 | 62.70 | 60.10 | 62.70 | 60.50 | 27.50 | 26.30 | 28.20 | 26.10 |
| 2^8 | 162.0 | 171.0 | 31.70 | 27.30 | 32.20 | 27.80 | 78.00 | 74.20 | 79.20 | 73.90 | 35.00 | 32.00 | 35.50 | 32.50 |
| 2^9 | 175.0 | 181.0 | 36.80 | 28.00 | 38.10 | 28.00 | 81.70 | 74.10 | 81.20 | 74.90 | 36.30 | 32.10 | 37.20 | 32.10 |
| 2^{10} | 176.0 | 183.0 | 40.00 | 28.90 | 37.40 | 28.20 | 82.10 | 74.50 | 82.10 | 74.70 | 36.90 | 32.00 | 37.40 | 32.20 |
| 2^{11} | 176.0 | 183.0 | 39.30 | 28.00 | 37.30 | 28.00 | 81.40 | 74.40 | 82.00 | 74.30 | 36.90 | 32.10 | 37.80 | 32.10 |
| 2^{12} | 179.0 | 185.0 | 39.40 | 28.00 | 37.10 | 28.00 | 81.80 | 74.10 | 81.60 | 74.40 | 37.00 | 32.00 | 37.80 | 32.20 |
| 2^{13} | 173.0 | 178.0 | 39.60 | 27.90 | 36.90 | 28.20 | 81.80 | 73.60 | 81.50 | 74.30 | 37.20 | 32.00 | 37.80 | 32.40 |
| 2^{14} | 157.0 | 160.0 | 41.00 | 29.90 | 38.80 | 29.90 | 81.50 | 74.10 | 82.20 | 74.00 | 44.00 | 39.30 | 45.10 | 39.20 |
| 2^{15} | 122.0 | 131.0 | 47.60 | 35.80 | 44.80 | 36.20 | 85.20 | 75.50 | 83.70 | 76.10 | 50.50 | 45.20 | 51.00 | 45.50 |
| 2^{16} | 95.40 | 106.0 | 51.40 | 40.50 | 48.10 | 38.90 | 84.80 | 76.20 | 88.70 | 75.90 | 53.10 | 48.50 | 54.80 | 48.20 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS9

`unordered_set<vector<int>>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 0.97 | 0.94 | 0.23 | 0.19 | 0.24 | 0.21 | 0.26 | 0.27 | 0.30 | 0.26 | 0.25 | 0.26 | 0.25 | 0.24 |
| 2^7 | 1.40 | 1.43 | 0.22 | 0.21 | 0.22 | 0.19 | 0.24 | 0.26 | 0.25 | 0.27 | 0.24 | 0.26 | 0.24 | 0.24 |
| 2^8 | 1.35 | 1.39 | 0.25 | 0.22 | 0.24 | 0.23 | 0.30 | 0.35 | 0.34 | 0.33 | 0.24 | 0.23 | 0.25 | 0.24 |
| 2^9 | 1.29 | 1.32 | 0.22 | 0.18 | 0.22 | 0.17 | 0.37 | 0.38 | 0.37 | 0.36 | 0.23 | 0.22 | 0.19 | 0.22 |
| 2^{10} | 1.32 | 1.38 | 0.24 | 0.22 | 0.22 | 0.19 | 0.41 | 0.39 | 0.42 | 0.39 | 0.23 | 0.24 | 0.23 | 0.22 |
| 2^{11} | 1.34 | 1.36 | 0.23 | 0.21 | 0.22 | 0.17 | 0.44 | 0.42 | 0.43 | 0.41 | 0.23 | 0.23 | 0.25 | 0.22 |
| 2^{12} | 1.34 | 1.41 | 0.22 | 0.20 | 0.22 | 0.16 | 0.46 | 0.42 | 0.45 | 0.43 | 0.23 | 0.17 | 0.27 | 0.22 |
| 2^{13} | 1.46 | 1.54 | 0.22 | 0.18 | 0.22 | 0.16 | 0.48 | 0.49 | 0.49 | 0.48 | 0.23 | 0.21 | 0.25 | 0.21 |
| 2^{14} | 1.53 | 1.61 | 0.22 | 0.17 | 0.22 | 0.18 | 0.43 | 0.42 | 0.45 | 0.41 | 0.24 | 0.22 | 0.24 | 0.22 |
| 2^{15} | 1.61 | 1.76 | 0.25 | 0.21 | 0.24 | 0.19 | 0.50 | 0.49 | 0.50 | 0.49 | 0.24 | 0.18 | 0.23 | 0.21 |
| 2^{16} | 1.79 | 1.92 | 0.28 | 0.25 | 0.29 | 0.24 | 0.55 | 0.51 | 0.56 | 0.55 | 0.30 | 0.23 | 0.32 | 0.24 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS10

`unordered_set<vector<string>>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|-------|---------|-------|-----------|-------|---------|-------|-----------------|-------|---------|-------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 73.00 | 73.20 | 9.41 | 9.39 | 9.34 | 8.97 | 41.70 | 39.70 | 41.10 | 39.30 | 11.20 | 10.40 | 11.20 | 10.30 |
| 2^7 | 74.70 | 75.30 | 9.32 | 9.34 | 9.24 | 8.87 | 46.20 | 43.70 | 45.30 | 44.20 | 12.70 | 10.60 | 11.40 | 10.80 |
| 2^8 | 83.10 | 85.40 | 18.00 | 17.30 | 16.90 | 17.20 | 62.20 | 58.90 | 61.90 | 57.60 | 23.20 | 22.30 | 23.10 | 22.40 |
| 2^9 | 91.40 | 94.90 | 19.00 | 19.00 | 18.80 | 18.60 | 65.00 | 59.90 | 64.40 | 58.90 | 24.30 | 22.60 | 24.10 | 22.60 |
| 2^{10} | 98.20 | 101.0 | 19.20 | 18.90 | 19.10 | 18.60 | 66.50 | 59.70 | 65.40 | 59.10 | 24.80 | 22.60 | 24.60 | 22.70 |
| 2^{11} | 99.50 | 101.0 | 19.00 | 19.10 | 19.30 | 18.40 | 66.90 | 59.50 | 66.10 | 58.70 | 24.90 | 22.70 | 25.10 | 22.50 |
| 2^{12} | 102.0 | 105.0 | 19.40 | 19.00 | 19.20 | 18.80 | 67.00 | 58.90 | 65.80 | 59.40 | 25.30 | 22.60 | 25.10 | 22.70 |
| 2^{13} | 103.0 | 104.0 | 19.00 | 19.20 | 19.40 | 18.40 | 66.70 | 59.20 | 66.20 | 58.20 | 25.30 | 22.90 | 25.50 | 22.60 |
| 2^{14} | 95.80 | 97.20 | 19.80 | 20.00 | 20.30 | 19.30 | 62.80 | 55.60 | 61.90 | 54.30 | 29.20 | 26.80 | 29.60 | 26.50 |
| 2^{15} | 87.10 | 89.80 | 24.00 | 23.70 | 24.00 | 23.50 | 64.30 | 55.00 | 61.90 | 54.90 | 33.60 | 30.80 | 33.50 | 31.00 |
| 2^{16} | 77.10 | 78.20 | 25.60 | 25.70 | 26.00 | 25.10 | 63.90 | 55.50 | 63.30 | 54.50 | 35.30 | 33.00 | 35.70 | 32.60 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS11

`unordered_set<unordered_set<int>>`

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|------|---------|------|-----------|------|---------|------|-----------------|------|---------|------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 28.70 | 29.10 | 3.06 | 2.75 | 3.55 | 3.14 | 4.96 | 4.40 | 5.41 | 4.84 | 3.24 | 2.73 | 3.73 | 3.15 |
| 2^7 | 29.10 | 29.00 | 3.02 | 2.71 | 3.47 | 3.06 | 5.03 | 4.52 | 5.49 | 4.89 | 3.23 | 2.66 | 3.68 | 3.08 |
| 2^8 | 28.80 | 29.10 | 3.00 | 2.68 | 3.45 | 3.04 | 5.18 | 4.55 | 5.57 | 4.98 | 3.24 | 2.66 | 3.65 | 3.06 |
| 2^9 | 31.80 | 32.30 | 2.99 | 2.64 | 3.43 | 2.98 | 5.12 | 4.54 | 5.55 | 4.95 | 3.22 | 2.60 | 3.65 | 2.99 |
| 2^{10} | 46.50 | 47.10 | 2.95 | 2.65 | 3.40 | 2.99 | 5.13 | 4.57 | 5.62 | 4.96 | 3.21 | 2.58 | 3.62 | 2.97 |
| 2^{11} | 53.30 | 53.50 | 2.94 | 2.64 | 3.43 | 2.96 | 5.58 | 4.84 | 5.75 | 5.39 | 3.20 | 2.63 | 3.67 | 3.01 |
| 2^{12} | 54.60 | 55.00 | 3.02 | 2.66 | 3.43 | 2.98 | 6.47 | 5.94 | 6.99 | 6.28 | 3.83 | 3.00 | 4.21 | 3.38 |
| 2^{13} | 56.50 | 56.50 | 3.38 | 2.98 | 3.72 | 3.26 | 7.04 | 6.04 | 7.48 | 6.45 | 4.15 | 3.03 | 4.58 | 3.39 |
| 2^{14} | 52.10 | 52.20 | 3.50 | 2.99 | 3.88 | 3.25 | 7.35 | 6.07 | 7.83 | 6.59 | 4.33 | 3.05 | 4.76 | 3.38 |
| 2^{15} | 45.70 | 46.20 | 3.62 | 2.99 | 3.95 | 3.27 | 7.70 | 6.39 | 8.11 | 6.83 | 4.43 | 3.06 | 4.81 | 3.44 |
| 2^{16} | 39.30 | 39.30 | 3.72 | 3.05 | 4.03 | 3.31 | 7.57 | 6.30 | 8.09 | 6.61 | 4.52 | 3.10 | 4.92 | 3.45 |

3. Analyzing the Benchmark Data

Benchmark I: DENSITY, VARIATION

DS12 unordered_set<unordered_set<string>>

| Size | Global | | Monotonic | | | | Multipool | | | | Multipool<Mono> | | | |
|----------|---------|-------|-----------|-------|---------|-------|-----------|-------|---------|-------|-----------------|-------|---------|-------|
| | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | | (wink) | | Virtual | |
| | AS1 | AS2 | AS3 | AS4 | AS5 | AS6 | AS7 | AS8 | AS9 | AS10 | AS11 | AS12 | AS13 | AS14 |
| 2^6 | 121.0 | 125.0 | 25.90 | 23.70 | 26.10 | 23.90 | 56.30 | 54.50 | 56.70 | 54.70 | 27.40 | 25.80 | 27.80 | 26.00 |
| 2^7 | 141.0 | 145.0 | 26.40 | 24.30 | 25.60 | 23.40 | 62.10 | 59.60 | 62.50 | 60.00 | 27.90 | 25.80 | 28.30 | 25.80 |
| 2^8 | 165.0 | 173.0 | 31.50 | 27.30 | 32.20 | 27.70 | 77.40 | 73.70 | 77.80 | 74.20 | 34.80 | 31.90 | 35.60 | 32.20 |
| 2^9 | 171.0 | 178.0 | 35.90 | 27.60 | 34.40 | 27.80 | 80.00 | 73.70 | 79.70 | 74.60 | 35.70 | 32.00 | 36.50 | 31.90 |
| 2^{10} | 177.0 | 182.0 | 38.70 | 28.60 | 35.60 | 27.90 | 81.10 | 74.30 | 81.30 | 74.30 | 36.70 | 31.80 | 37.10 | 32.00 |
| 2^{11} | 177.0 | 183.0 | 38.20 | 27.60 | 36.20 | 27.70 | 81.30 | 74.30 | 82.20 | 74.10 | 37.00 | 32.00 | 37.80 | 31.90 |
| 2^{12} | 179.0 | 186.0 | 39.10 | 27.70 | 36.50 | 28.00 | 81.60 | 73.50 | 81.50 | 74.10 | 37.30 | 31.80 | 37.90 | 32.10 |
| 2^{13} | 165.0 | 169.0 | 39.00 | 27.80 | 36.70 | 27.80 | 81.30 | 73.90 | 82.80 | 73.50 | 37.30 | 32.10 | 38.30 | 32.10 |
| 2^{14} | 153.0 | 156.0 | 40.90 | 29.60 | 38.70 | 29.60 | 81.50 | 74.10 | 82.40 | 73.70 | 44.40 | 39.20 | 45.40 | 39.10 |
| 2^{15} | 122.0 | 131.0 | 47.60 | 35.70 | 44.80 | 36.10 | 85.70 | 75.20 | 83.90 | 75.40 | 51.00 | 45.10 | 51.40 | 45.50 |
| 2^{16} | 100.0 | 111.0 | 51.40 | 40.40 | 48.00 | 38.80 | 85.10 | 75.50 | 86.20 | 75.60 | 53.60 | 48.40 | 54.60 | 48.20 |

3. Analyzing the Benchmark Data

Benchmark I: **D**ENSITY, **V**ARIATION

Questions
and/or
Discussion?

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I. Short Running: Build Up, Use, Tear Down

- Allocation **D**ENSITY and **V**ARIATION in Allocated Sizes

II. Long Running: Time-Multiplexed Subsystems

- Access **L**OCALITY – both *Physical* and *Temporal*

III. Short Running: Varying Memory Reusability

- Memory **U**TILIZATION

IV. Multithreaded: Varying Numbers of Threads

- Allocator **C**ONTENTION

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Considerations:

- Investigate access **LOCALITY**.
 - Observe its effects both *physically* and *temporally*.
- Simulate concurrent subsystems.
 - Vary both their *sizes* and *time slices* independently.
- Access **LOCALITY** should dominate results.
 - Time accessing data should be substantial (hours).
 - Time to set-up/tear-down should be negligible (seconds).
- Simulate use of local allocator using global allocator.
 - Measure runtime affects of *memory diffusion* using *ASO*.

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Creation Plan:

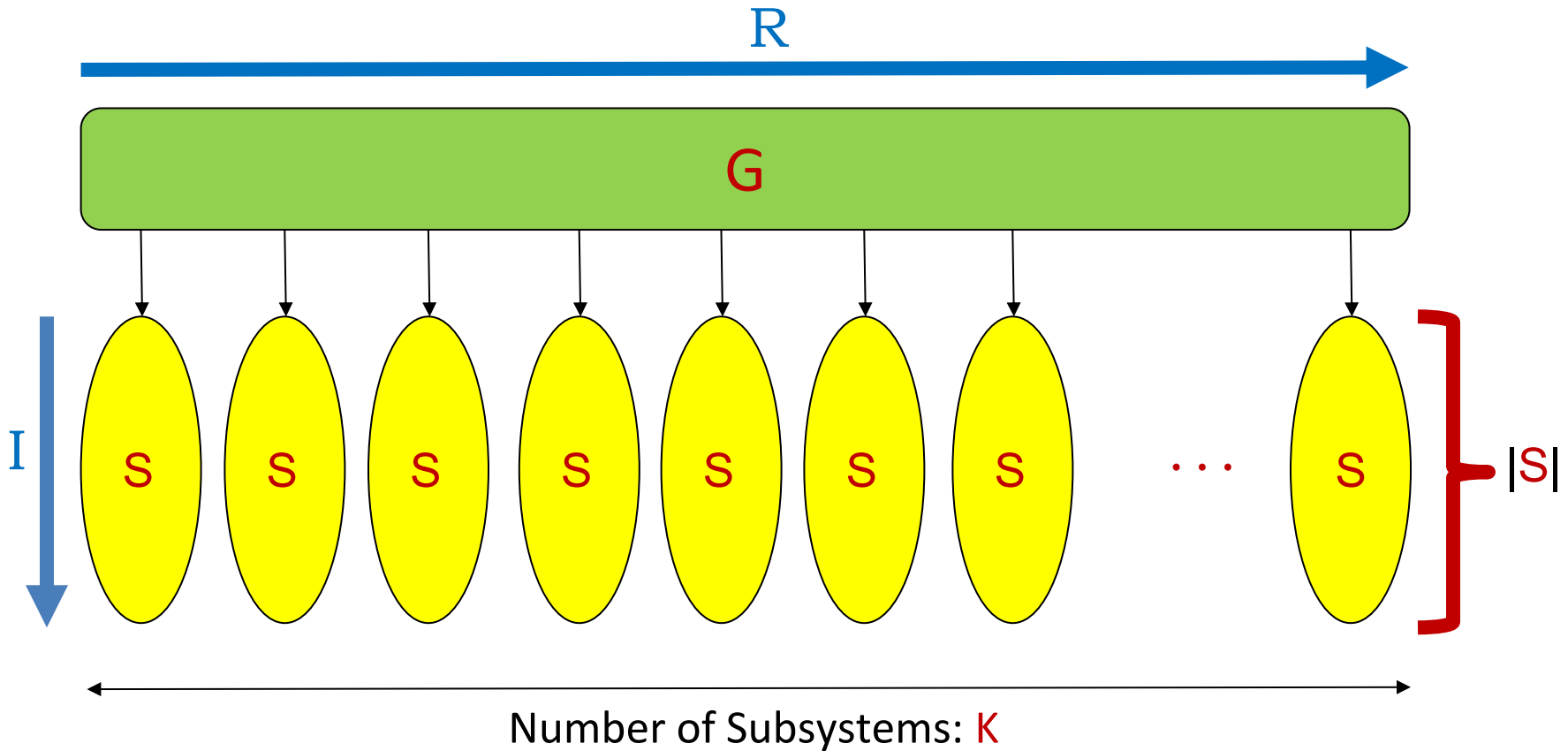
- Build up a data structure **G**: `vector<list<int>>`
 - of K subsystems: `G.size()`
 - each of size |**S**|: `S.length()`
- Tear down data structure **G**.
 - Occurs automatically at the end of the program.
- The result is an initialized data structure **G**.
 - Also used to measure the Build-up + Tear-down runtime.

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Problem Size: $N = |G| \cdot I \cdot R$

Physical System Size $|G| = K \cdot |S|$

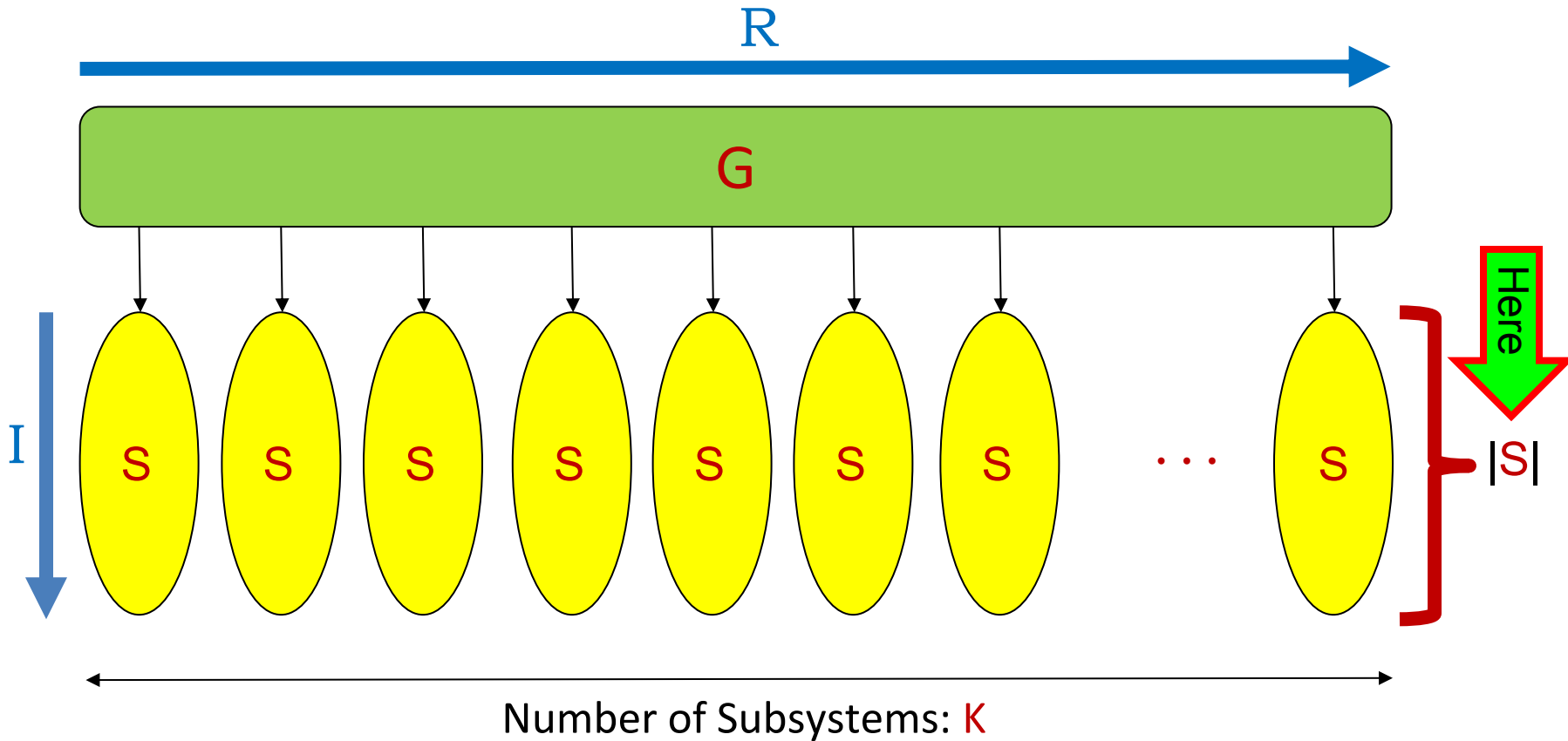


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Problem Size: $N = |G| \cdot I \cdot R$

Physical System Size $|G| = K \cdot |S|$

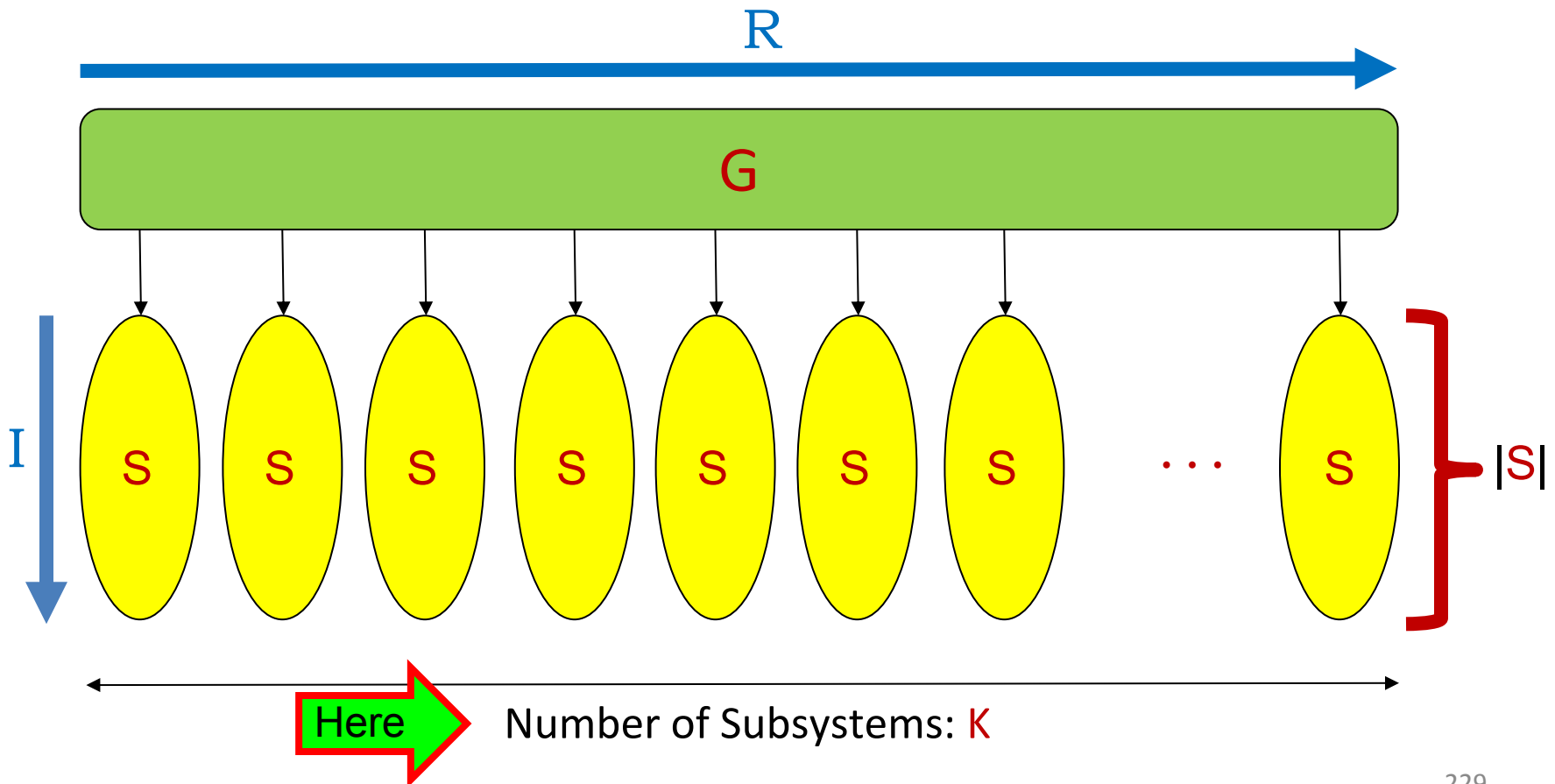


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Problem Size: $N = |G| \cdot I \cdot R$

Physical System Size $|G| = K \cdot |S|$

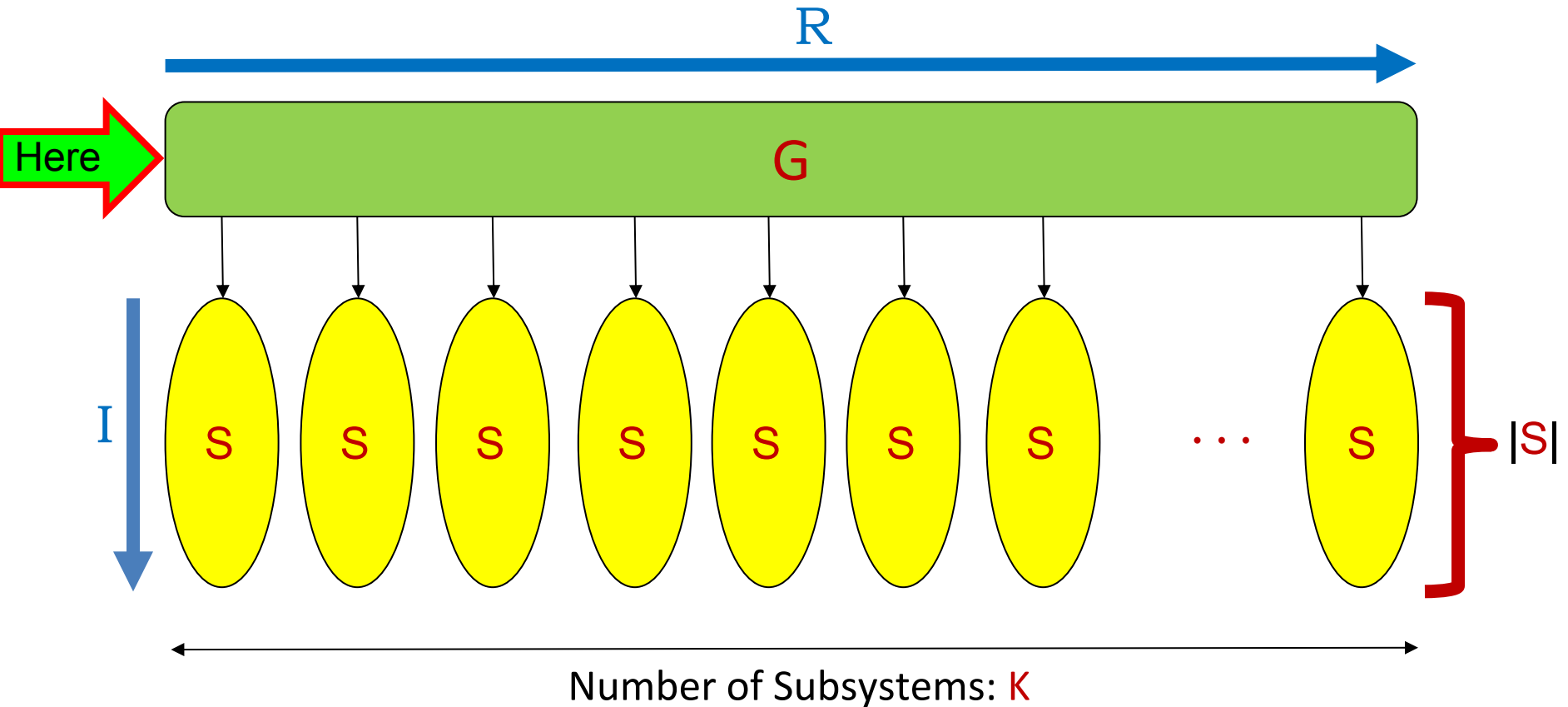


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

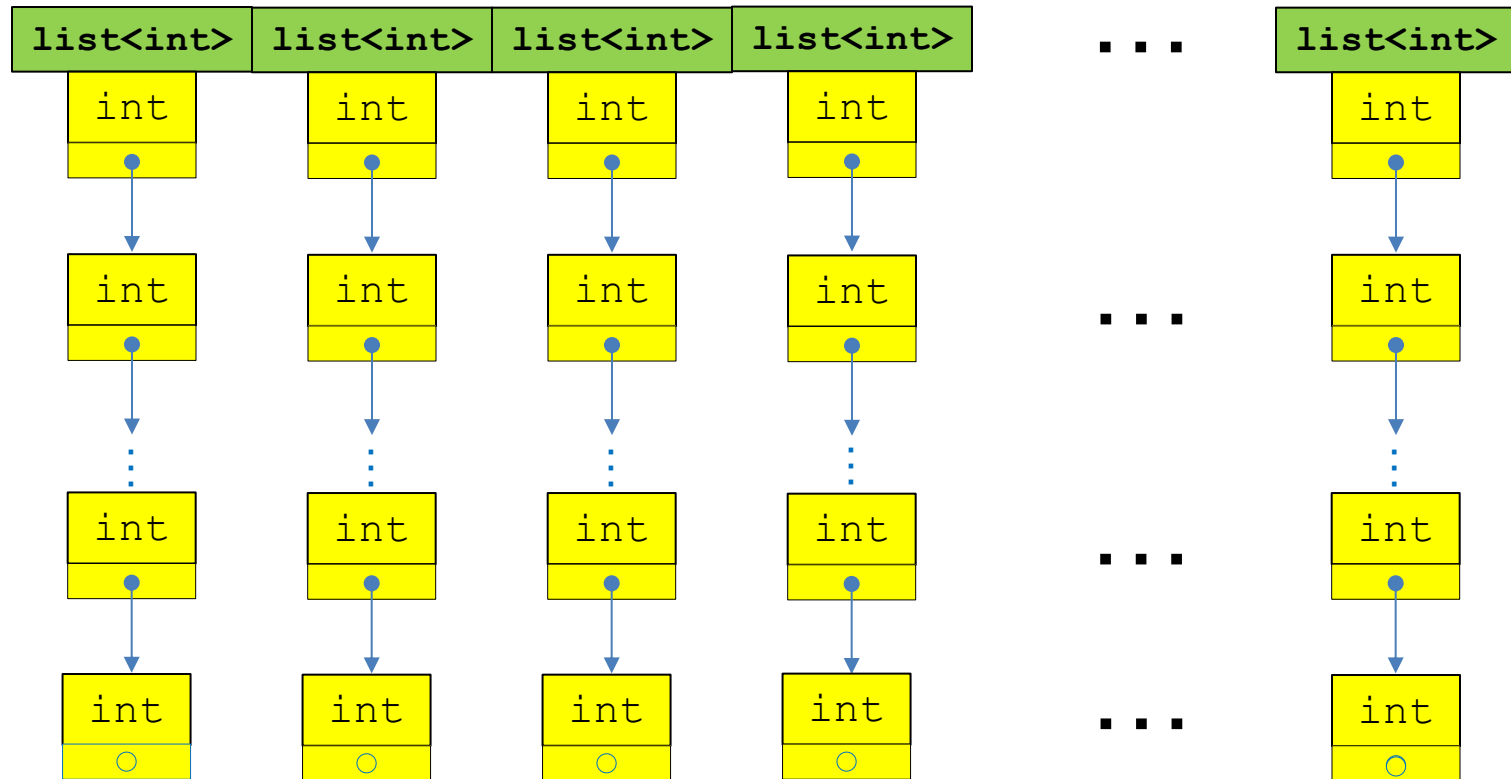
$$\text{Problem Size: } \mathbf{N} = |\mathbf{G}| \cdot \mathbf{I} \cdot \mathbf{R}$$

Here \rightarrow Physical System Size $|\mathbf{G}| = \mathbf{K} \cdot |\mathbf{S}|$



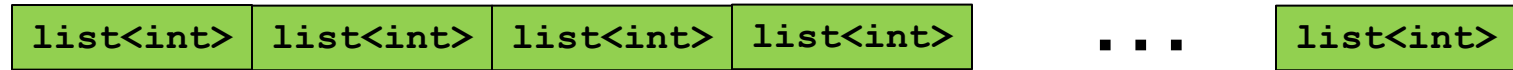
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



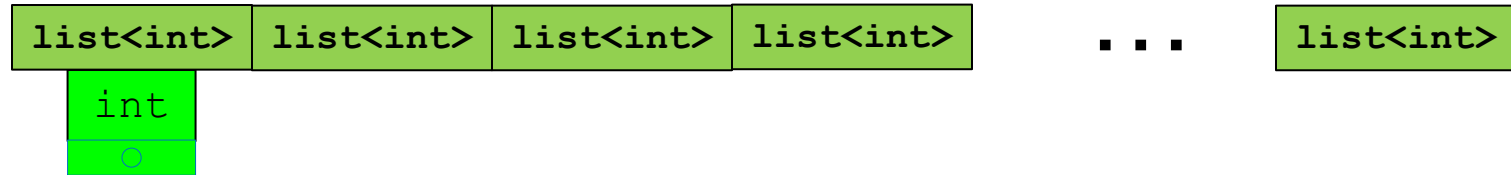
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



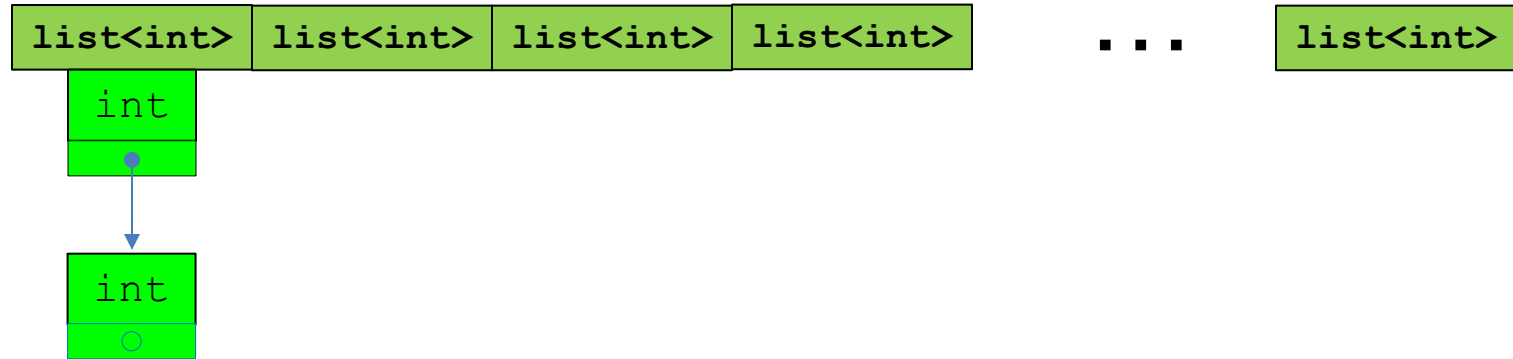
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



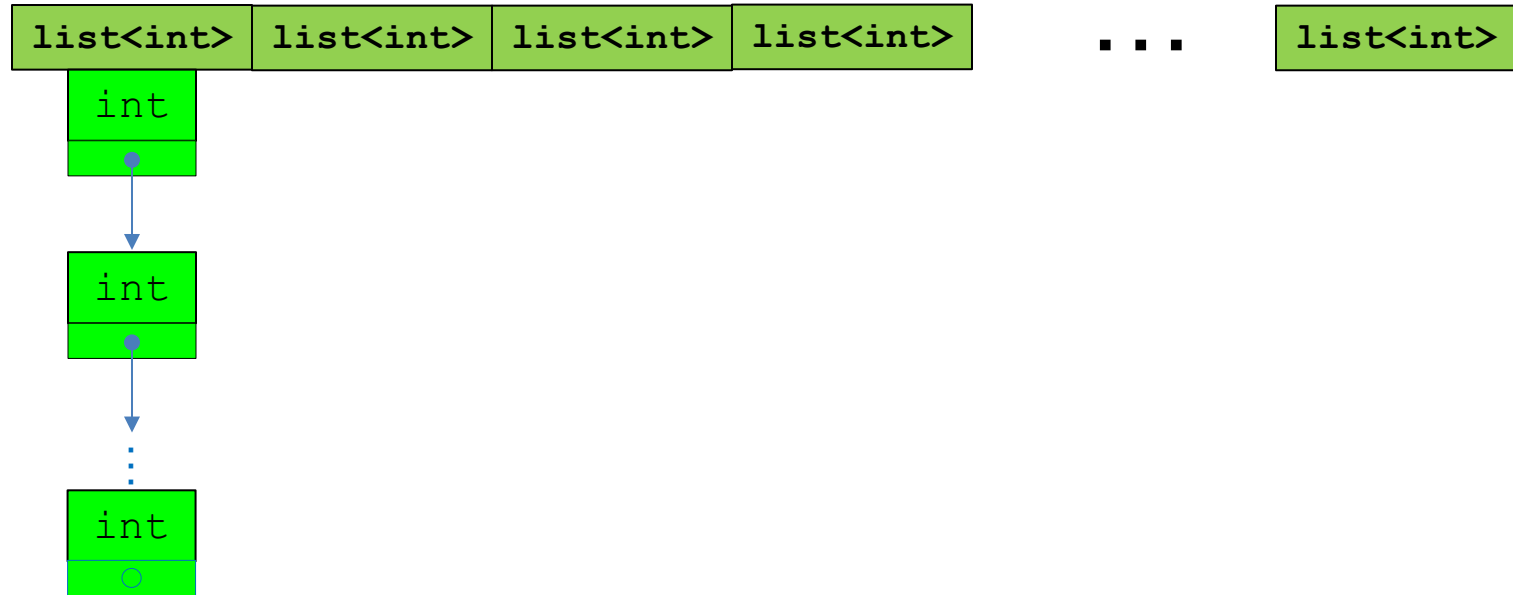
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



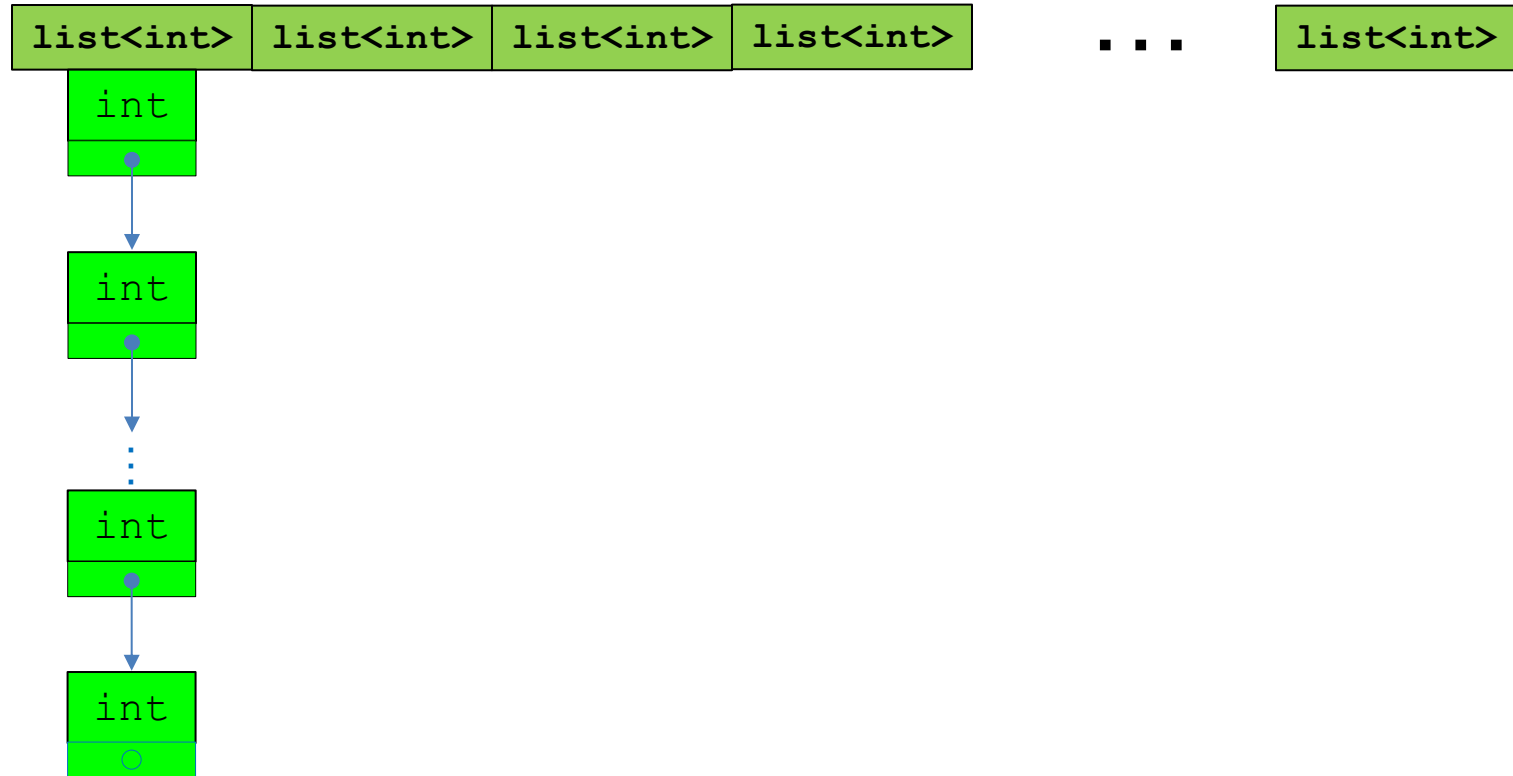
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



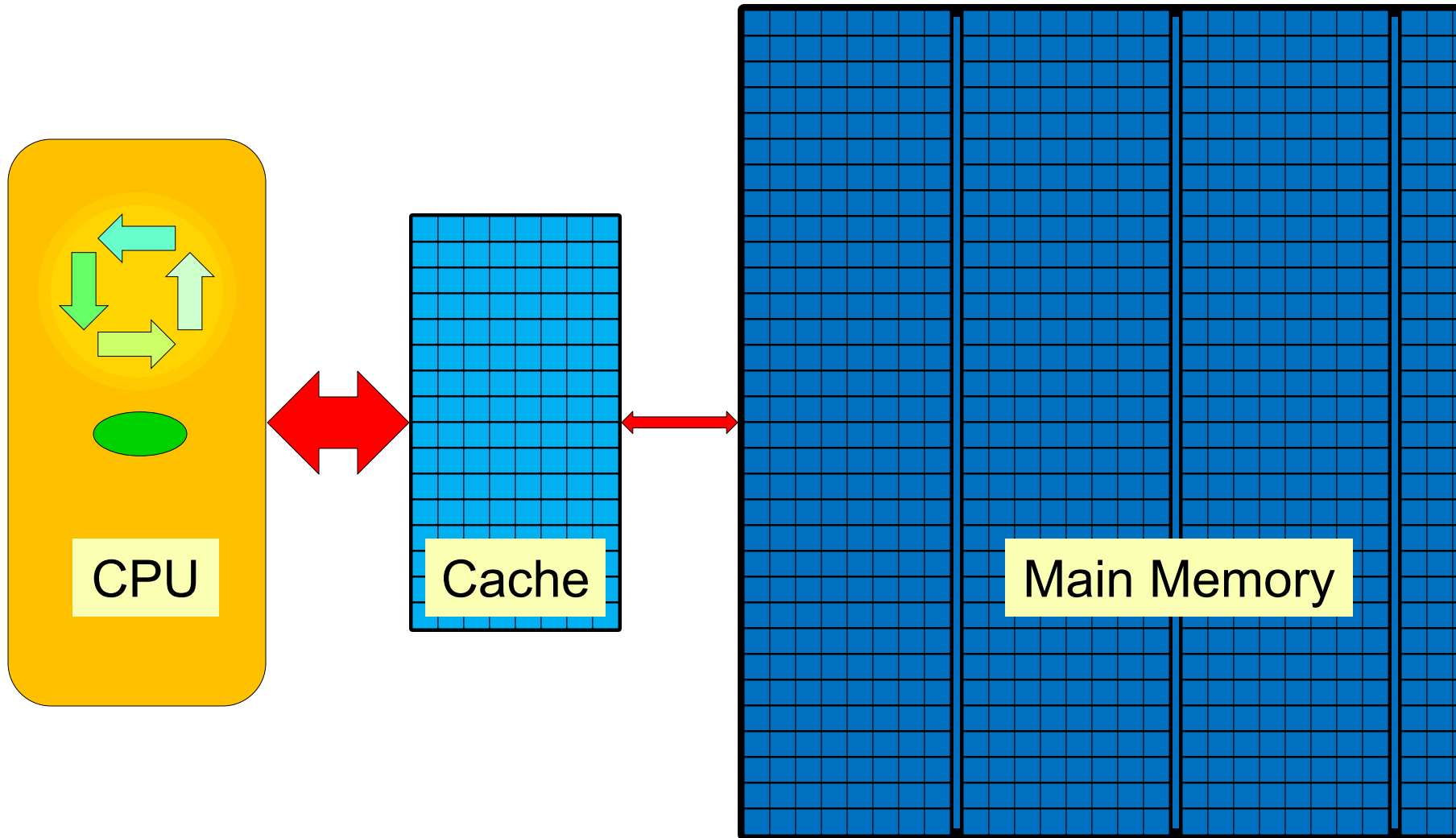
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



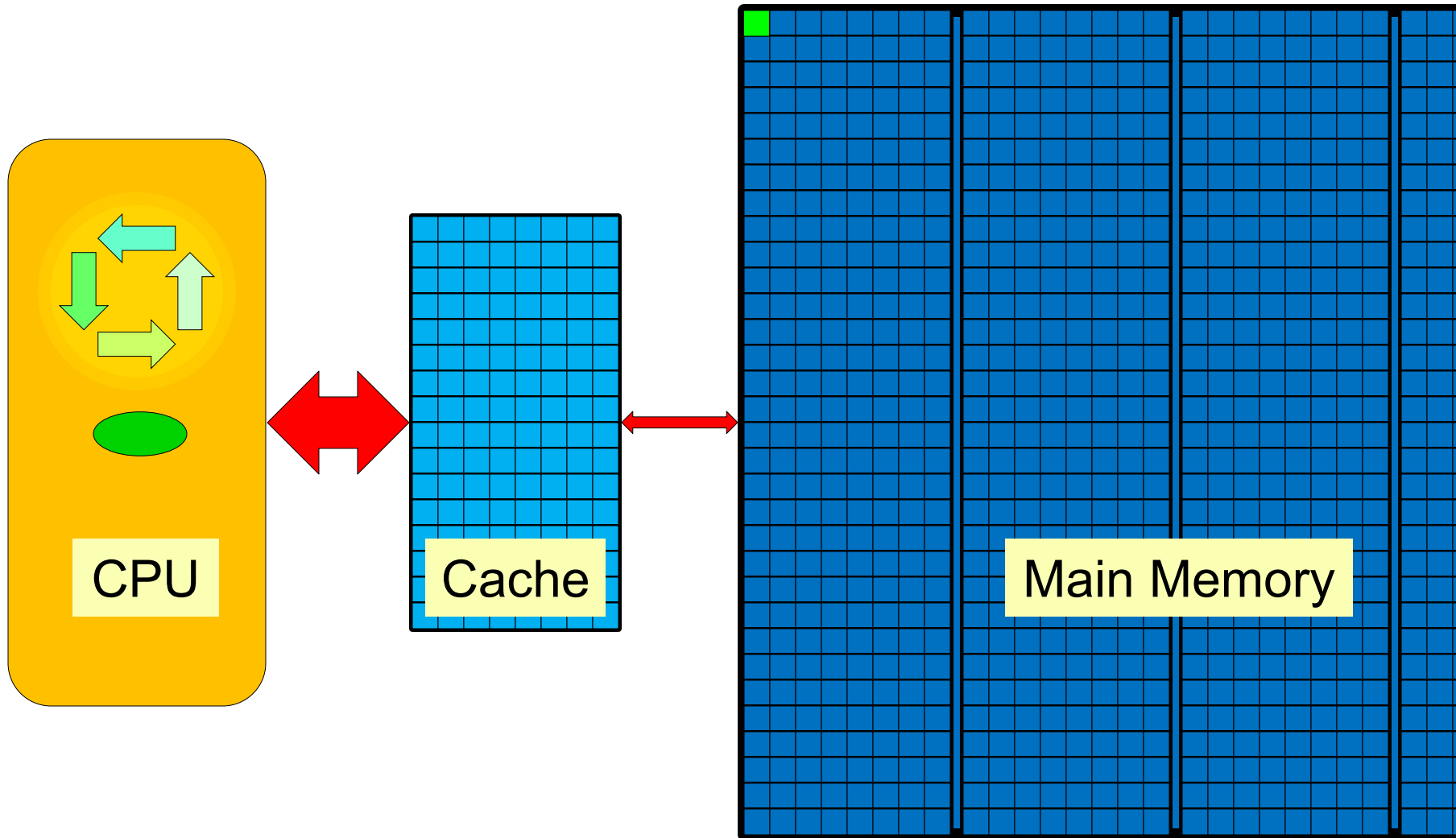
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



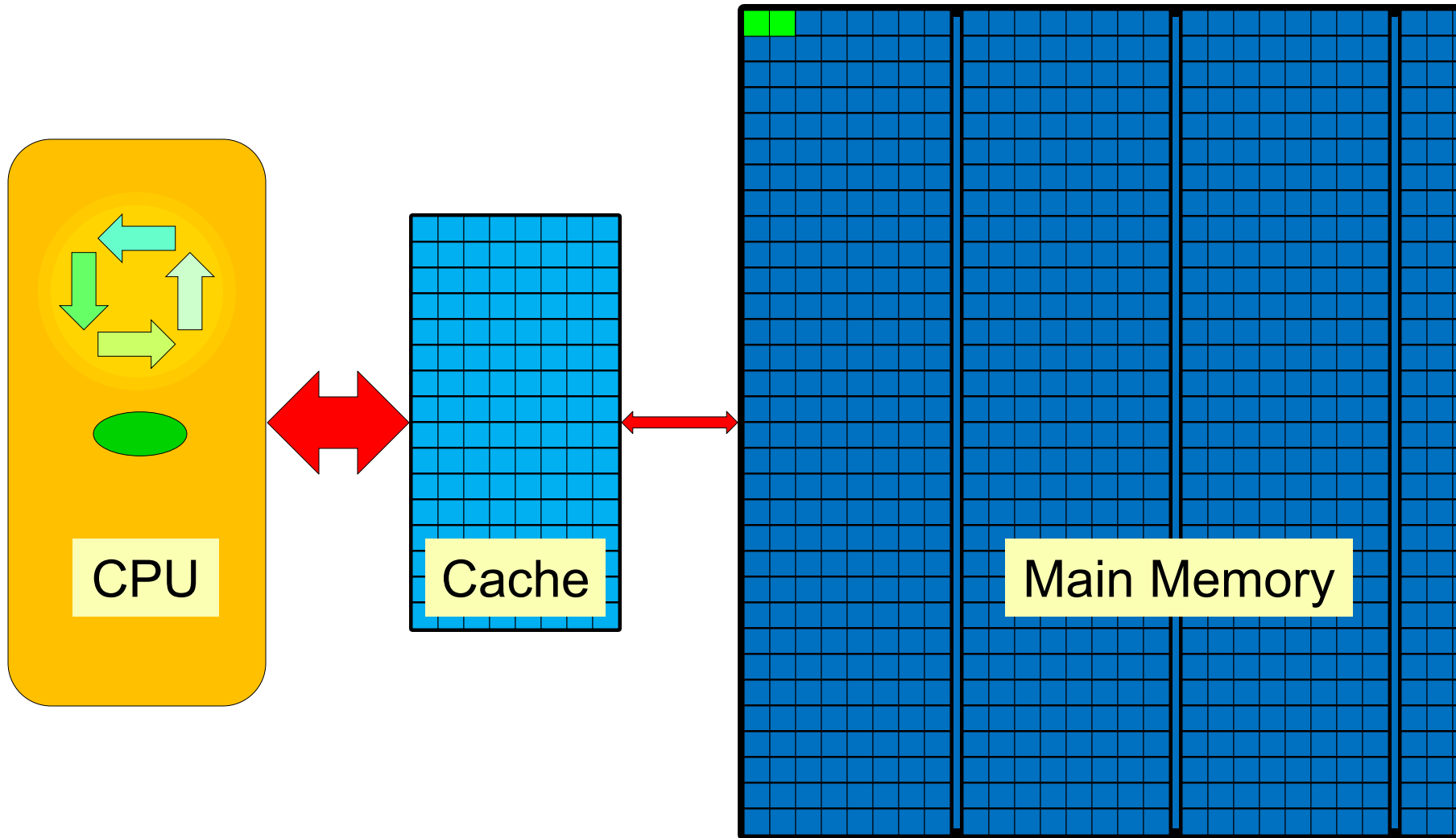
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



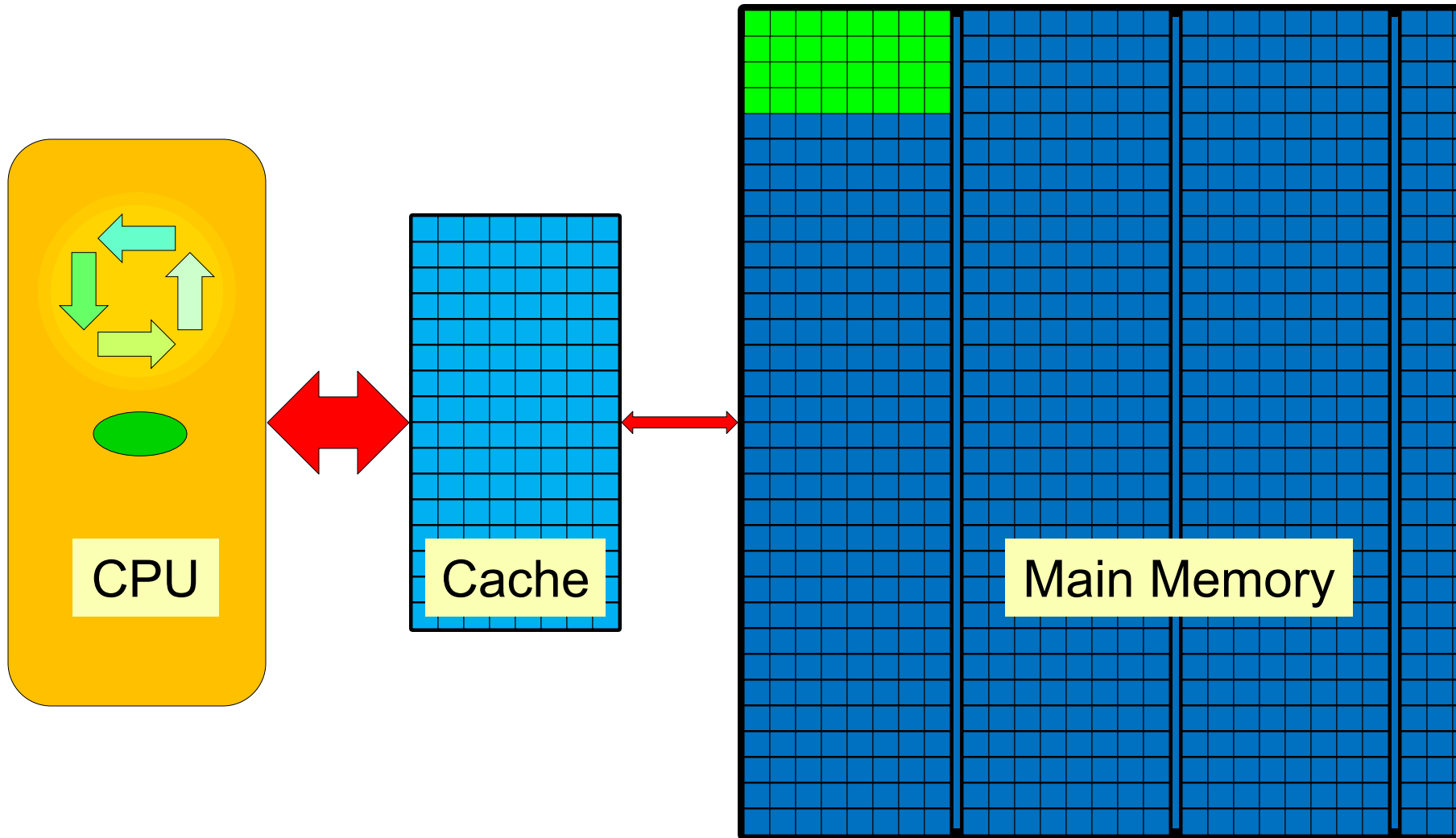
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



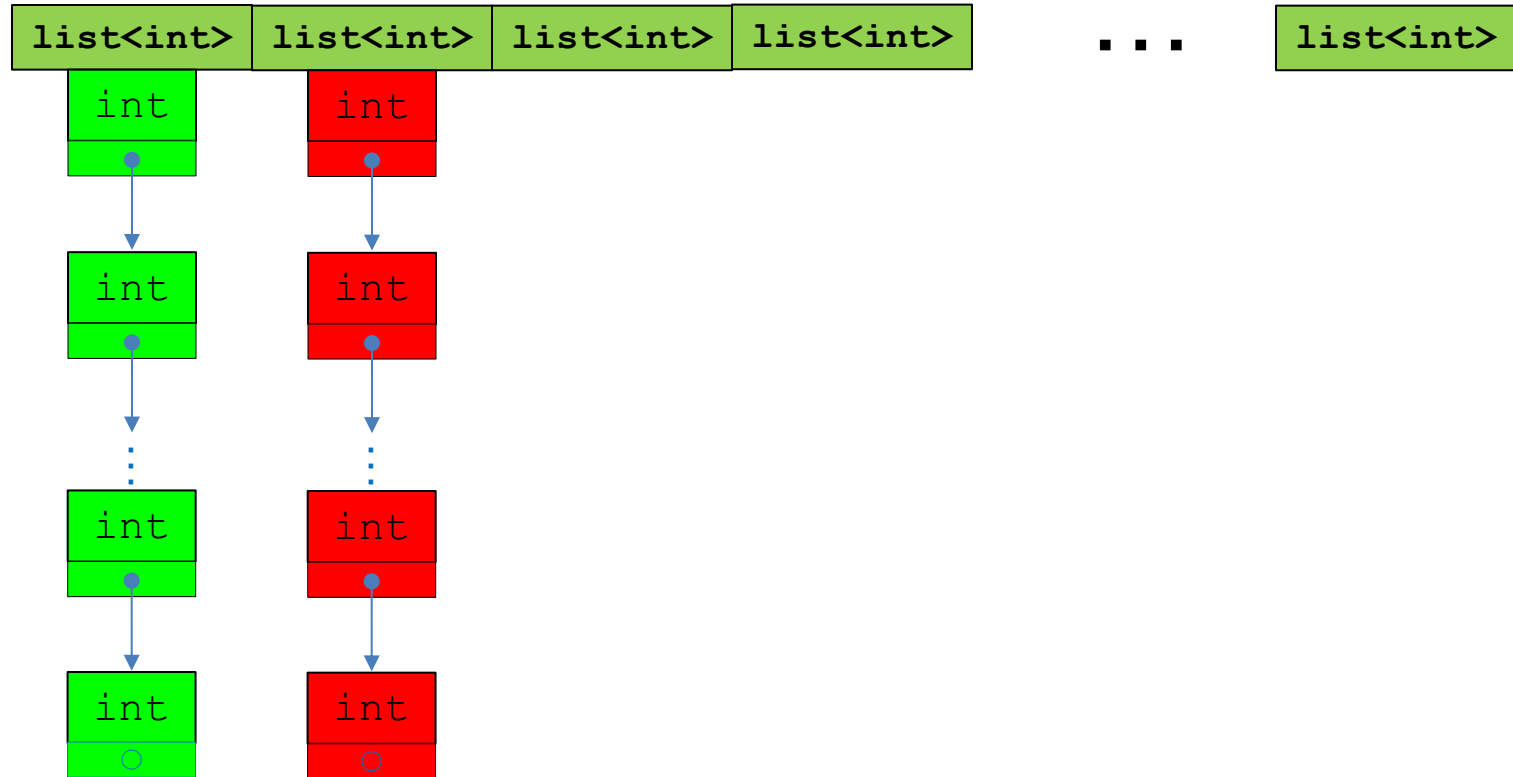
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



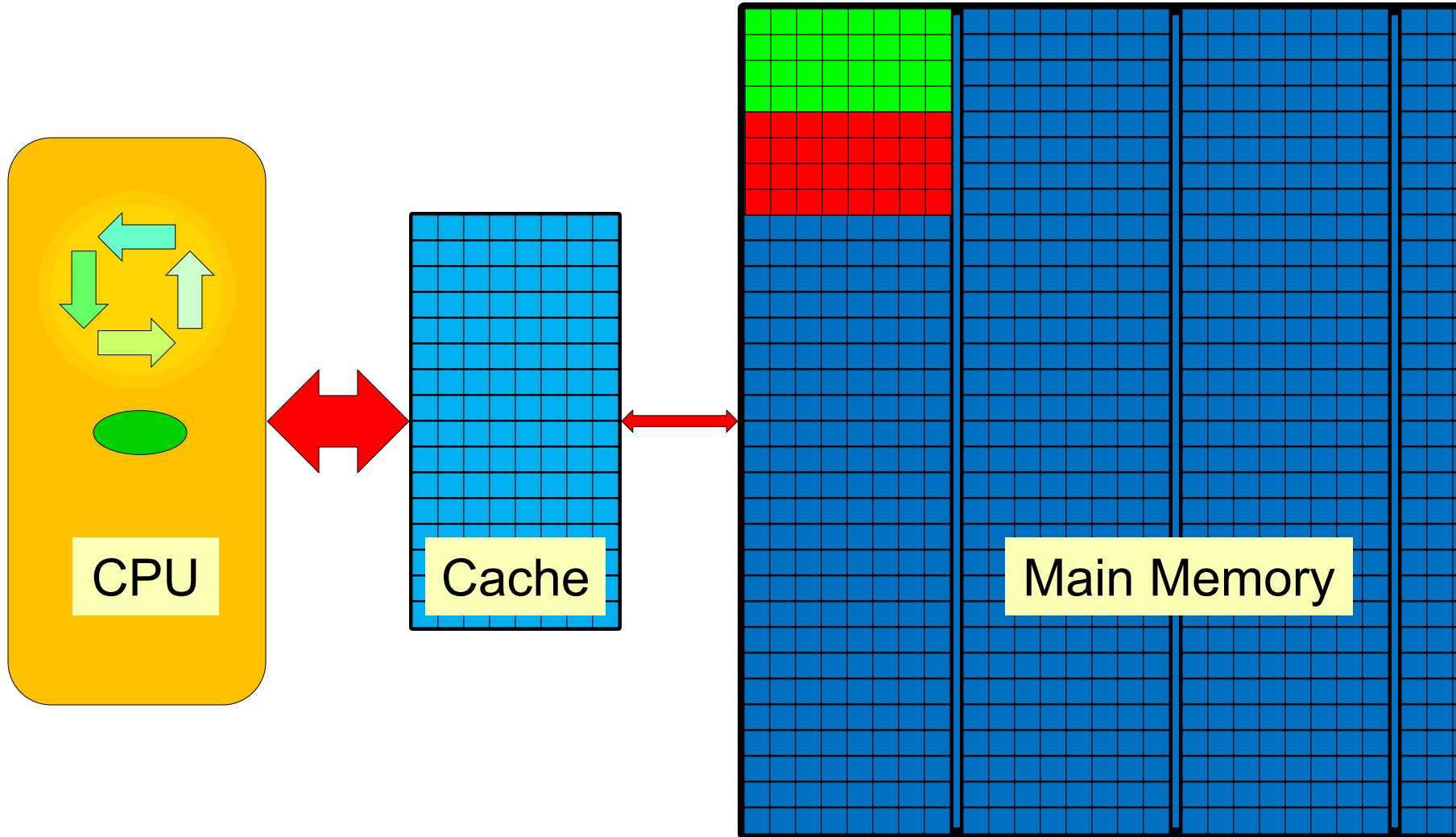
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



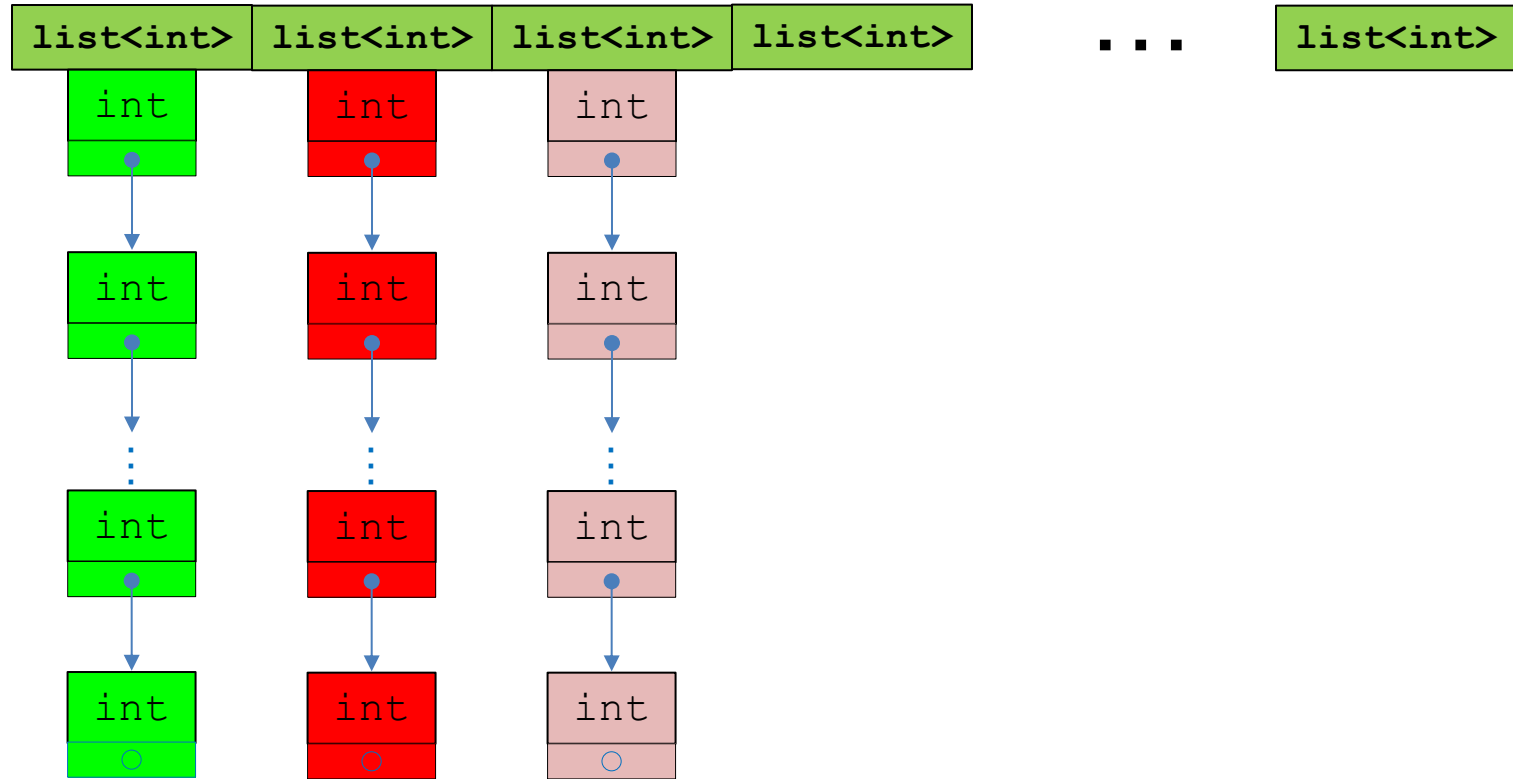
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



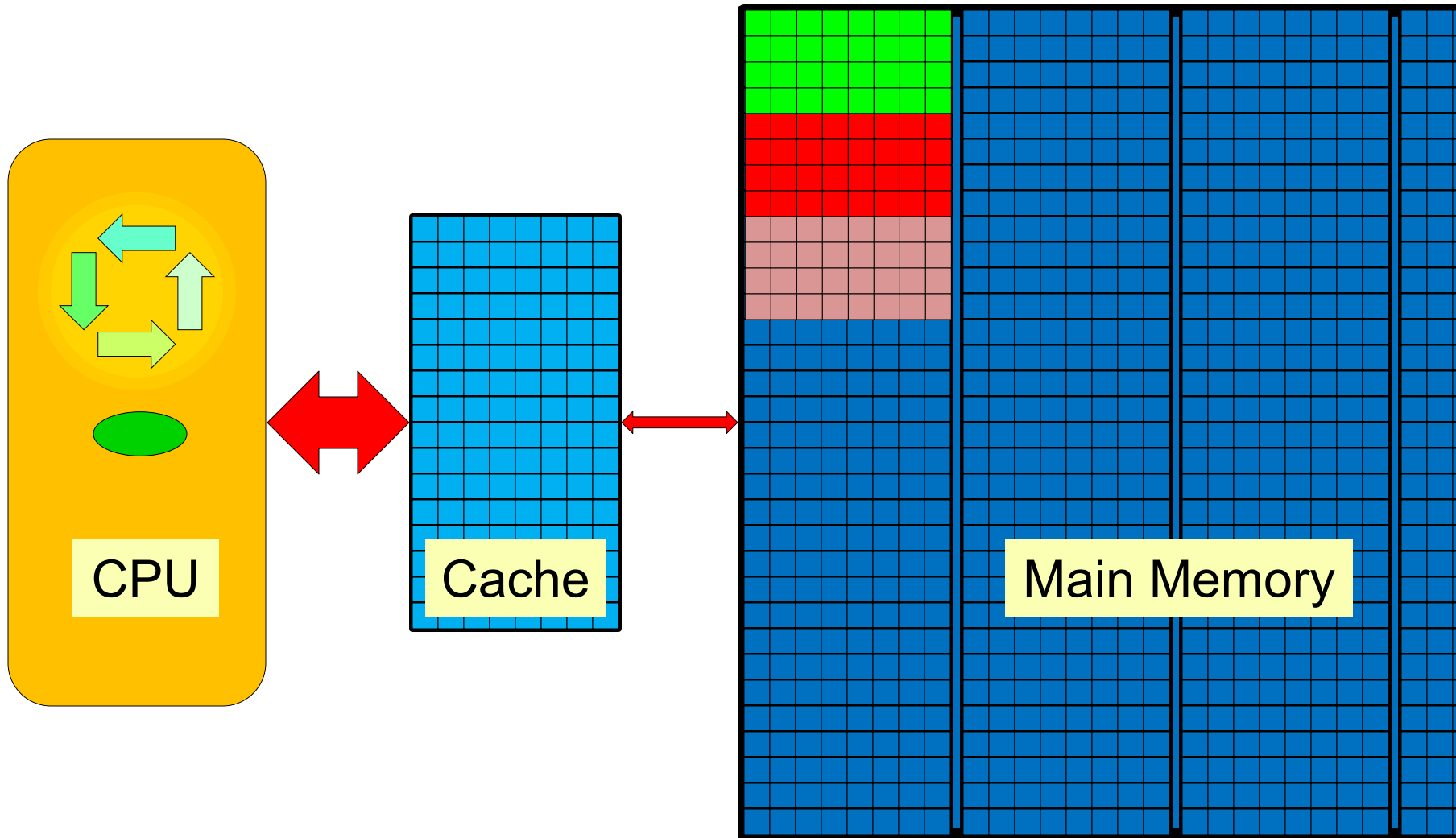
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



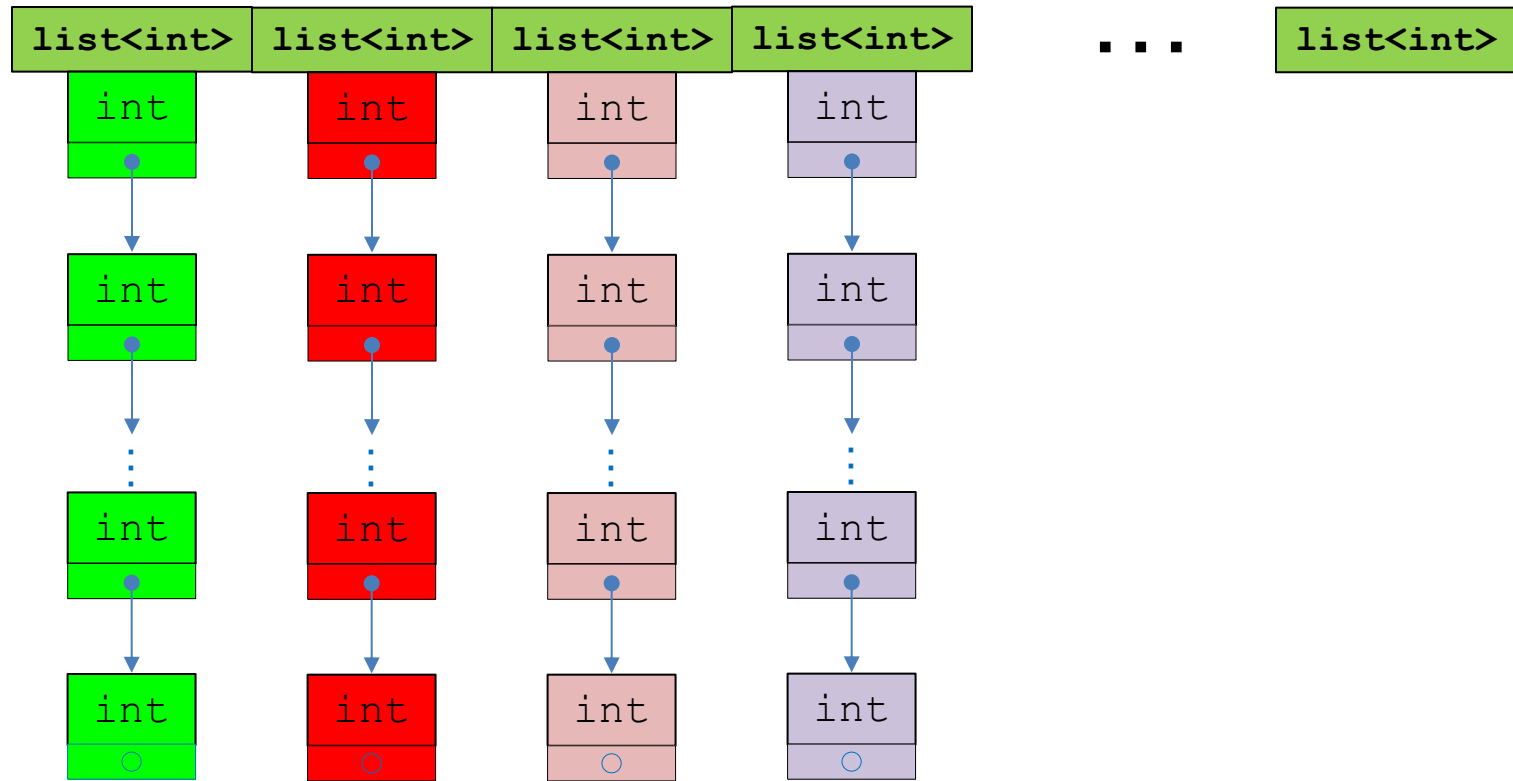
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



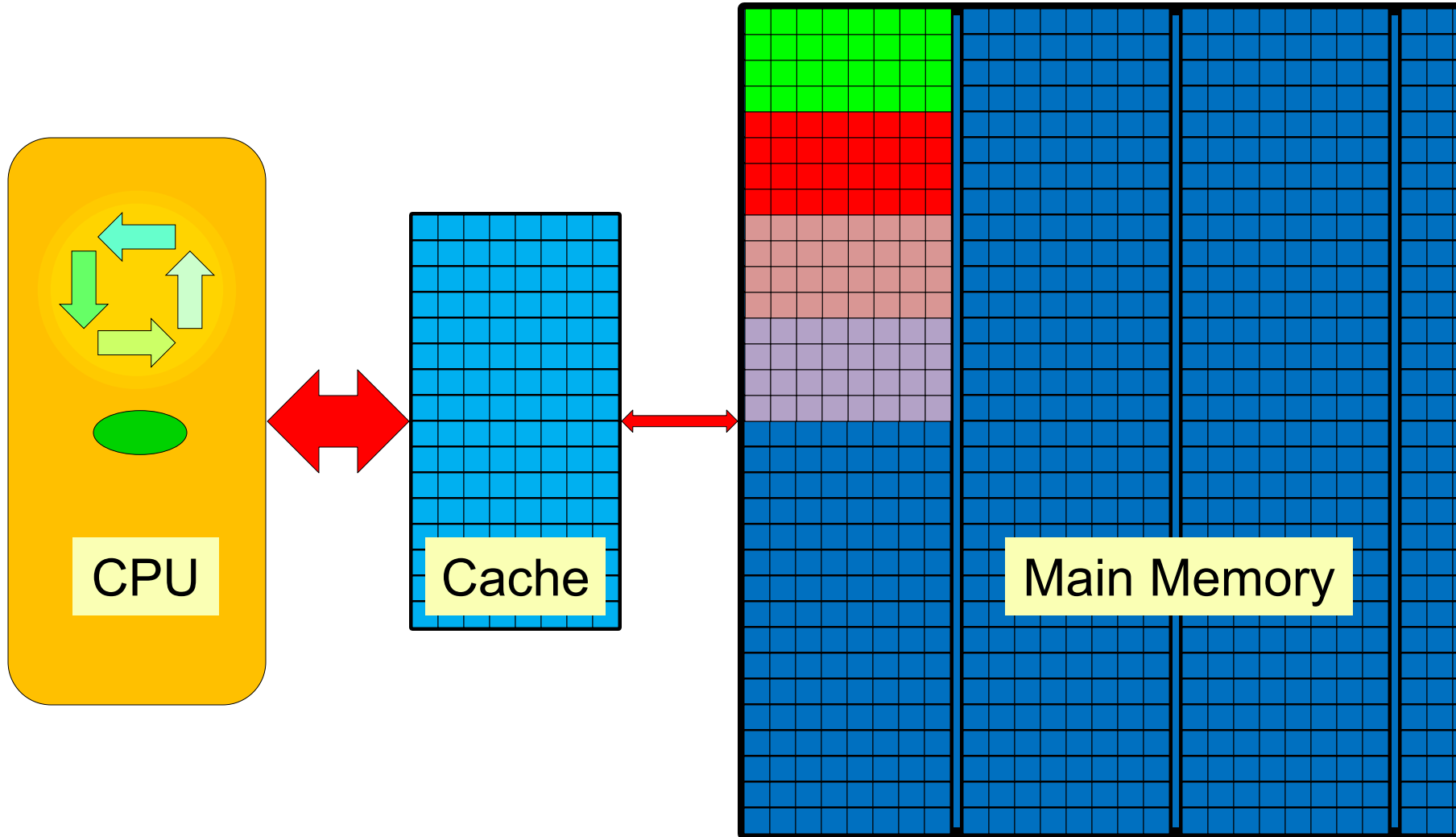
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



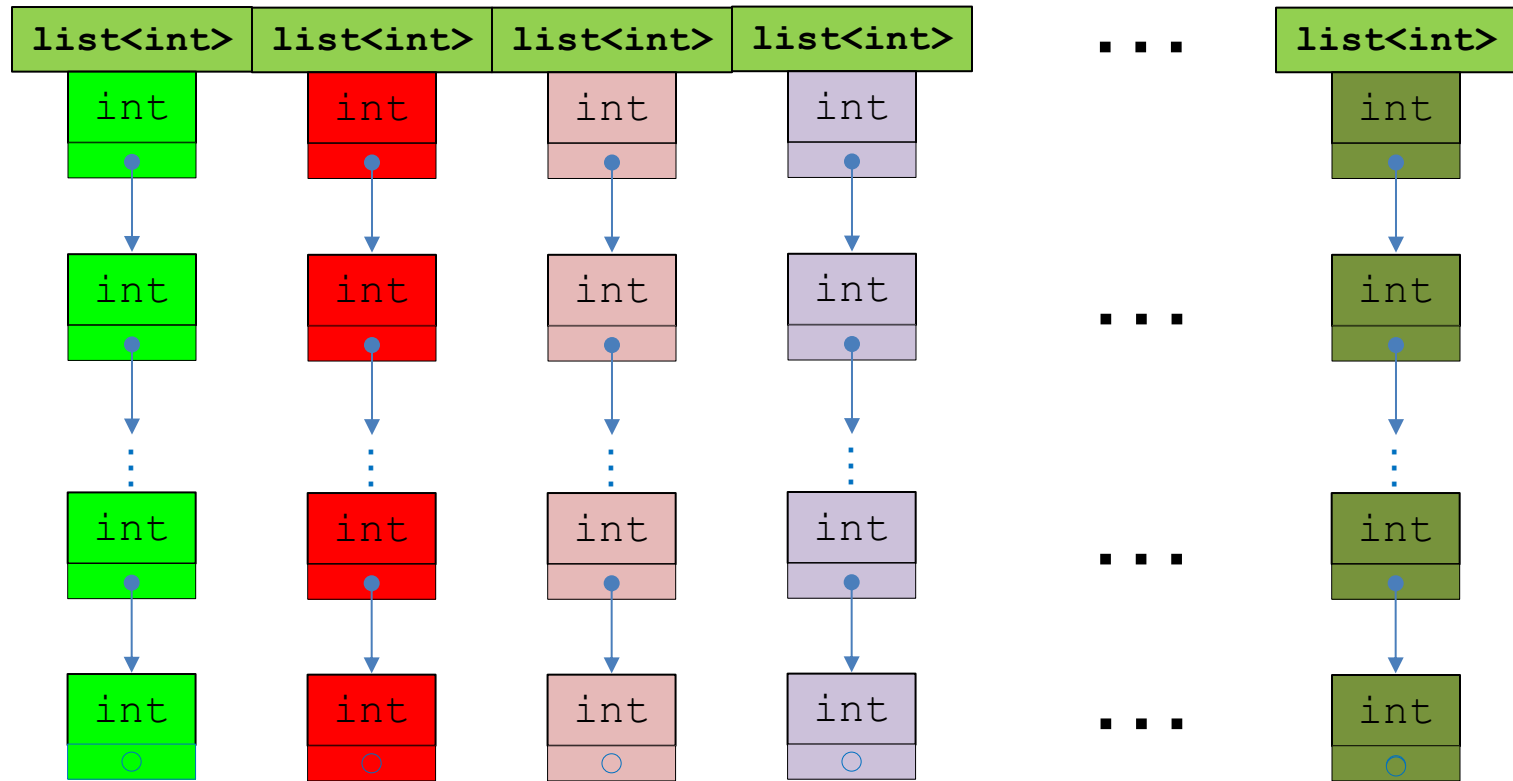
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



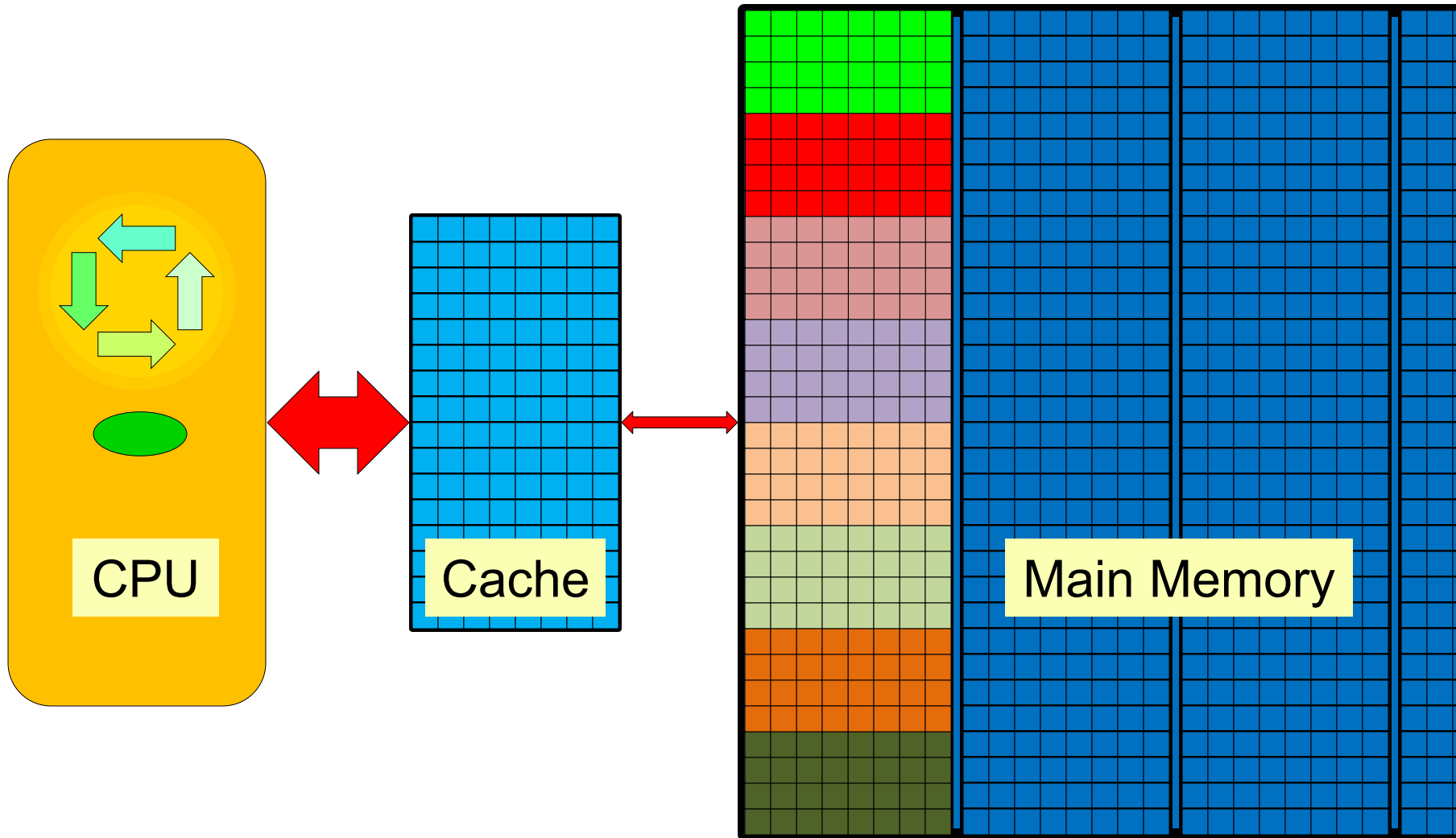
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Access Plan:

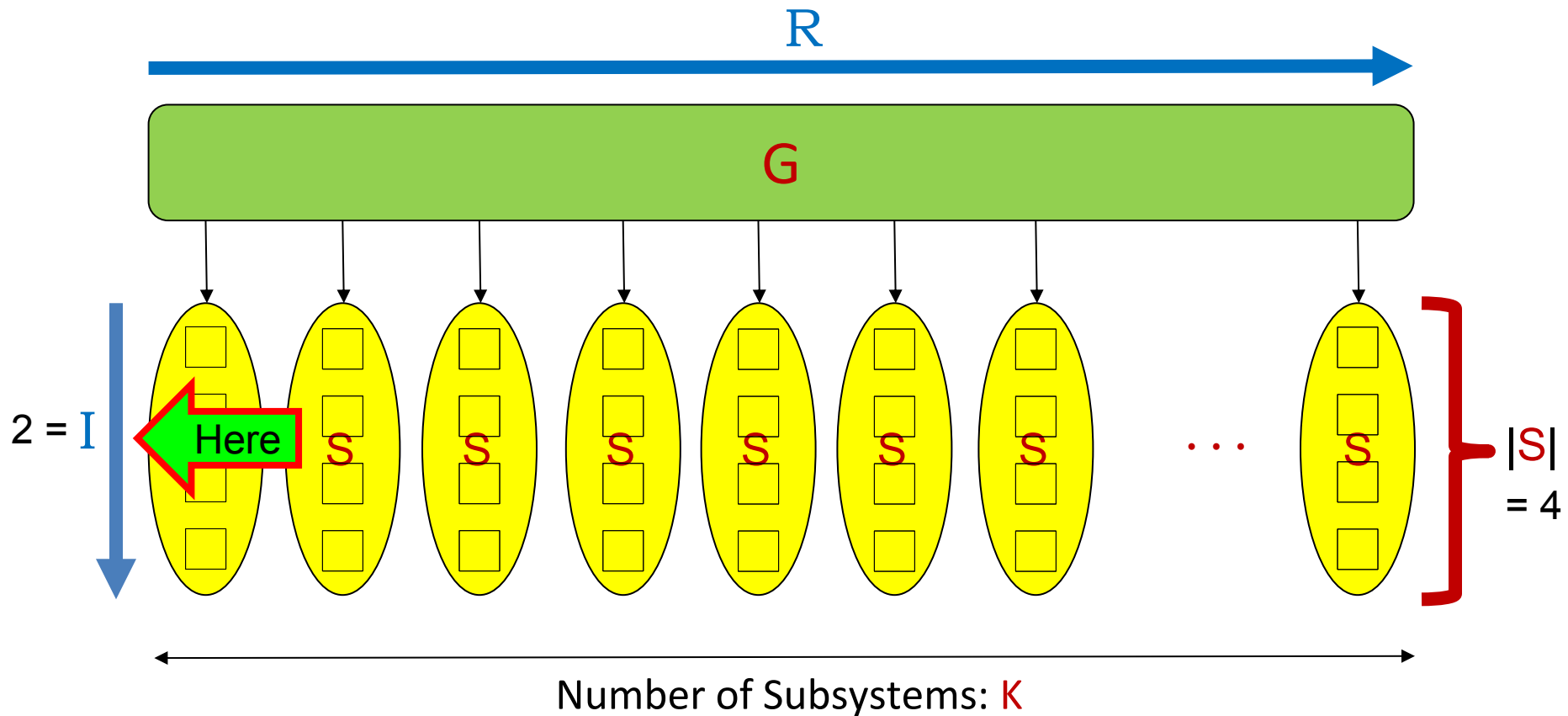
- Visit each of the subsystems \mathbf{S}_j of \mathbf{G} in turn.
 - Traverse \mathbf{S}_j – \mathbf{I} times – before moving to the next.
 - Increment the `int` value of each link of the list in \mathbf{S}_j
 - Repeat (until the problem size \mathbf{N} is reached).
 - We chose the overall problem size $\mathbf{N} \gg 2^{30}$ (very c large).
- The result of this experiment is its (wall) **RUNTIME**.
 - No memory is allocated or deallocated.

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

$$\text{Problem Size: } \mathbf{N} = |\mathbf{G}| \cdot \mathbf{I} \cdot \mathbf{R}$$

$$\text{Physical System Size } |\mathbf{G}| = \mathbf{K} \cdot |\mathbf{S}|$$

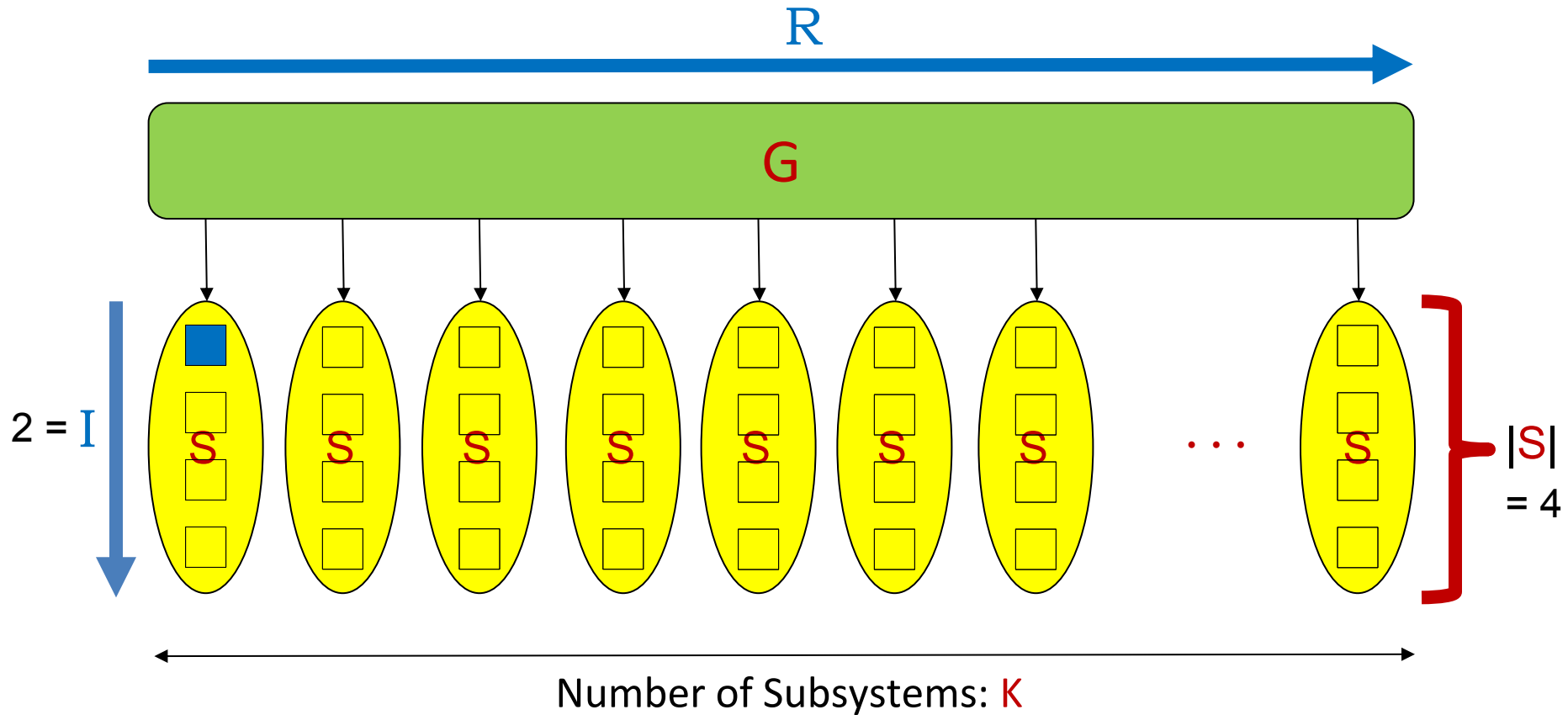


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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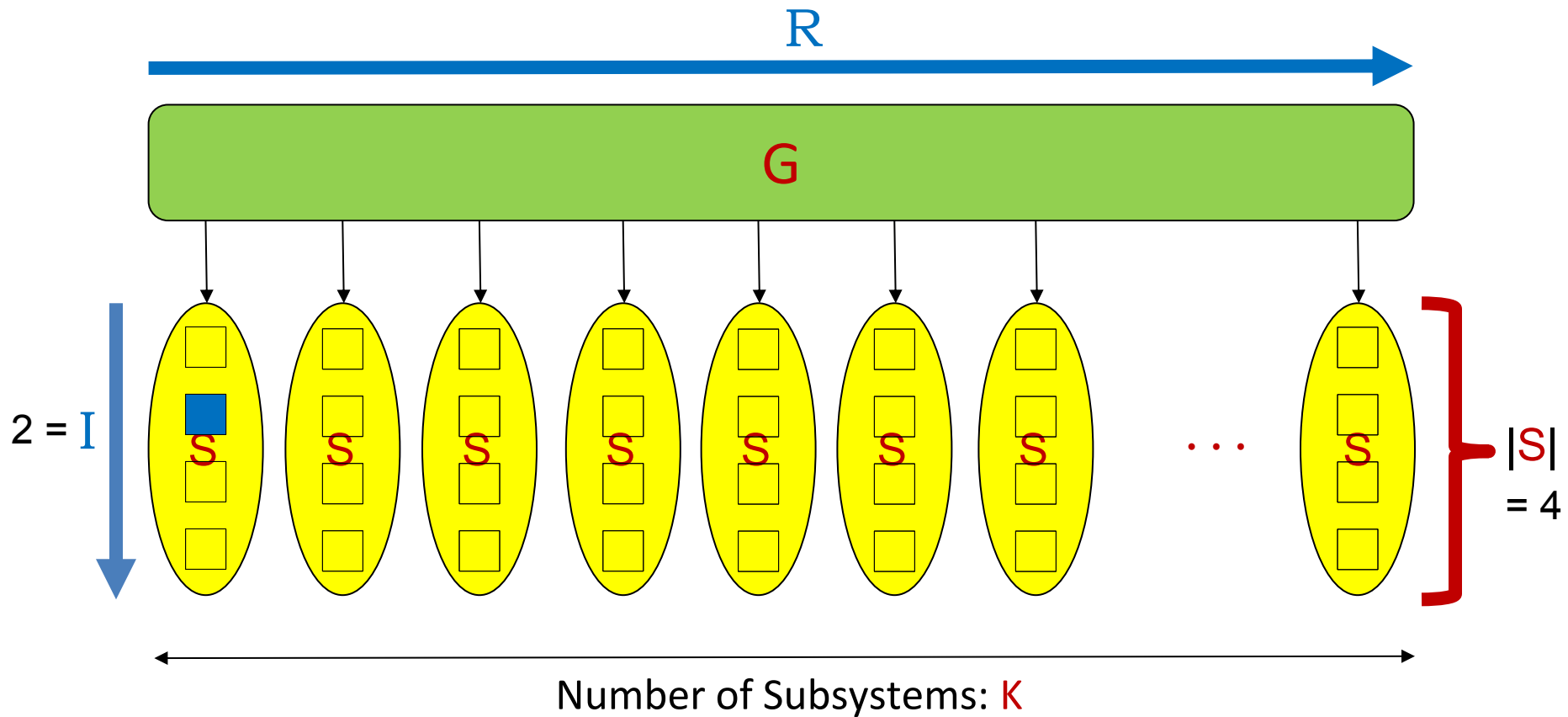


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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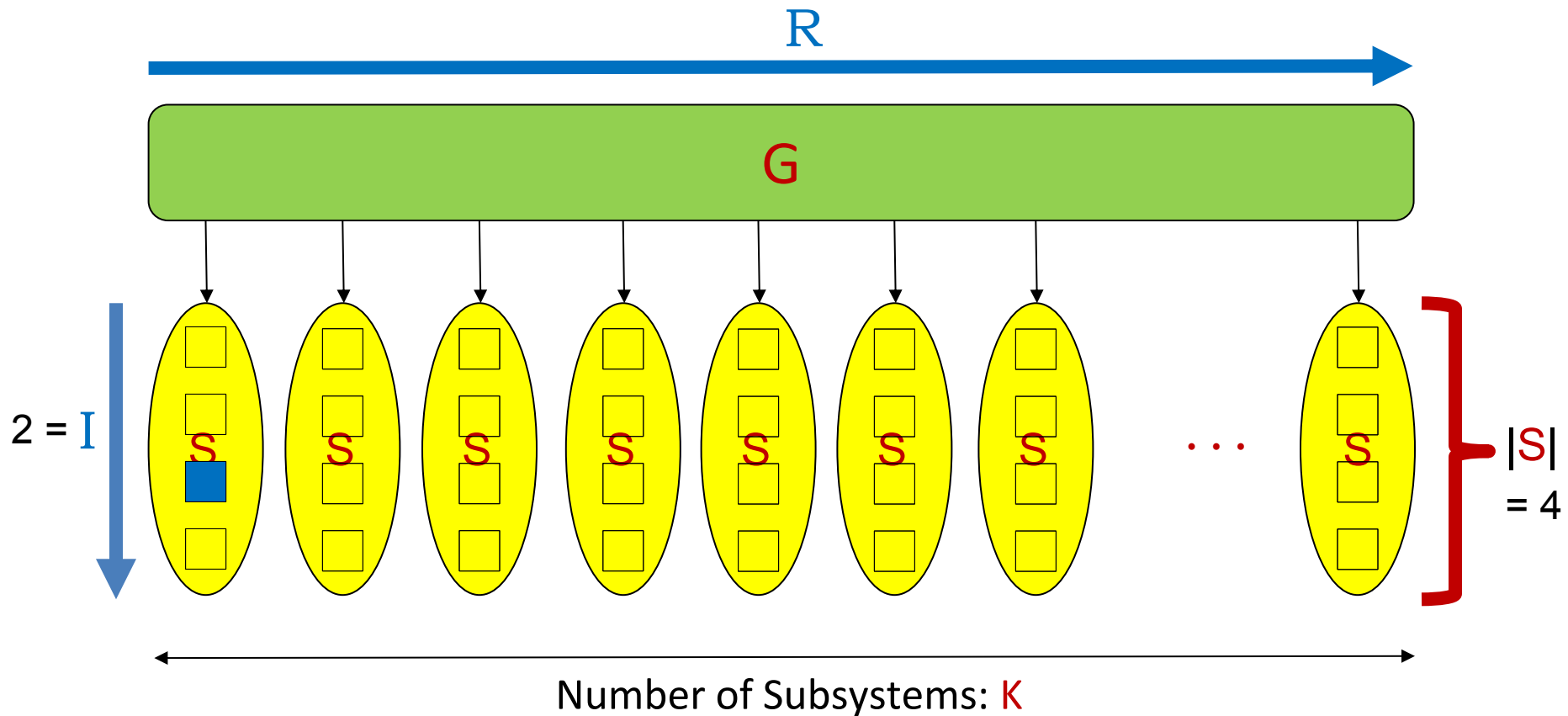


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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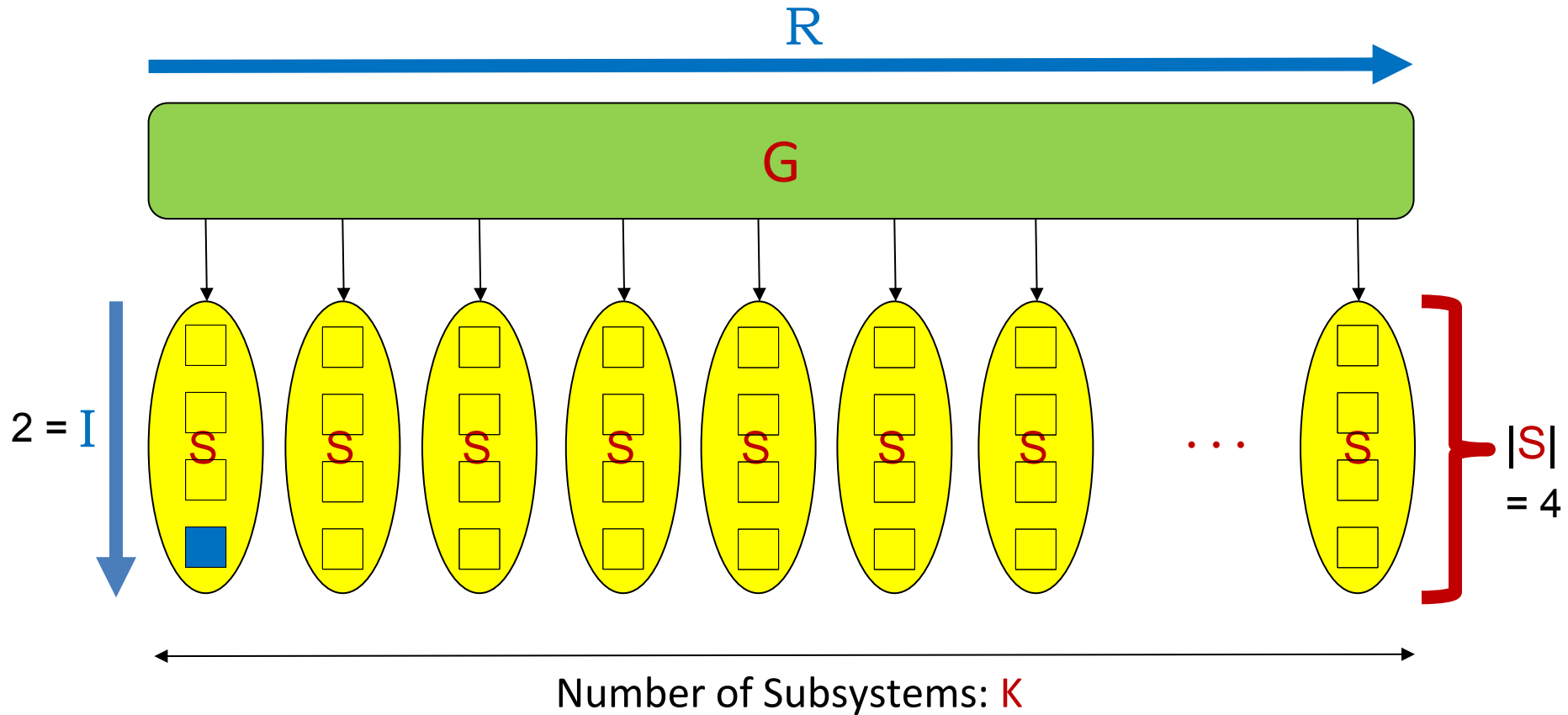


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Benchmark II: LOCALITY

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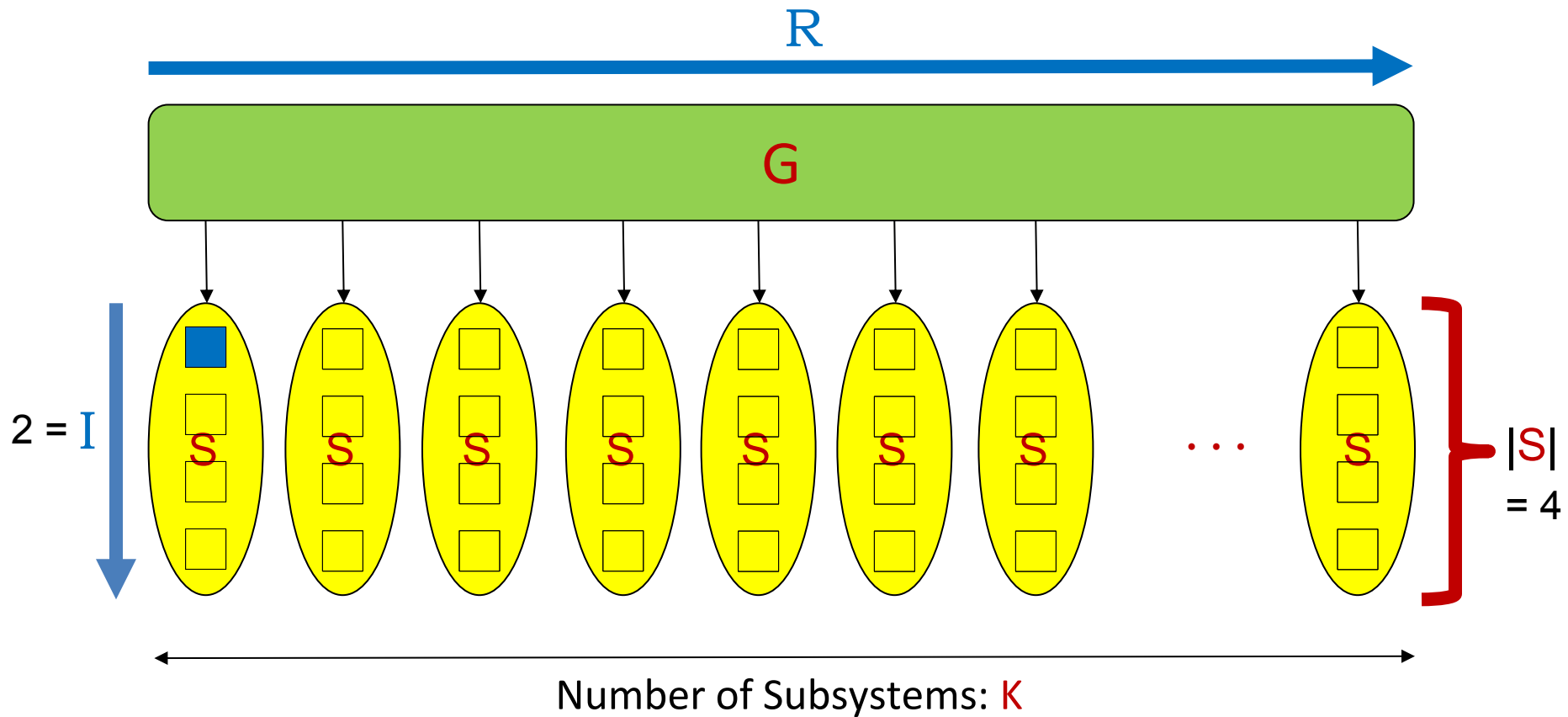


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Benchmark II: LOCALITY

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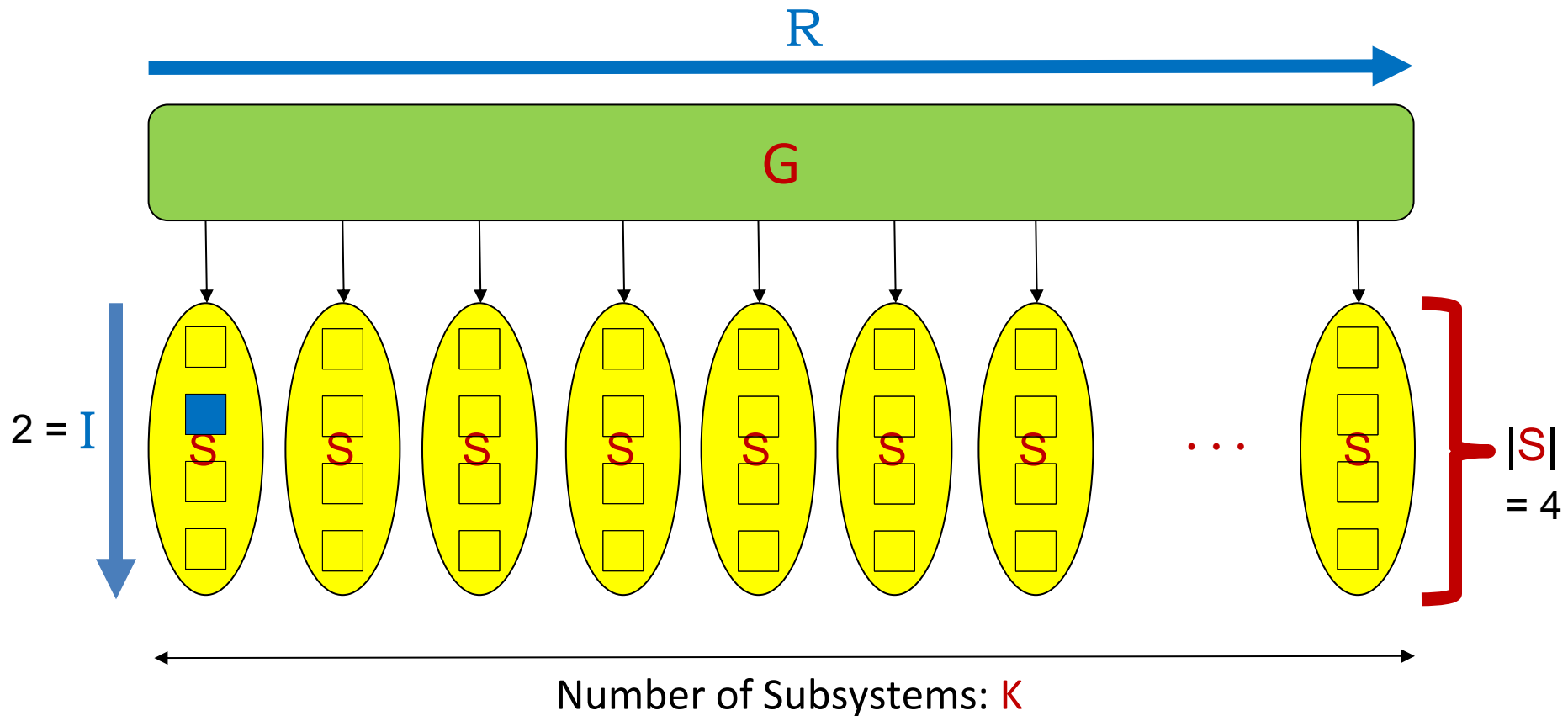


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Benchmark II: LOCALITY

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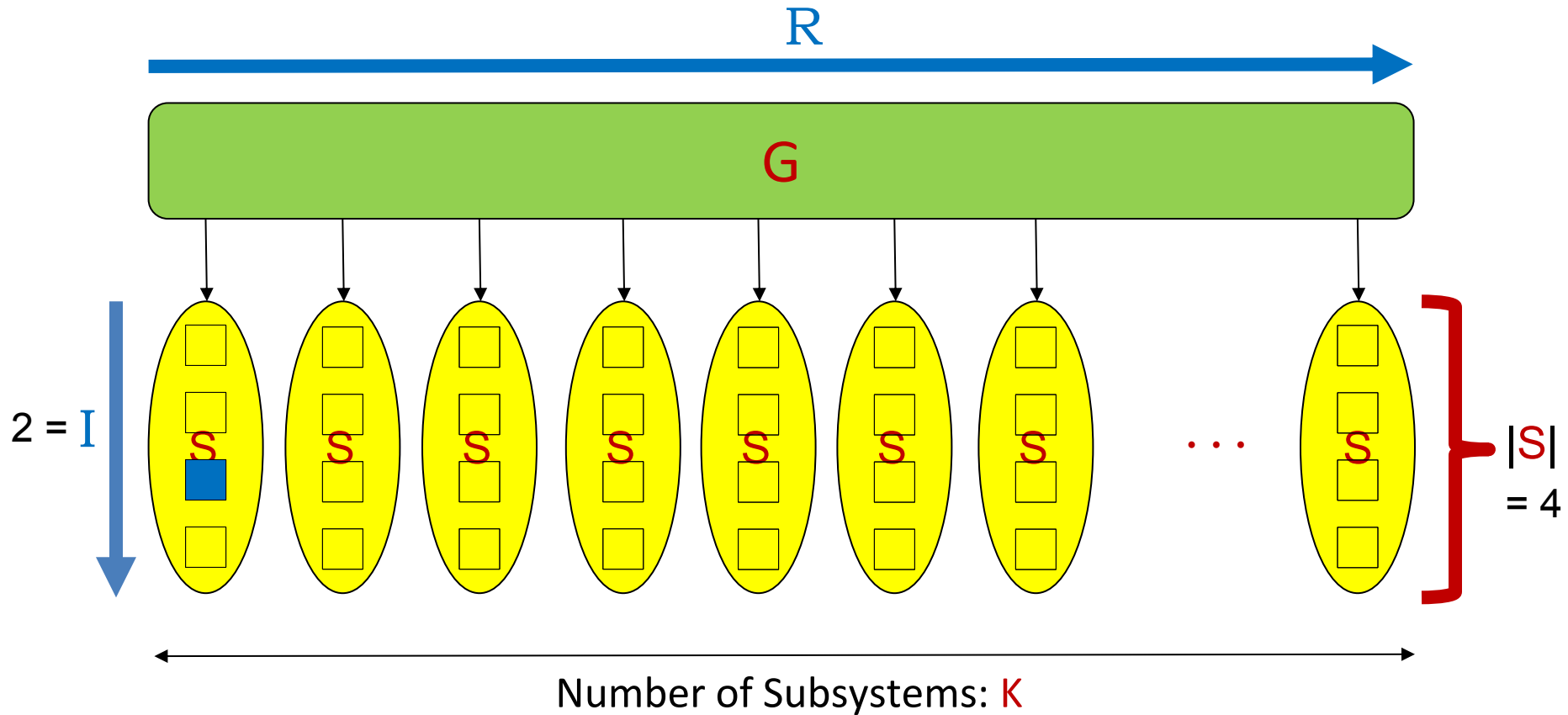


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Benchmark II: LOCALITY

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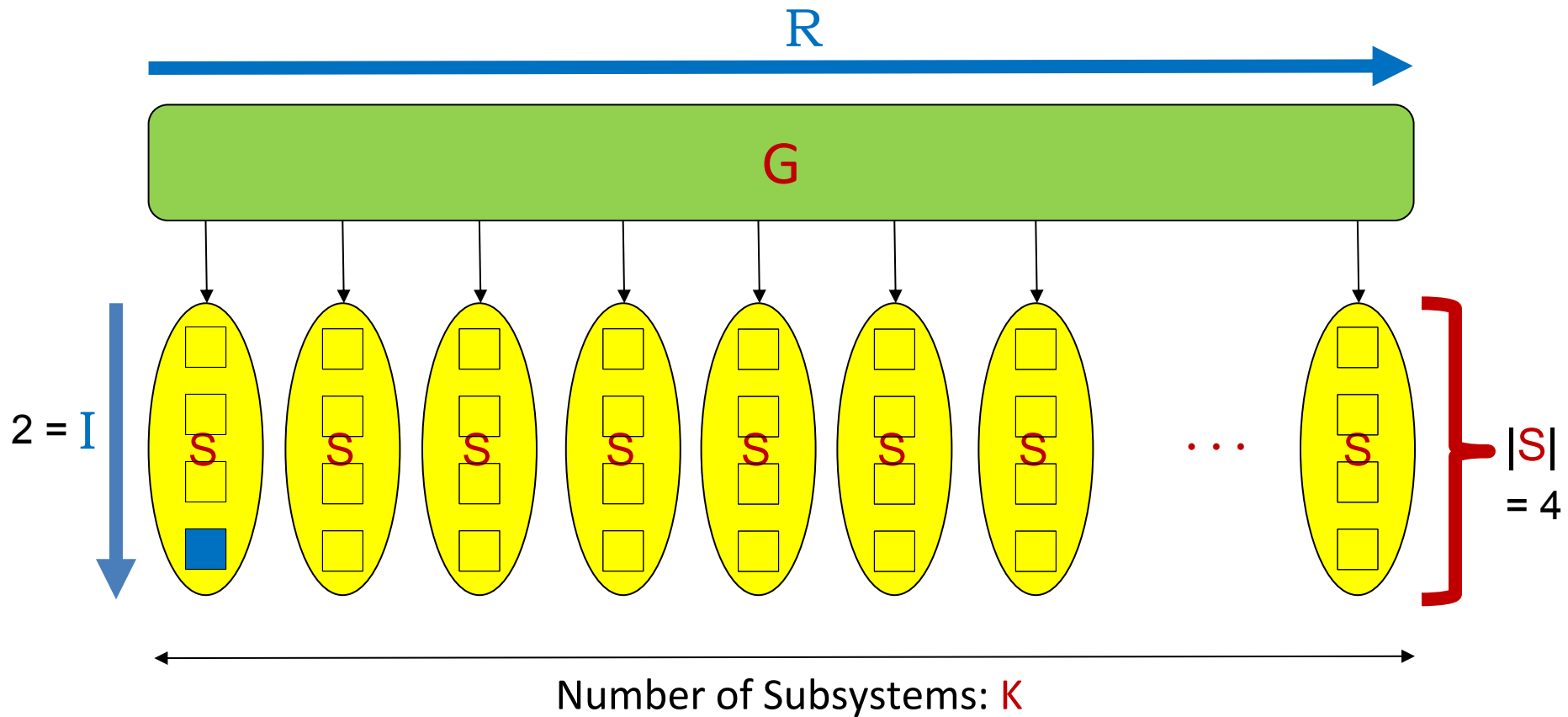


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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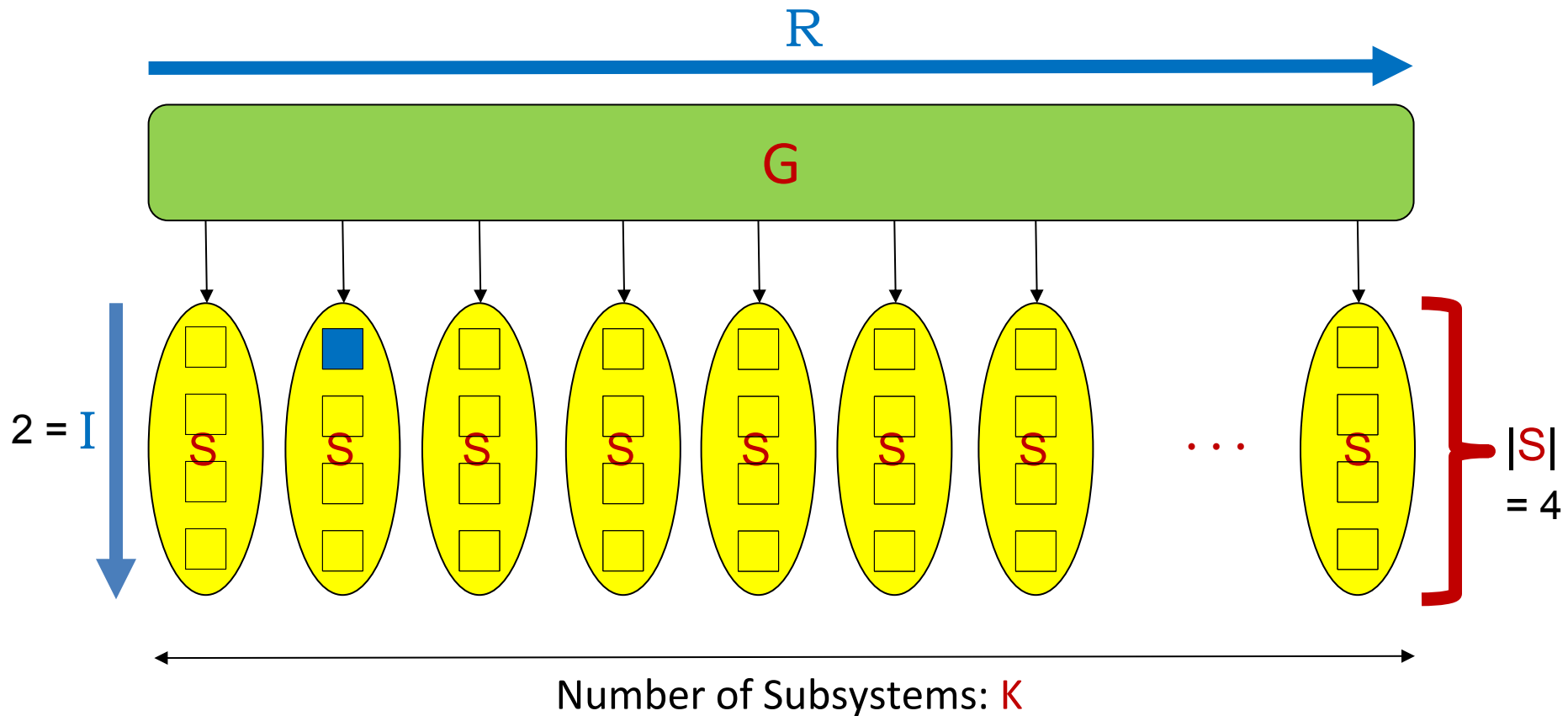


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Benchmark II: LOCALITY

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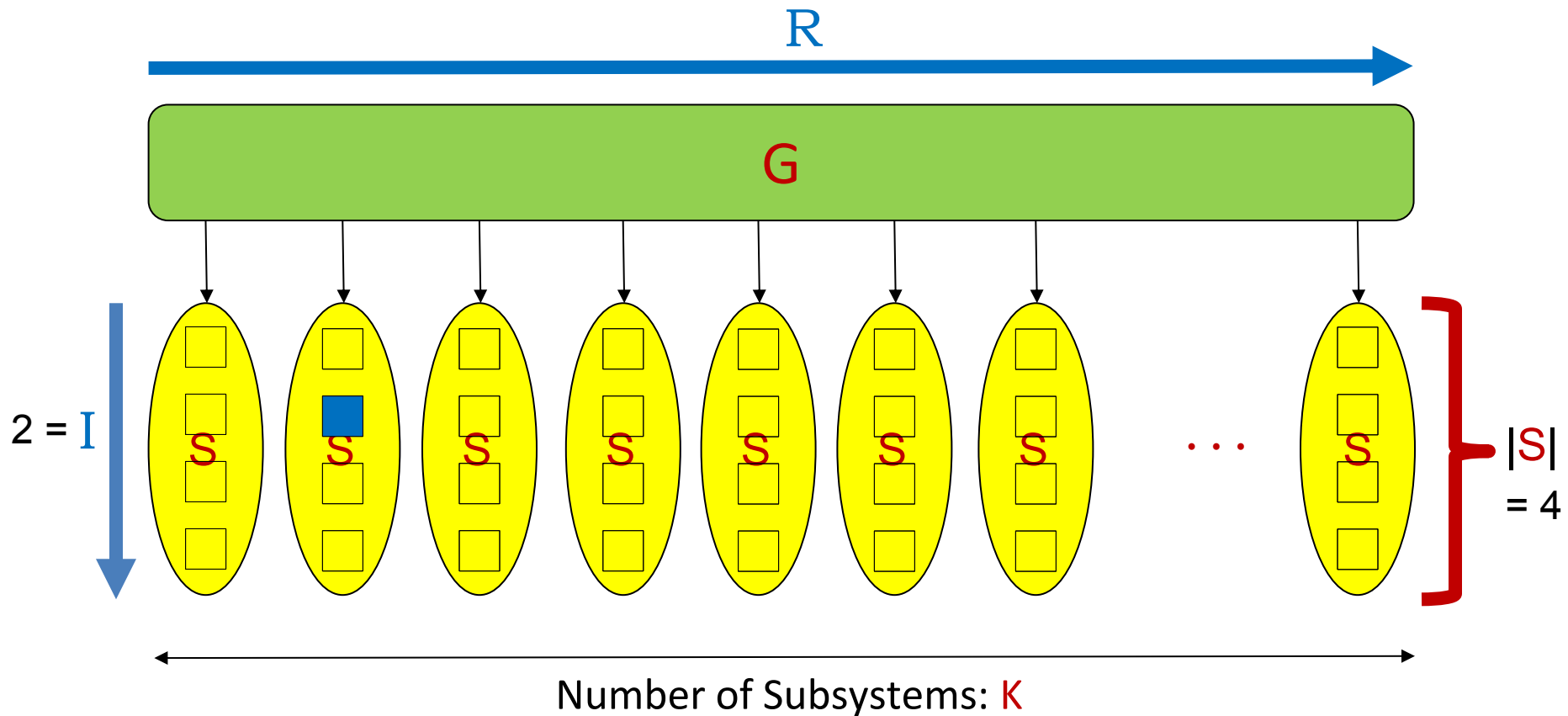


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Benchmark II: LOCALITY

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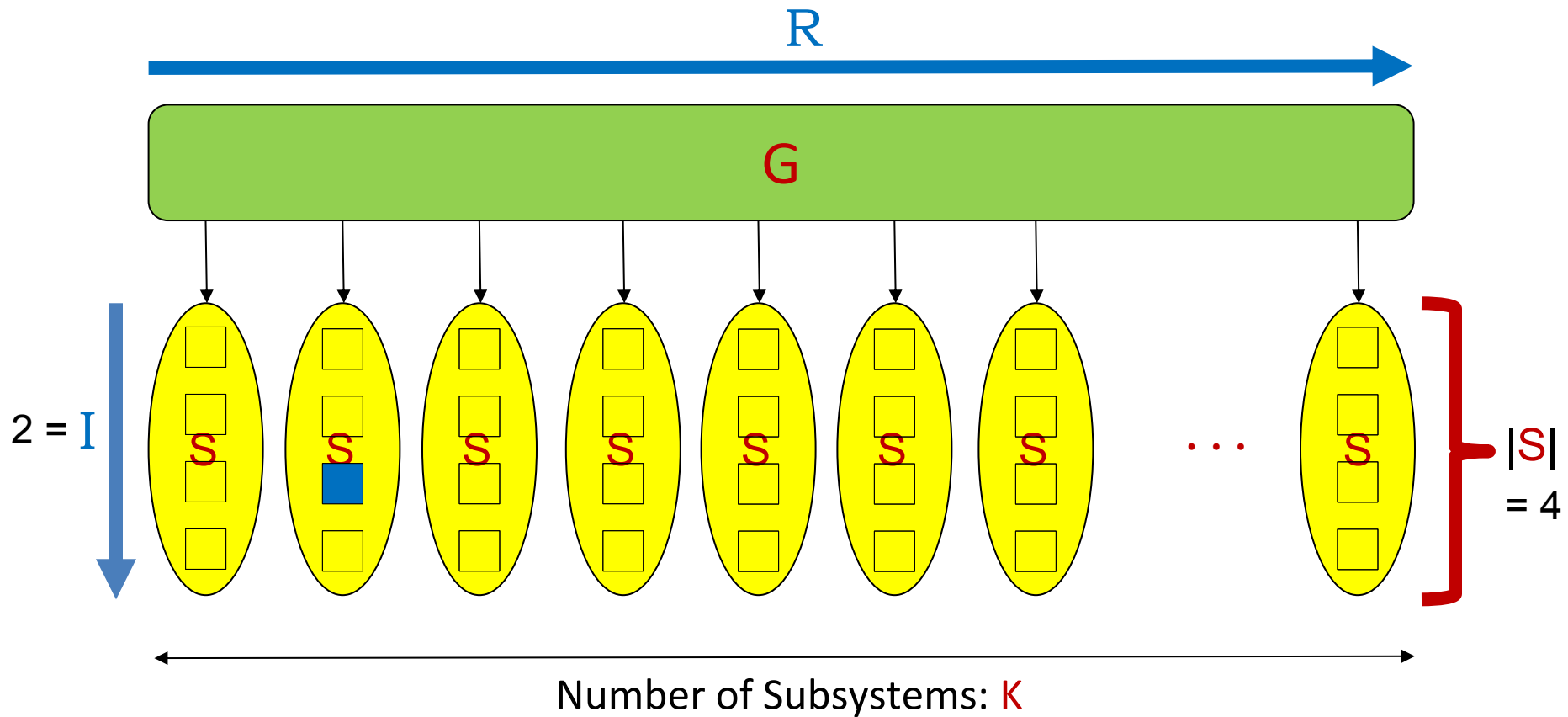


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Benchmark II: LOCALITY

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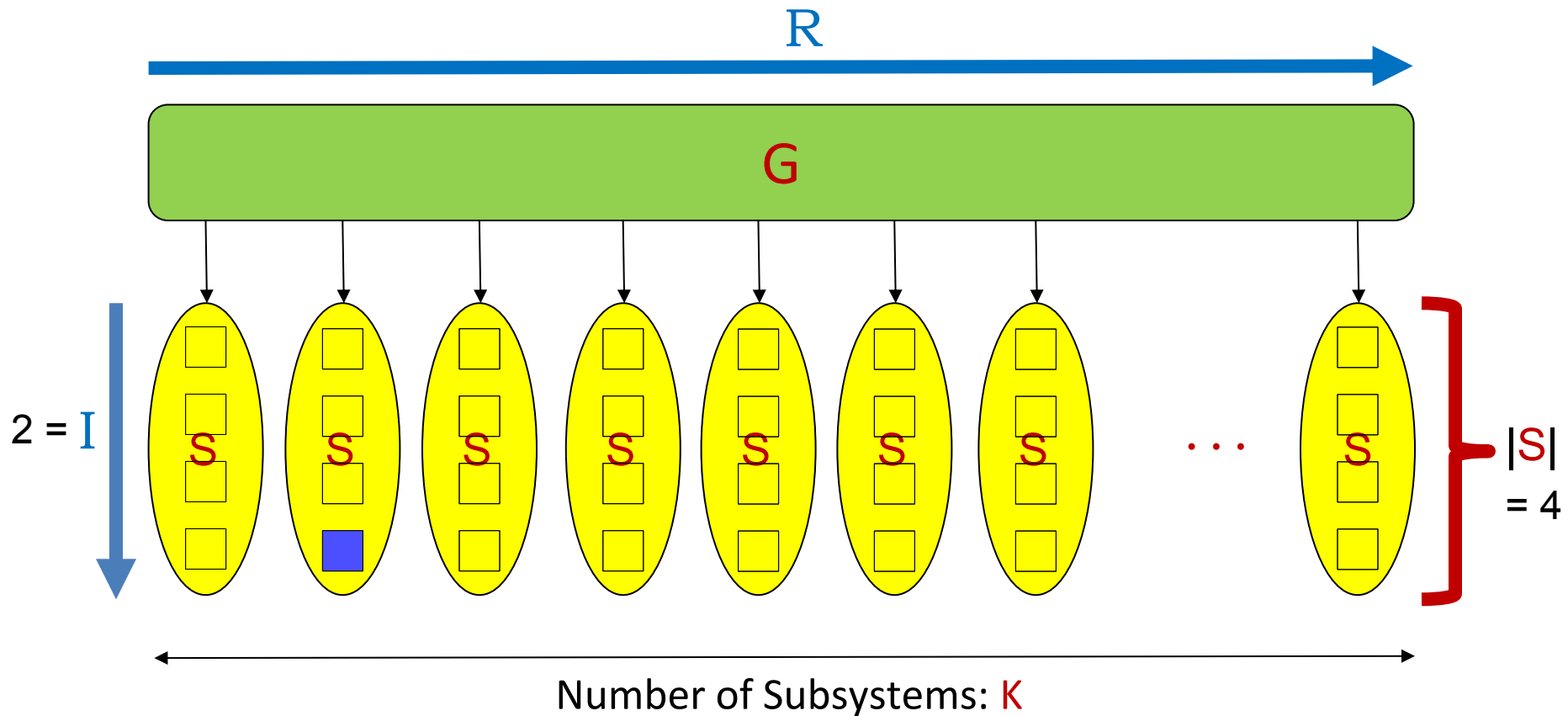


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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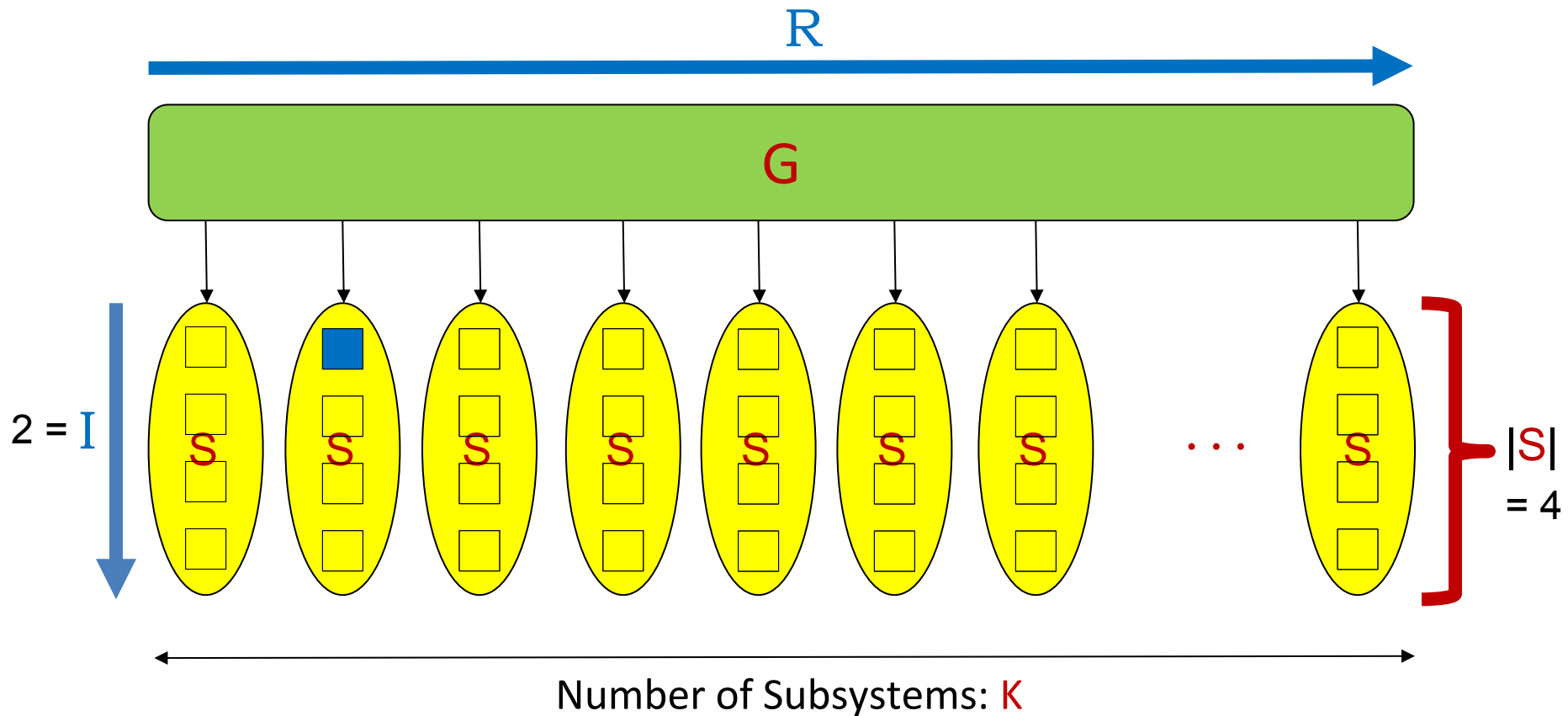


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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$$\text{Physical System Size } |\mathbf{G}| = \mathbf{K} \cdot |\mathbf{S}|$$

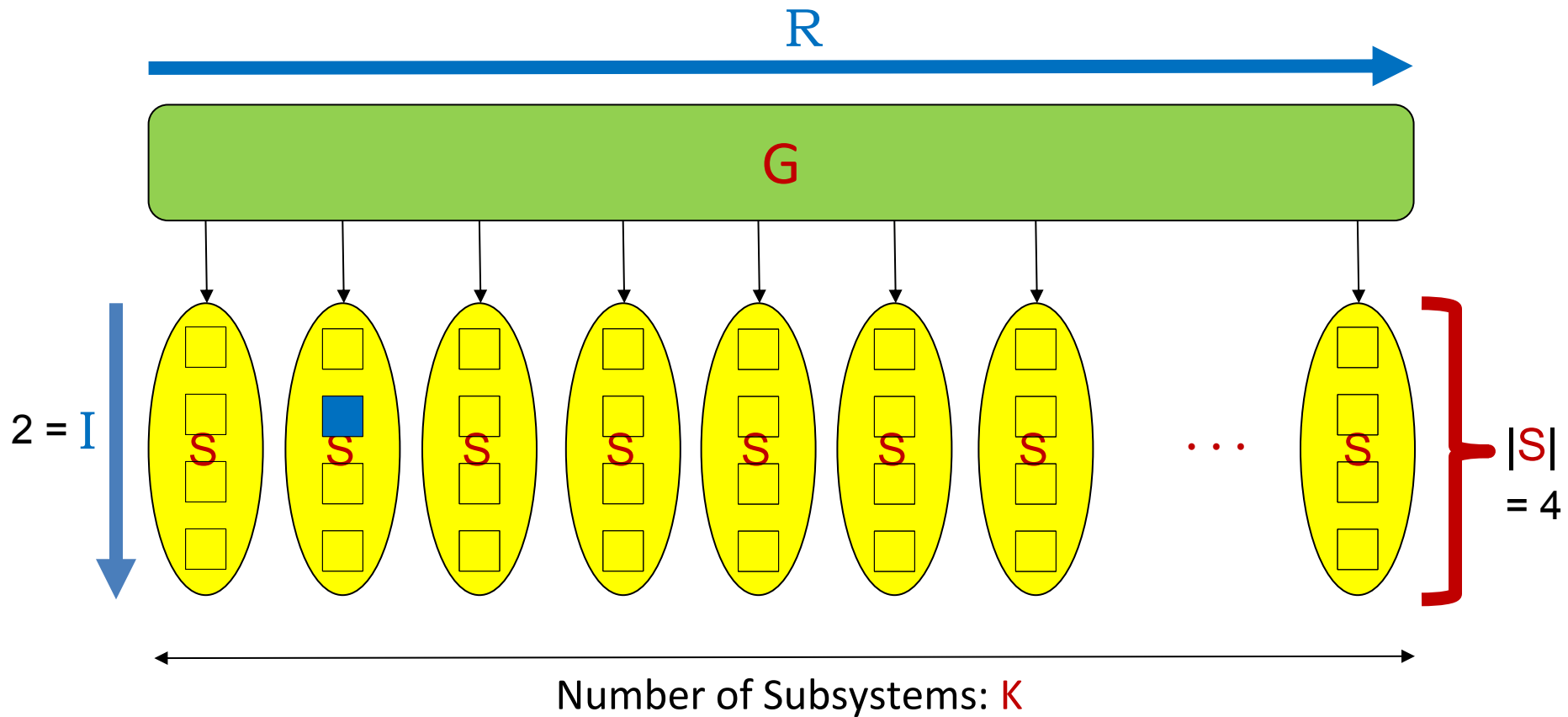


3. Analyzing the Benchmark Data

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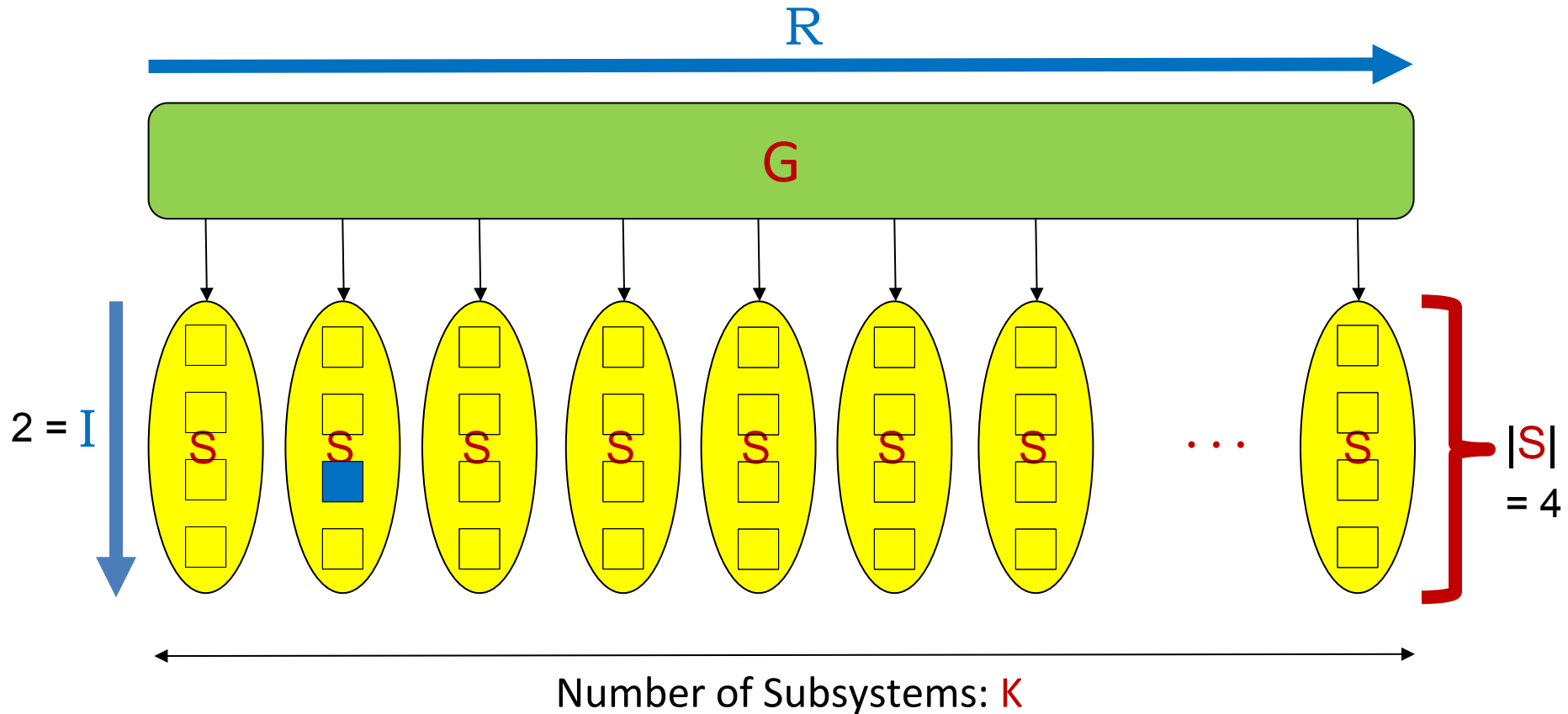


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Benchmark II: LOCALITY

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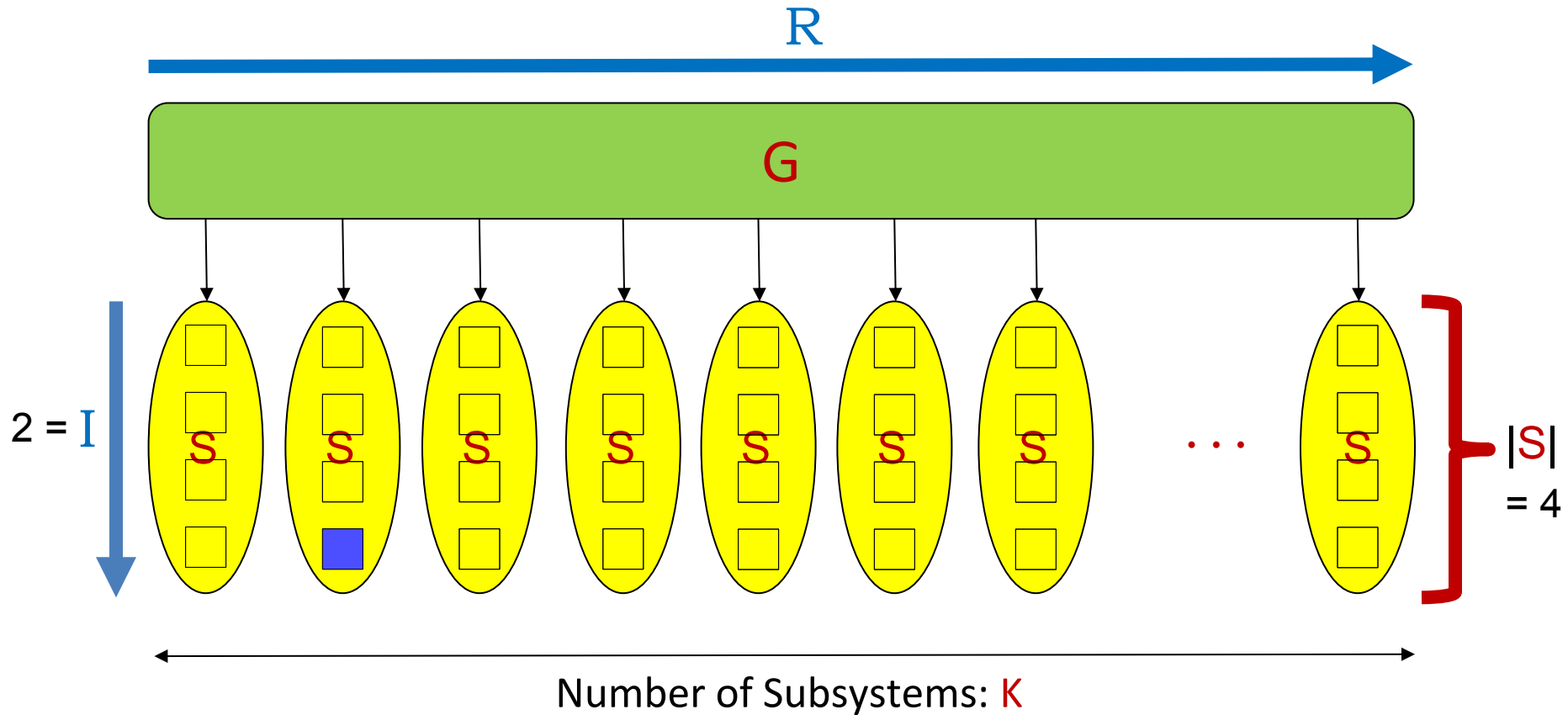


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

$$\text{Problem Size: } \mathbf{N} = |\mathbf{G}| \cdot \mathbf{I} \cdot \mathbf{R}$$

$$\text{Physical System Size } |\mathbf{G}| = \mathbf{K} \cdot |\mathbf{S}|$$

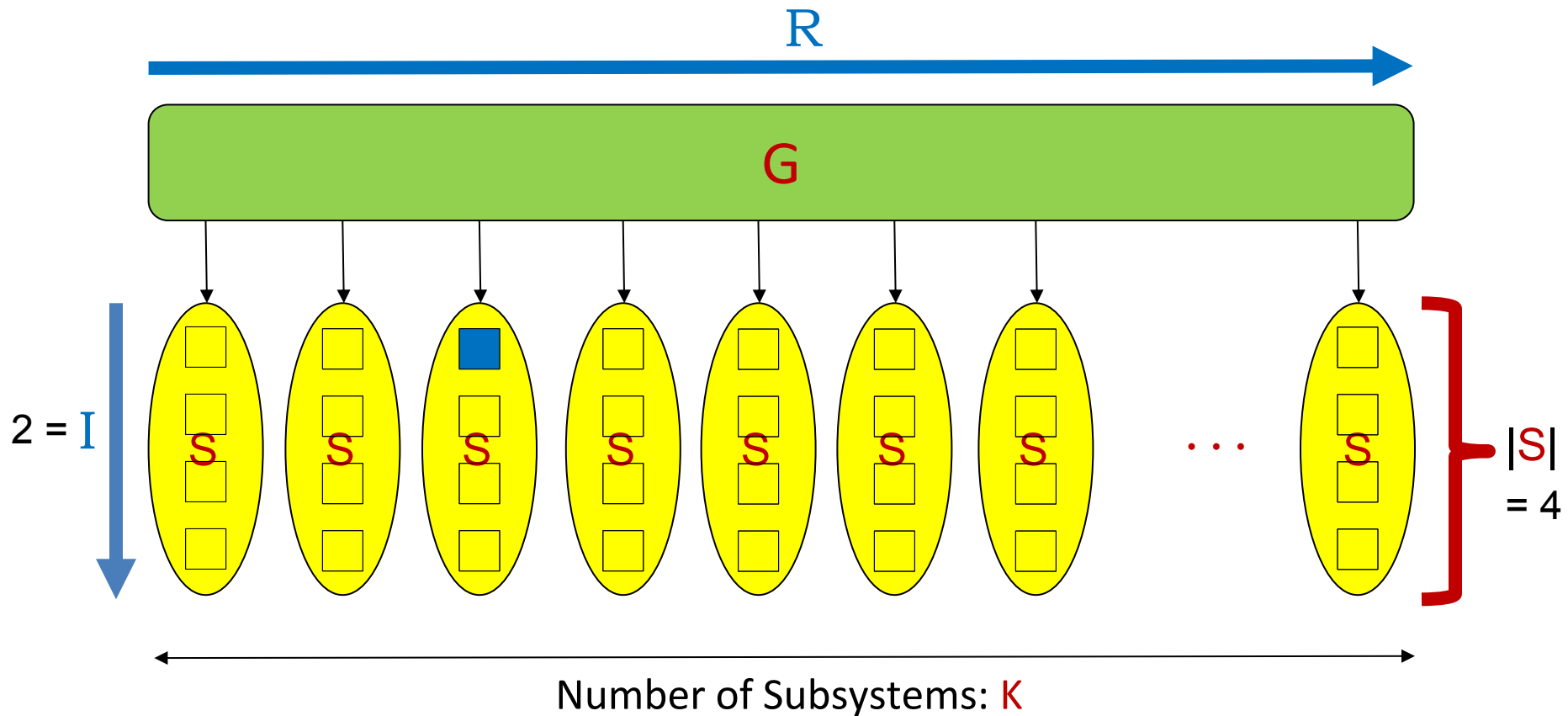


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

$$\text{Problem Size: } \mathbf{N} = |\mathbf{G}| \cdot \mathbf{I} \cdot \mathbf{R}$$

$$\text{Physical System Size } |\mathbf{G}| = \mathbf{K} \cdot |\mathbf{S}|$$

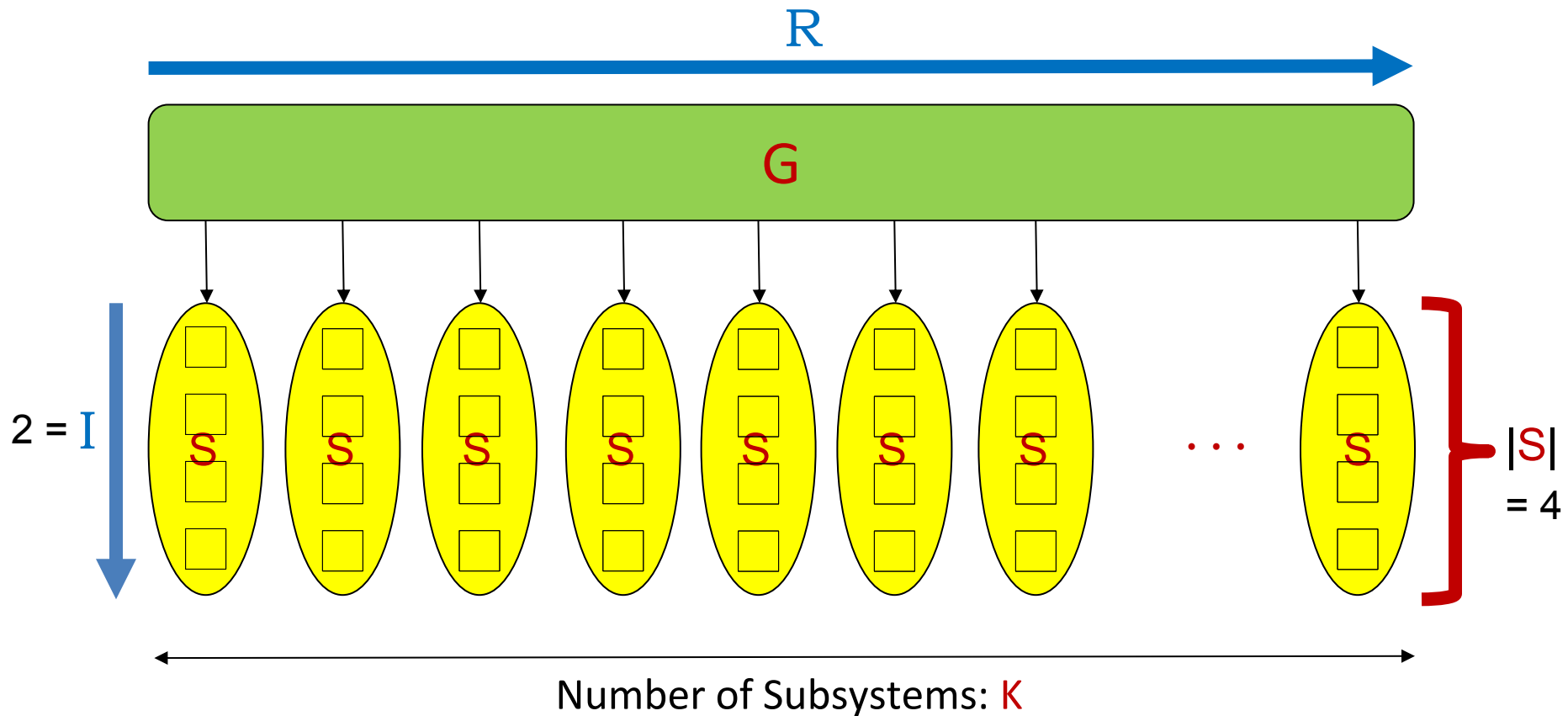


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

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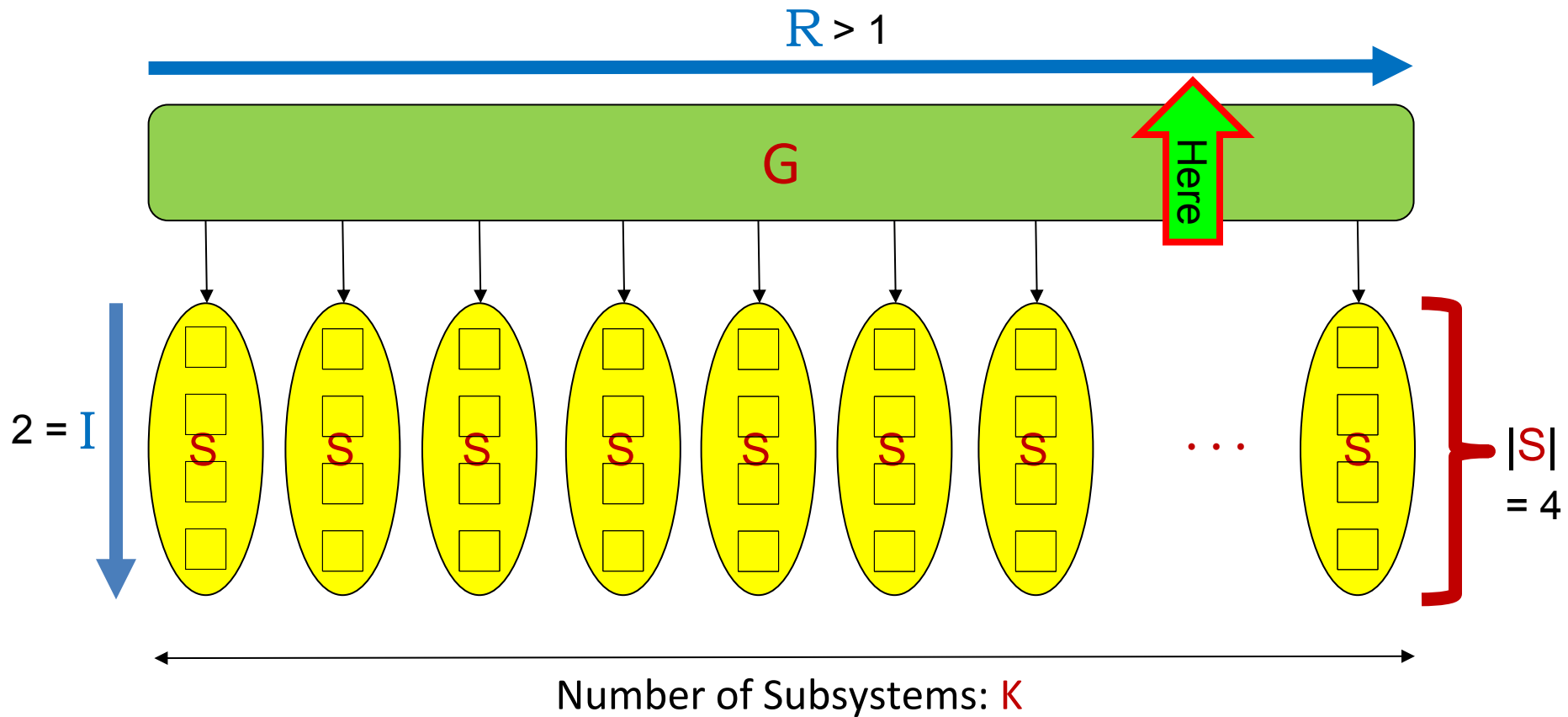


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Benchmark II: LOCALITY

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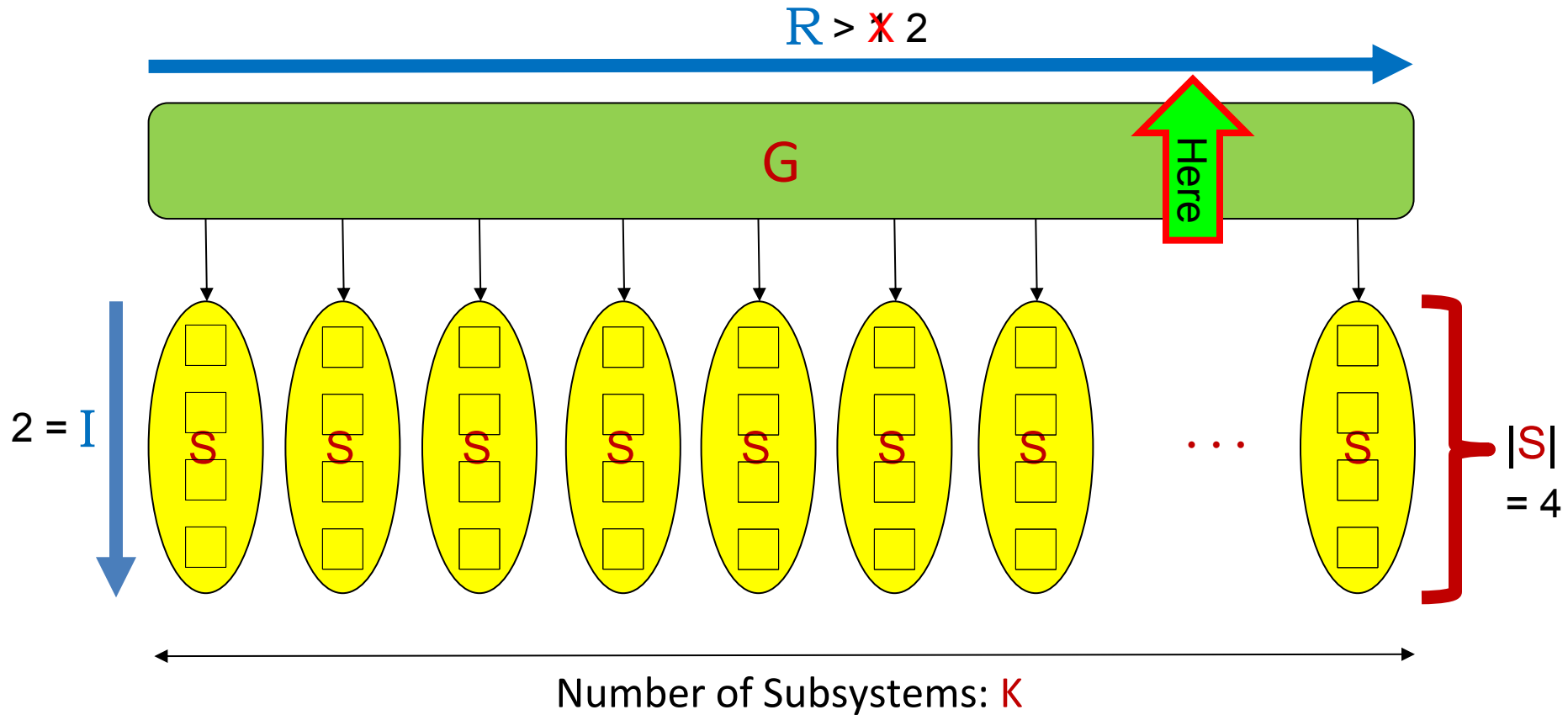


3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Problem Size: $N = |G| \cdot I \cdot R$

Physical System Size $|G| = K \cdot |S|$



3. Analyzing the Benchmark Data

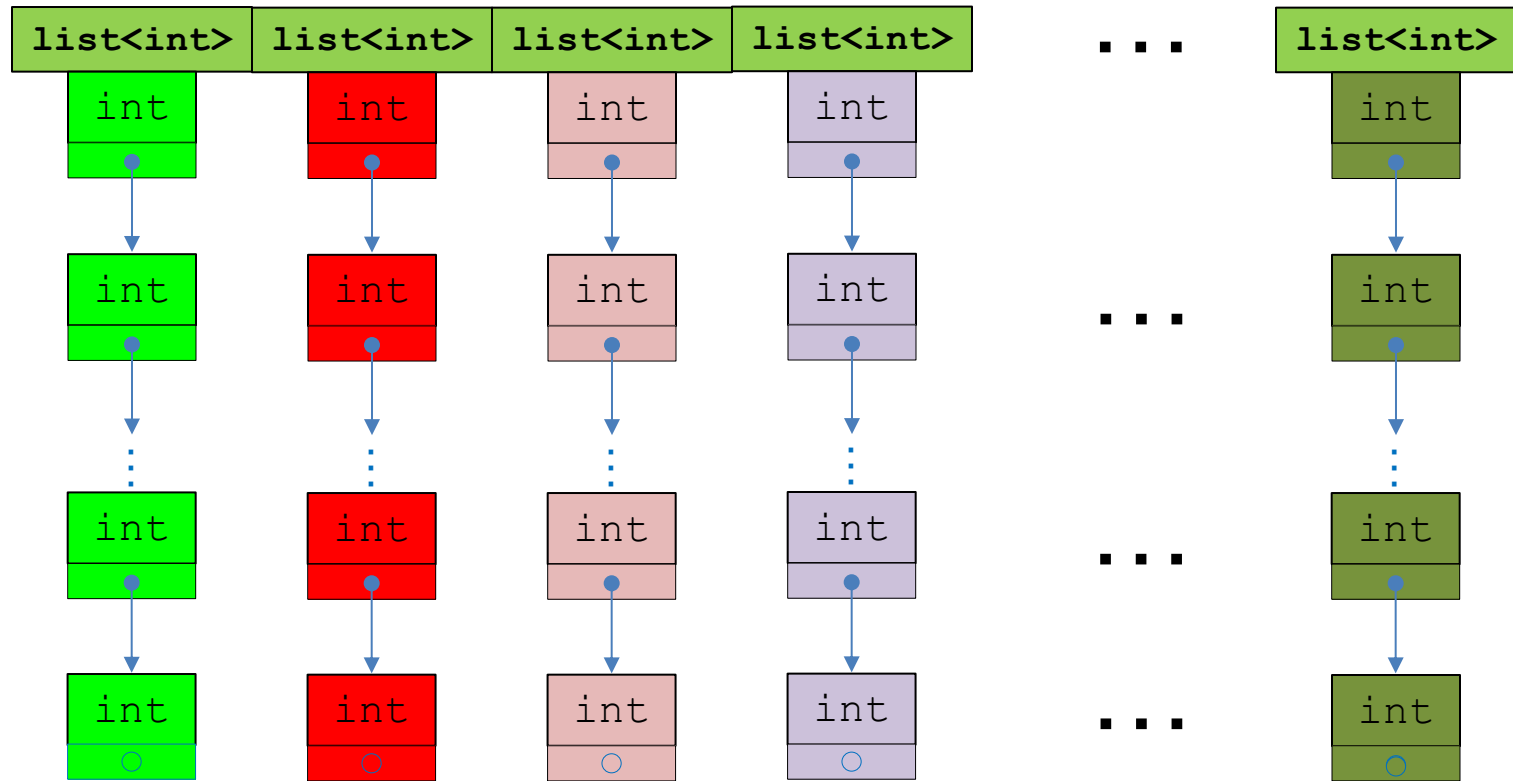
Benchmark II: LOCALITY

Shuffle Plan:

- Build up a data structure **G**: `vector<list<int>>`
- Visit each of the subsystems **S_j** of **G** in turn.
 - Pop the last element of **S_j** after saving its `int` value.
 - Push that value onto the front of a random **S_i**.
 - Repeat until the number of moves reaches **sf** · |**G**|.
 - The non-negative integer **sf** represents the **shuffle factor**.
- The result of this experiment is a shuffled system **G**.
 - There is also the added runtime to do the shuffle.
- Additional consideration: The shuffle is heuristic ...
 - This to keep the time to shuffle as small as possible.

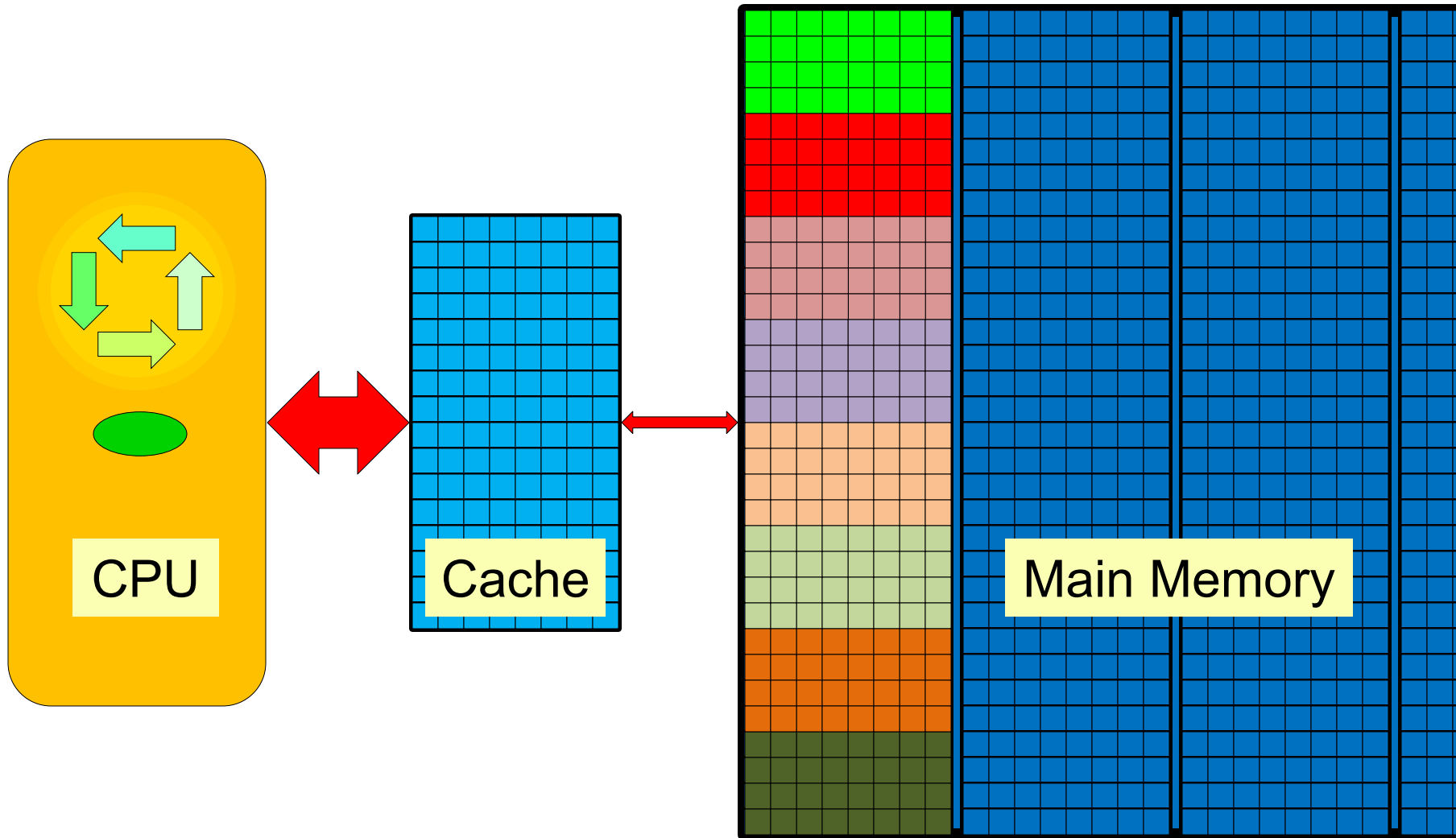
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Overall (Multiprogram) Plan:

- A. Create and Access After Shuffle:
- B. Create and Access Before Shuffle.
- C. Create and Shuffle Only

The result of each program is its (wall) **RUNTIME**.

Shuffled-Memory Access Time: $A - C$

Unshuffled-Memory Access Time: $B - C$

Degradation Ratio due to memory diffusion (DR):

$$\text{Degredation Ratio (DR)} = \frac{A - C}{B - C}$$

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Contrasting access times across (sub)system size

Overall System Size = 10^7

$$\log_{10} |G| = 7$$

These
are all
exponents
of 10.

| Subsystem Size | Number of Subsystems |
|----------------|----------------------|
| 0 | 7 |
| 1 | 6 |
| 2 | 5 |
| 3 | 4 |
| 4 | 3 |
| 5 | 2 |
| 6 | 1 |
| 7 | 0 |

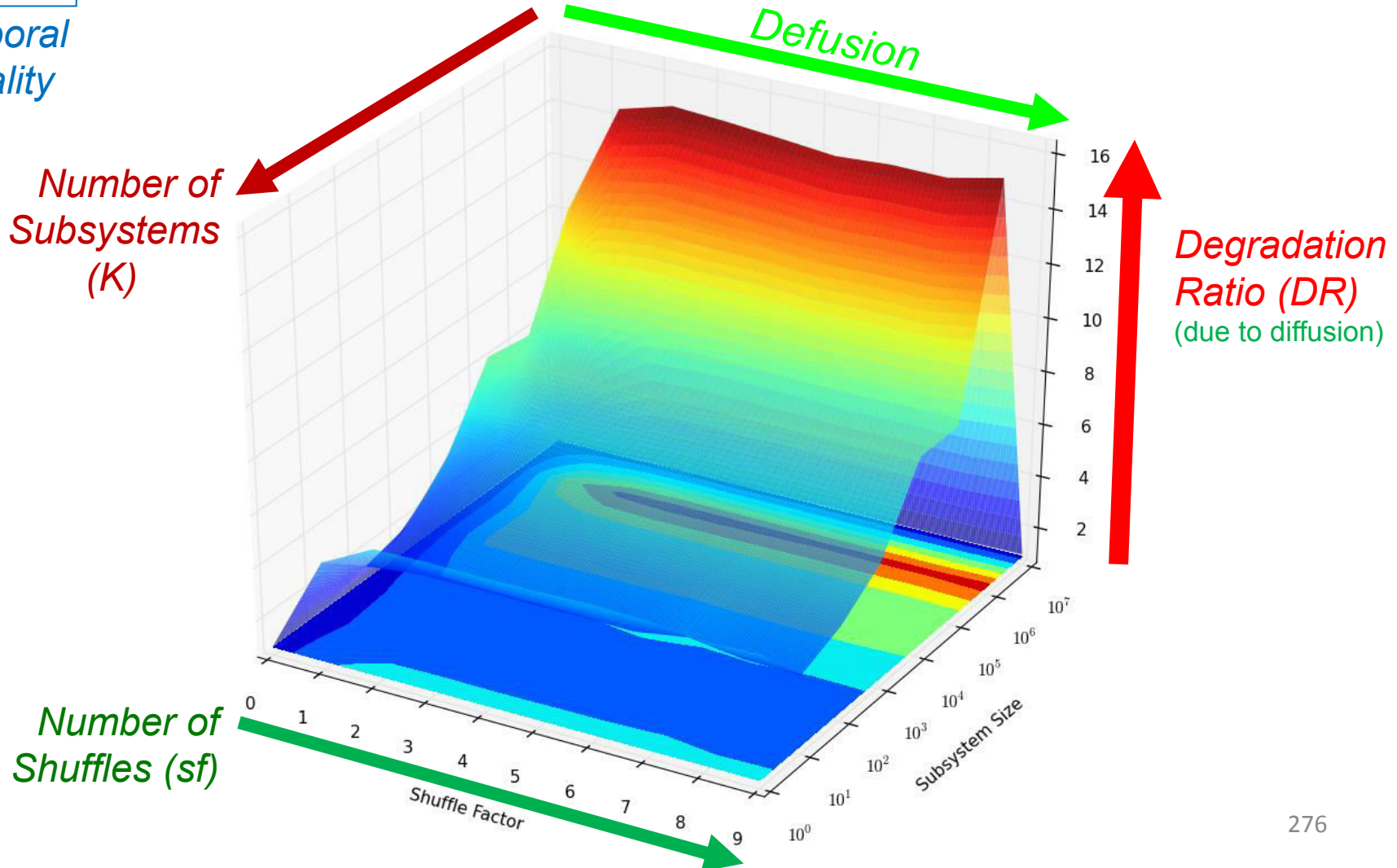
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

$I = 10$

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

We'll use *shuffle factor*
sf = 5 from now on.

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$

Diffusion



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Degradation Ratio (DR)

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

I = 10

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



Number of Complete Shuffles (10^7 move operations)

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|-----|------|------|------|------|------|------|------|------|------|
| 10^7 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 10^6 | 1.0 | 11.4 | 15.6 | 16.2 | 16.0 | 15.8 | 15.6 | 15.8 | 15.7 | 16.2 |
| 10^5 | 1.0 | 7.7 | 7.8 | 7.8 | 7.8 | 8.0 | 8.0 | 8.0 | 8.0 | 8.2 |
| 10^4 | 1.0 | 8.0 | 8.1 | 8.1 | 8.1 | 7.9 | 8.2 | 8.2 | 8.3 | 8.2 |
| 10^3 | 1.0 | 5.4 | 5.4 | 5.4 | 5.4 | 5.7 | 5.3 | 5.4 | 5.3 | 5.4 |
| 10^2 | 1.0 | 3.8 | 4.0 | 4.1 | 4.2 | 4.1 | 4.2 | 4.3 | 4.2 | 4.2 |
| 10^1 | 1.0 | 3.4 | 3.6 | 3.6 | 3.6 | 3.6 | 3.6 | 3.9 | 3.6 | 3.6 |
| 10^0 | 1.0 | 4.7 | 5.7 | 5.8 | 5.7 | 5.8 | 5.8 | 5.7 | 5.5 | 5.6 |

Subsystem size
is just one link!

Degradation Ratio (DR)

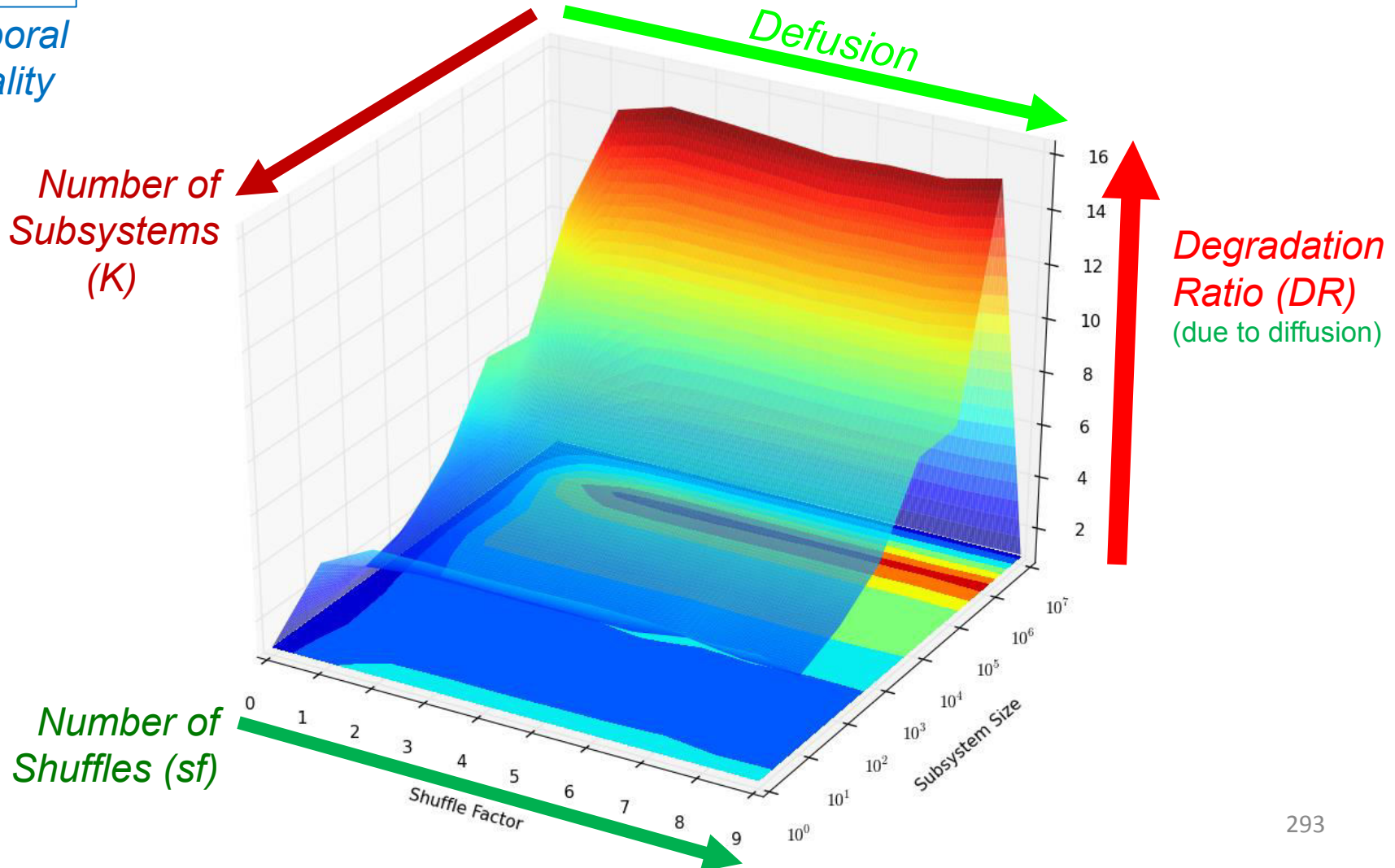
3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

$I = 10$

Temporal
Locality

Physical System Size $|G| = K \cdot |S| = 10^7$



3. Analyzing the Benchmark Data
Benchmark II: LOCALITY

Questions
and/or
Discussion?

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Which local
Allocation Strategy
should we use?

3. Analyzing the Benchmark Data
Benchmark II: LOCALITY

Which local
Allocation Strategy
should we use?

AS7, AS9, AS11, or AS13

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Contrasting access times across (sub)system size

Overall System Size = 2^{21}

$$\log_2 |G| = 21$$

These
are all
exponents
of 2.

| Subsystem Size | Number of Subsystems |
|----------------|----------------------|
| 0 | 21 |
| 1 | 20 |
| 2 | 19 |
| 3 | 18 |
| 4 | 17 |
| 5 | 16 |
| 6 | 15 |
| : | : |

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

Contrasting access times across access rates

Overall Access Size = 2^{32}

$$\log_2 \mathbf{N} = 32$$

These
are all
exponents
of 2.

| Number of Iterations (I) | Number of Repitions (R) |
|--------------------------|-------------------------|
| 8 | 24 |
| 7 | 25 |
| 6 | 26 |
| 5 | 27 |
| 4 | 28 |
| 3 | 29 |
| 2 | 30 |
| 1 | 31 |
| 0 | 32 |

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21}

Without Local Allocators

sf = 5

Diffusion

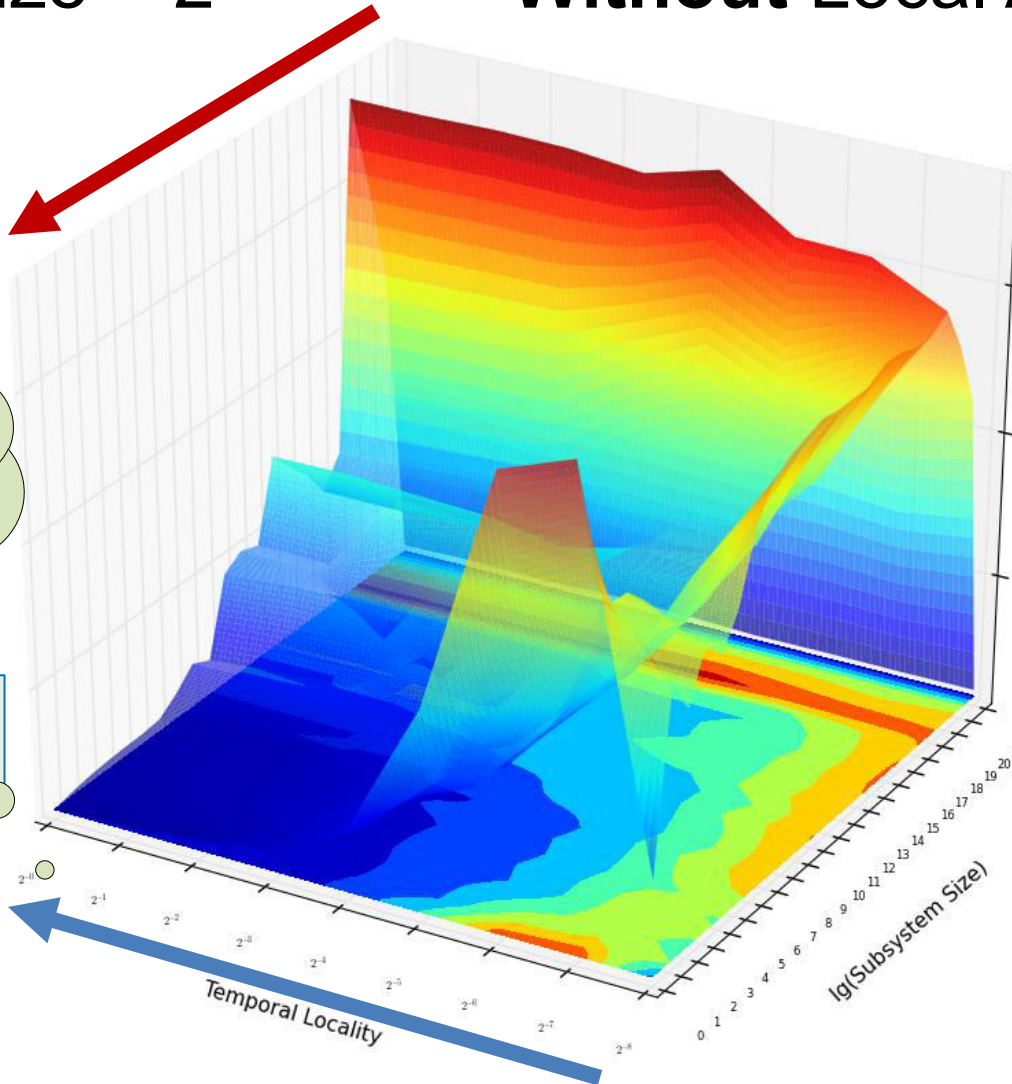
*Physical
Locality*

I · **R** is fixed.

I ranges from
[2^8 .. 2^0].

Max *Temporal
Locality* = 256

*Temporal
Locality*



15.0

10.0

5.0

*Degradation
Ratio (DR)*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21}

Without Local Allocators

sf = 5

Diffusion

*Physical
Locality*

Max *Temporal
Locality* = 256

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 21 | 1.00 | 1.06 | 1.01 | 1.09 | 1.04 | 0.96 | 0.98 | 0.97 | 0.99 |
| 20 | 11.30 | 11.50 | 11.30 | 11.40 | 11.20 | 11.30 | 11.30 | 11.00 | 11.60 |
| 19 | 14.80 | 15.00 | 14.70 | 14.80 | 14.70 | 14.80 | 14.30 | 13.10 | 13.80 |
| 18 | 18.00 | 18.00 | 18.00 | 17.90 | 17.70 | 18.40 | 16.70 | 16.60 | 15.40 |
| 17 | 6.04 | 6.17 | 6.30 | 6.51 | 8.64 | 9.95 | 9.17 | 11.50 | 15.00 |
| 16 | 5.07 | 5.07 | 5.13 | 5.19 | 7.16 | 7.24 | 7.52 | 10.80 | 14.90 |
| 15 | 6.08 | 6.08 | 6.15 | 6.05 | 5.37 | 7.30 | 7.72 | 10.40 | 15.20 |
| 14 | 6.77 | 6.81 | 6.78 | 6.67 | 6.25 | 7.23 | 7.73 | 10.90 | 15.20 |
| 13 | 7.55 | 7.59 | 7.46 | 7.36 | 6.92 | 7.51 | 7.99 | 10.80 | 14.90 |
| 12 | 4.82 | 4.79 | 7.70 | 7.60 | 7.08 | 7.26 | 7.55 | 11.40 | 14.90 |
| 11 | 5.05 | 4.99 | 3.21 | 6.66 | 6.23 | 5.85 | 6.27 | 9.83 | 14.90 |
| 10 | 4.65 | 4.87 | 4.93 | 2.92 | 5.71 | 5.99 | 6.15 | 10.70 | 15.00 |
| 9 | 2.01 | 2.23 | 2.38 | 4.15 | 3.03 | 6.14 | 6.18 | 9.67 | 14.80 |
| 8 | 2.32 | 2.40 | 2.60 | 2.08 | 3.63 | 4.86 | 6.01 | 9.25 | 14.60 |
| 7 | 1.68 | 1.75 | 1.92 | 2.36 | 2.30 | 3.51 | 6.12 | 10.50 | 14.20 |
| 6 | 1.22 | 1.31 | 1.44 | 2.06 | 2.76 | 4.18 | 6.16 | 9.93 | 13.20 |
| 5 | 1.15 | 1.24 | 1.39 | 1.75 | 2.40 | 3.45 | 6.35 | 9.50 | 10.90 |
| 4 | 1.13 | 1.23 | 1.37 | 1.72 | 2.53 | 4.05 | 6.60 | 11.00 | 9.77 |
| 3 | 1.10 | 1.19 | 1.37 | 1.72 | 2.55 | 3.66 | 6.42 | 11.60 | 10.50 |
| 2 | 1.04 | 1.14 | 1.36 | 1.79 | 2.43 | 4.61 | 8.51 | 11.70 | 8.91 |
| 1 | 0.93 | 1.06 | 1.26 | 1.66 | 2.55 | 4.86 | 11.60 | 12.90 | 10.00 |
| 0 | 0.78 | 0.90 | 1.10 | 1.61 | 2.88 | 7.75 | 16.20 | 17.20 | 4.06 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21}

Without Local Allocators

sf = 5

Diffusion

*Physical
Locality*

*Degradation
Ratio (DR)*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 21 | 1.00 | 1.06 | 1.01 | 1.09 | 1.04 | 0.96 | 0.98 | 0.97 | 0.99 |
| 20 | 11.30 | 11.50 | 11.30 | 11.40 | 11.20 | 11.30 | 11.30 | 11.00 | 11.60 |
| 19 | 14.80 | 15.00 | 14.70 | 14.80 | 14.70 | 14.80 | 14.30 | 13.10 | 13.80 |
| 18 | 18.00 | 18.00 | 18.00 | 17.90 | 17.70 | 18.40 | 16.70 | 16.60 | 15.40 |
| 17 | 6.04 | 6.17 | 6.30 | 6.51 | 8.64 | 9.95 | 9.17 | 11.50 | 15.00 |
| 16 | 5.07 | 5.07 | 5.13 | 5.19 | 7.16 | 7.24 | 7.52 | 10.80 | 14.90 |
| 15 | 6.08 | 6.08 | 6.15 | 6.05 | 5.37 | 7.30 | 7.72 | 10.40 | 15.20 |
| 14 | 6.77 | 6.81 | 6.78 | 6.67 | 6.25 | 7.23 | 7.73 | 10.90 | 15.20 |
| 13 | 7.55 | 7.59 | 7.46 | 7.36 | 6.92 | 7.51 | 7.99 | 10.80 | 14.90 |
| 12 | 4.82 | 4.79 | 7.70 | 7.60 | 7.08 | 7.26 | 7.55 | 11.40 | 14.90 |
| 11 | 5.05 | 4.99 | 3.21 | 6.66 | 6.23 | 5.85 | 6.27 | 9.83 | 14.90 |
| 10 | 4.65 | 4.87 | 4.93 | 2.92 | 5.71 | 5.99 | 6.15 | 10.70 | 15.00 |
| 9 | 2.01 | 2.23 | 2.38 | 4.15 | 3.03 | 6.14 | 6.18 | 9.67 | 14.80 |
| 8 | 2.32 | 2.40 | 2.60 | 2.08 | 3.63 | 4.86 | 6.01 | 9.25 | 14.60 |
| 7 | 1.68 | 1.75 | 1.92 | 2.36 | 2.30 | 3.51 | 6.12 | 10.50 | 14.20 |
| 6 | 1.22 | 1.31 | 1.44 | 2.06 | 2.76 | 4.18 | 6.16 | 9.93 | 13.20 |
| 5 | 1.15 | 1.24 | 1.39 | 1.75 | 2.40 | 3.45 | 6.35 | 9.50 | 10.90 |
| 4 | 1.13 | 1.23 | 1.37 | 1.72 | 2.53 | 4.05 | 6.60 | 11.00 | 9.77 |
| 3 | 1.10 | 1.19 | 1.37 | 1.72 | 2.55 | 3.66 | 6.42 | 11.60 | 10.50 |
| 2 | 1.04 | 1.14 | 1.36 | 1.79 | 2.43 | 4.61 | 8.51 | 11.70 | 8.91 |
| 1 | 0.93 | 1.06 | 1.26 | 1.66 | 2.55 | 4.86 | mask | 10.00 | |
| 0 | 0.78 | 0.90 | 1.10 | 1.61 | 2.88 | 7.75 | mask | 4.06 | |

Max *Temporal
Locality* = 256

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25}

Without Local Allocators

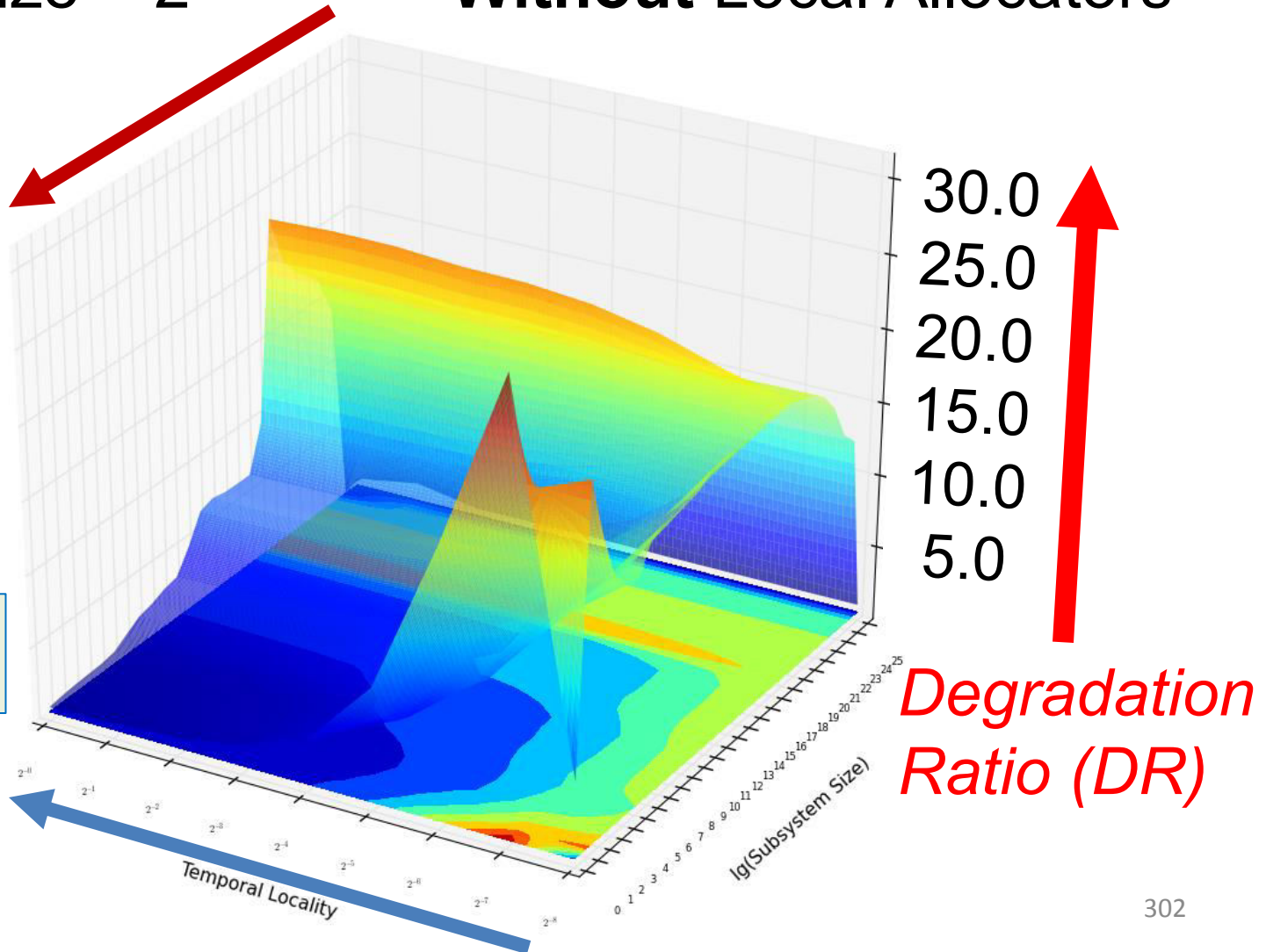
sf = 5

Diffusion

*Physical
Locality*

Max *Temporal
Locality* = 256

*Temporal
Locality*



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25}

Without Local Allocators

sf = 5
Diffusion

*Physical
Locality*

*Degradation
Ratio (DR)*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 25 | 0.97 | 1.72 | 0.98 | 1.02 | 1.04 | 1.00 | 1.00 | 1.00 | 1.01 |
| 24 | 0.50 | 12.71 | 12.81 | 13.02 | 13.08 | 13.02 | 13.01 | 12.95 | 13.11 |
| 23 | 14.20 | 14.03 | 14.10 | 14.07 | 14.14 | 14.05 | 14.07 | 14.13 | 14.14 |
| 22 | 16.70 | 16.71 | 16.50 | 16.55 | 16.49 | 16.62 | 16.55 | 16.56 | 16.53 |
| 21 | 17.80 | 17.90 | 17.87 | 17.72 | 17.85 | 17.83 | 17.83 | 17.76 | 17.89 |
| 20 | 18.60 | 18.60 | 18.52 | 18.54 | 18.45 | 18.64 | 18.43 | 18.62 | 18.66 |
| 19 | 20.10 | 20.16 | 19.96 | 19.85 | 19.80 | 19.64 | 19.25 | 19.12 | 18.93 |
| 18 | 23.40 | 23.54 | 23.51 | 23.20 | 23.13 | 22.72 | 21.85 | 20.45 | 19.34 |
| 17 | 9.81 | 10.00 | 10.06 | 10.29 | 10.69 | 11.53 | 13.01 | 15.53 | 19.30 |
| 16 | 6.81 | 6.87 | 6.98 | 7.21 | 7.70 | 8.64 | 10.41 | 13.75 | 19.33 |
| 15 | 6.80 | 6.88 | 7.00 | 7.17 | 7.66 | 8.63 | 10.38 | 13.66 | 19.32 |
| 14 | 6.82 | 6.86 | 7.00 | 7.20 | 7.66 | 8.56 | 10.39 | 13.66 | 19.18 |
| 13 | 7.03 | 7.08 | 7.19 | 7.39 | 7.85 | 8.79 | 10.56 | 13.77 | 19.15 |
| 12 | 6.72 | 6.75 | 6.90 | 7.12 | 7.62 | 8.52 | 10.21 | 13.62 | 19.30 |
| 11 | 4.86 | 4.92 | 5.07 | 5.35 | 5.88 | 6.92 | 9.01 | 13.00 | 19.16 |
| 10 | 3.36 | 3.49 | 3.71 | 4.07 | 4.69 | 5.91 | 8.25 | 12.32 | 18.43 |
| 9 | 3.15 | 3.29 | 3.51 | 3.86 | 4.54 | 5.87 | 8.25 | 12.37 | 18.28 |
| 8 | 2.76 | 2.89 | 3.13 | 3.54 | 4.33 | 5.66 | 8.12 | 12.43 | 18.16 |
| 7 | 2.52 | 2.66 | 2.96 | 3.45 | 4.25 | 5.67 | 8.16 | 12.65 | 18.10 |
| 6 | 1.94 | 2.14 | 2.49 | 3.03 | 3.91 | 5.45 | 8.02 | 12.72 | 17.64 |
| 5 | 1.34 | 1.49 | 1.78 | 2.33 | 3.24 | 4.79 | 7.54 | 12.41 | 15.84 |
| 4 | 1.17 | 1.28 | 1.51 | 1.96 | 2.83 | 4.39 | 7.39 | 13.22 | 16.25 |
| 3 | 1.12 | 1.24 | 1.45 | 1.89 | 2.73 | 4.30 | 7.85 | 14.74 | 17.32 |
| 2 | 1.06 | 1.19 | 1.43 | 1.90 | 2.71 | 4.70 | 9.98 | 18.32 | 20.54 |
| 1 | 0.97 | 1.11 | 1.36 | 1.78 | 2.91 | 5.68 | 13.74 | 22.91 | 24.73 |
| 0 | 0.82 | 0.97 | 1.22 | 1.88 | 3.50 | 8.30 | 18.92 | 30.99 | 5.68 |

Max *Temporal
Locality* = 256

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25}

Without Local Allocators

sf = 5
Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 25 | 0.97 | 1.72 | 0.98 | 1.02 | 1.04 | 1.00 | 1.00 | 1.00 | 1.01 |
| 24 | 0.50 | 12.71 | 12.81 | 13.02 | 13.08 | 13.02 | 13.01 | 12.95 | 13.11 |
| 23 | 14.20 | 14.03 | 14.10 | 14.07 | 14.14 | 14.05 | 14.07 | 14.13 | 14.14 |
| 22 | 16.70 | 16.71 | 16.50 | 16.55 | 16.49 | 16.62 | 16.55 | 16.56 | 16.53 |
| 21 | 17.80 | 17.90 | 17.87 | 17.72 | 17.85 | 17.83 | 17.83 | 17.76 | 17.89 |
| 20 | 18.60 | 18.60 | 18.52 | 18.54 | 18.45 | 18.64 | 18.43 | 18.62 | 18.66 |
| 19 | 20.10 | 20.16 | 19.96 | 19.85 | 19.80 | 19.64 | 19.25 | 19.12 | 18.93 |
| 18 | 23.40 | 23.54 | 23.51 | 23.20 | 23.13 | 22.72 | 21.85 | 20.45 | 19.34 |
| 17 | 9.81 | 10.00 | 10.06 | 10.29 | 10.69 | 11.53 | 13.01 | 15.53 | 19.30 |
| 16 | 6.81 | 6.87 | 6.98 | 7.21 | 7.70 | 8.64 | 10.41 | 13.75 | 19.33 |
| 15 | 6.80 | 6.88 | 7.00 | 7.17 | 7.66 | 8.63 | 10.38 | 13.66 | 19.32 |
| 14 | 6.82 | 6.86 | 7.00 | 7.20 | 7.66 | 8.56 | 10.39 | 13.66 | 19.18 |
| 13 | 7.03 | 7.08 | 7.19 | 7.39 | 7.85 | 8.79 | 10.56 | 13.77 | 19.15 |
| 12 | 6.72 | 6.75 | 6.90 | 7.12 | 7.62 | 8.52 | 10.21 | 13.62 | 19.30 |
| 11 | 4.86 | 4.92 | 5.07 | 5.35 | 5.88 | 6.92 | 9.01 | 13.00 | 19.16 |
| 10 | 3.36 | 3.49 | 3.71 | 4.07 | 4.69 | 5.91 | 8.25 | 12.32 | 18.43 |
| 9 | 3.15 | 3.29 | 3.51 | 3.86 | 4.54 | 5.87 | 8.25 | 12.37 | 18.28 |
| 8 | 2.76 | 2.89 | 3.13 | 3.54 | 4.33 | 5.66 | 8.12 | 12.43 | 18.16 |
| 7 | 2.52 | 2.66 | 2.96 | 3.45 | 4.25 | 5.67 | 8.16 | 12.65 | 18.10 |
| 6 | 1.94 | 2.14 | 2.49 | 3.03 | 3.91 | 5.45 | 8.02 | 12.72 | 17.64 |
| 5 | 1.34 | 1.49 | 1.78 | 2.33 | 3.24 | 4.79 | 7.54 | 12.41 | 15.84 |
| 4 | 1.17 | 1.28 | 1.51 | 1.96 | 2.83 | 4.39 | 7.39 | 13.22 | 16.25 |
| 3 | 1.12 | 1.24 | 1.45 | 1.89 | 2.73 | 4.30 | 7.85 | 14.74 | 17.32 |
| 2 | 1.06 | 1.19 | 1.43 | 1.90 | 2.71 | 4.70 | 9.98 | 18.32 | 20.54 |
| 1 | 0.97 | 1.11 | 1.36 | 1.78 | 2.91 | 5.68 | | | 24.73 |
| 0 | 0.82 | 0.97 | 1.22 | 1.88 | 3.50 | 8.30 | mask | | 5.68 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21}

With Local Allocators

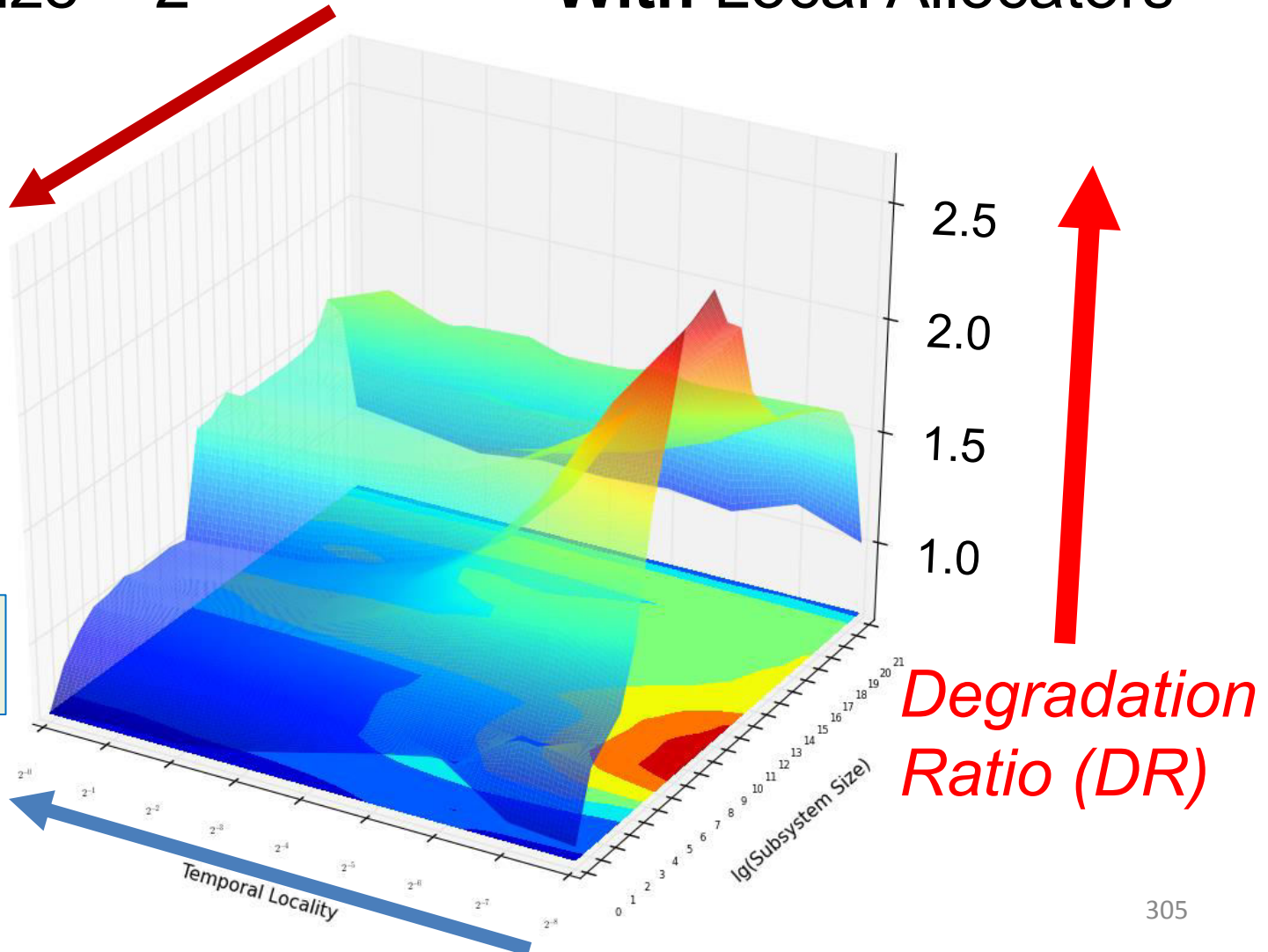
sf = 5

Diffusion

*Physical
Locality*

Max *Temporal
Locality* = 256

*Temporal
Locality*



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21}

With Local Allocators

sf = 5

Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 21 | 1.06 | 1.02 | 0.98 | 1.02 | 1.02 | 1.04 | 1.00 | 1.11 | 1.01 |
| 20 | 1.53 | 1.52 | 1.62 | 1.63 | 1.55 | 1.63 | 1.58 | 1.54 | 1.53 |
| 19 | 1.65 | 1.75 | 1.65 | 1.65 | 1.65 | 1.66 | 1.66 | 1.68 | 1.69 |
| 18 | 1.51 | 1.49 | 1.46 | 1.42 | 1.43 | 1.47 | 1.52 | 1.66 | 1.75 |
| 17 | 1.48 | 1.48 | 1.48 | 1.51 | 1.48 | 1.54 | 1.59 | 1.65 | 1.81 |
| 16 | 1.48 | 1.52 | 1.49 | 1.50 | 1.55 | 1.56 | 1.56 | 1.67 | 1.82 |
| 15 | 1.48 | 1.48 | 1.48 | 1.49 | 1.51 | 1.55 | 1.60 | 1.69 | 1.88 |
| 14 | 1.47 | 1.48 | 1.48 | 1.49 | 1.50 | 1.54 | 1.61 | 1.72 | 1.90 |
| 13 | 1.48 | 1.49 | 1.50 | 1.50 | 1.53 | 1.58 | 1.66 | 1.79 | 1.99 |
| 12 | 1.54 | 1.51 | 1.54 | 1.55 | 1.57 | 1.65 | 1.72 | 1.91 | 2.11 |
| 11 | 1.48 | 1.53 | 1.53 | 1.55 | 1.60 | 1.65 | 1.82 | 2.00 | 2.42 |
| 10 | 1.47 | 1.49 | 1.51 | 1.54 | 1.57 | 1.70 | 1.88 | 2.11 | 2.49 |
| 9 | 1.02 | 1.04 | 1.06 | 1.13 | 1.22 | 1.39 | 1.69 | 2.14 | 2.67 |
| 8 | 1.03 | 1.05 | 1.08 | 1.13 | 1.22 | 1.42 | 1.73 | 2.18 | 2.62 |
| 7 | 1.03 | 1.05 | 1.09 | 1.14 | 1.24 | 1.43 | 1.75 | 2.22 | 2.59 |
| 6 | 1.03 | 1.06 | 1.09 | 1.12 | 1.24 | 1.44 | 1.72 | 2.08 | 2.23 |
| 5 | 1.05 | 1.03 | 1.08 | 1.13 | 1.22 | 1.38 | 1.61 | 1.84 | 1.94 |
| 4 | 1.02 | 1.04 | 1.06 | 1.11 | 1.21 | 1.35 | 1.53 | 1.63 | 1.43 |
| 3 | 1.01 | 1.01 | 1.03 | 1.07 | 1.15 | 1.21 | 1.29 | 1.25 | 1.17 |
| 2 | 0.95 | 0.95 | 0.97 | 1.01 | 1.00 | 1.04 | 1.04 | 0.99 | 1.10 |
| 1 | 0.85 | 0.86 | 0.89 | 0.90 | 0.93 | 0.97 | 0.89 | 1.10 | 1.04 |
| 0 | 0.68 | 0.71 | 0.71 | 0.75 | 0.83 | 0.91 | 0.97 | 0.77 | 0.74 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25}

With Local Allocators

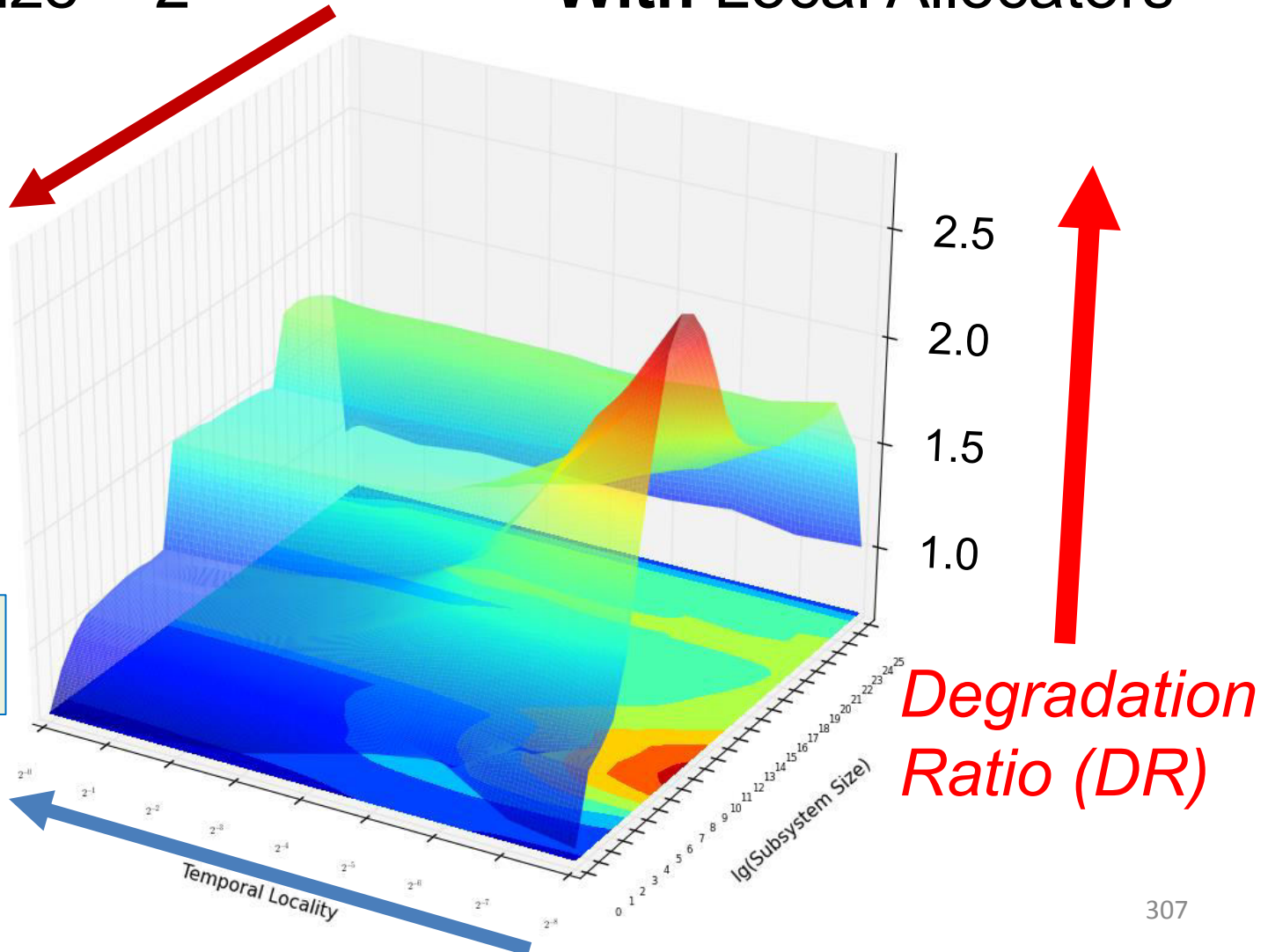
sf = 5

Diffusion

*Physical
Locality*

Max *Temporal
Locality* = 256

*Temporal
Locality*



3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25}

With Local Allocators

sf = 5
Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 25 | 1.00 | 0.97 | 1.01 | 1.00 | 1.00 | 1.01 | 1.04 | 0.99 | 1.01 |
| 24 | 1.00 | 1.54 | 1.57 | 1.55 | 1.55 | 1.53 | 1.55 | 1.56 | 1.53 |
| 23 | 1.71 | 1.67 | 1.70 | 1.69 | 1.68 | 1.68 | 1.68 | 1.69 | 1.67 |
| 22 | 1.75 | 1.75 | 1.76 | 1.76 | 1.75 | 1.72 | 1.76 | 1.76 | 1.83 |
| 21 | 1.79 | 1.78 | 1.78 | 1.80 | 1.79 | 1.74 | 1.80 | 1.80 | 1.80 |
| 20 | 1.80 | 1.80 | 1.80 | 1.81 | 1.81 | 1.82 | 1.81 | 1.81 | 1.82 |
| 19 | 1.79 | 1.78 | 1.79 | 1.80 | 1.79 | 1.80 | 1.80 | 1.82 | 1.82 |
| 18 | 1.47 | 1.47 | 1.47 | 1.49 | 1.50 | 1.53 | 1.58 | 1.67 | 1.83 |
| 17 | 1.49 | 1.49 | 1.49 | 1.50 | 1.51 | 1.54 | 1.59 | 1.67 | 1.84 |
| 16 | 1.50 | 1.50 | 1.53 | 1.51 | 1.53 | 1.55 | 1.61 | 1.70 | 1.88 |
| 15 | 1.51 | 1.51 | 1.51 | 1.52 | 1.53 | 1.56 | 1.63 | 1.74 | 1.92 |
| 14 | 1.51 | 1.51 | 1.52 | 1.52 | 1.54 | 1.58 | 1.65 | 1.78 | 1.97 |
| 13 | 1.51 | 1.52 | 1.52 | 1.53 | 1.55 | 1.60 | 1.67 | 1.82 | 2.05 |
| 12 | 1.53 | 1.54 | 1.54 | 1.56 | 1.59 | 1.64 | 1.74 | 1.92 | 2.20 |
| 11 | 1.54 | 1.54 | 1.55 | 1.57 | 1.60 | 1.67 | 1.84 | 2.08 | 2.43 |
| 10 | 1.54 | 1.55 | 1.56 | 1.58 | 1.61 | 1.74 | 1.93 | 2.25 | 2.63 |
| 9 | 1.07 | 1.08 | 1.11 | 1.16 | 1.26 | 1.44 | 1.87 | 2.22 | 2.76 |
| 8 | 1.06 | 1.10 | 1.12 | 1.18 | 1.27 | 1.47 | 1.85 | 2.29 | 2.80 |
| 7 | 1.07 | 1.06 | 1.12 | 1.17 | 1.28 | 1.48 | 1.82 | 2.32 | 2.67 |
| 6 | 1.07 | 1.08 | 1.10 | 1.16 | 1.26 | 1.46 | 1.75 | 2.13 | 2.31 |
| 5 | 1.05 | 1.06 | 1.09 | 1.14 | 1.23 | 1.40 | 1.62 | 1.86 | 1.93 |
| 4 | 1.04 | 1.05 | 1.07 | 1.12 | 1.22 | 1.38 | 1.54 | 1.65 | 1.44 |
| 3 | 1.02 | 1.03 | 1.05 | 1.08 | 1.15 | 1.23 | 1.30 | 1.29 | 1.20 |
| 2 | 0.96 | 0.97 | 0.99 | 1.02 | 1.02 | 1.04 | 1.05 | 1.00 | 1.12 |
| 1 | 0.85 | 0.86 | 0.89 | 0.90 | 0.94 | 0.99 | 0.90 | 1.08 | 1.06 |
| 0 | 0.69 | 0.70 | 0.72 | 0.75 | 0.84 | 0.92 | 0.98 | 0.79 | 0.74 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21} Without/With Local Allocators

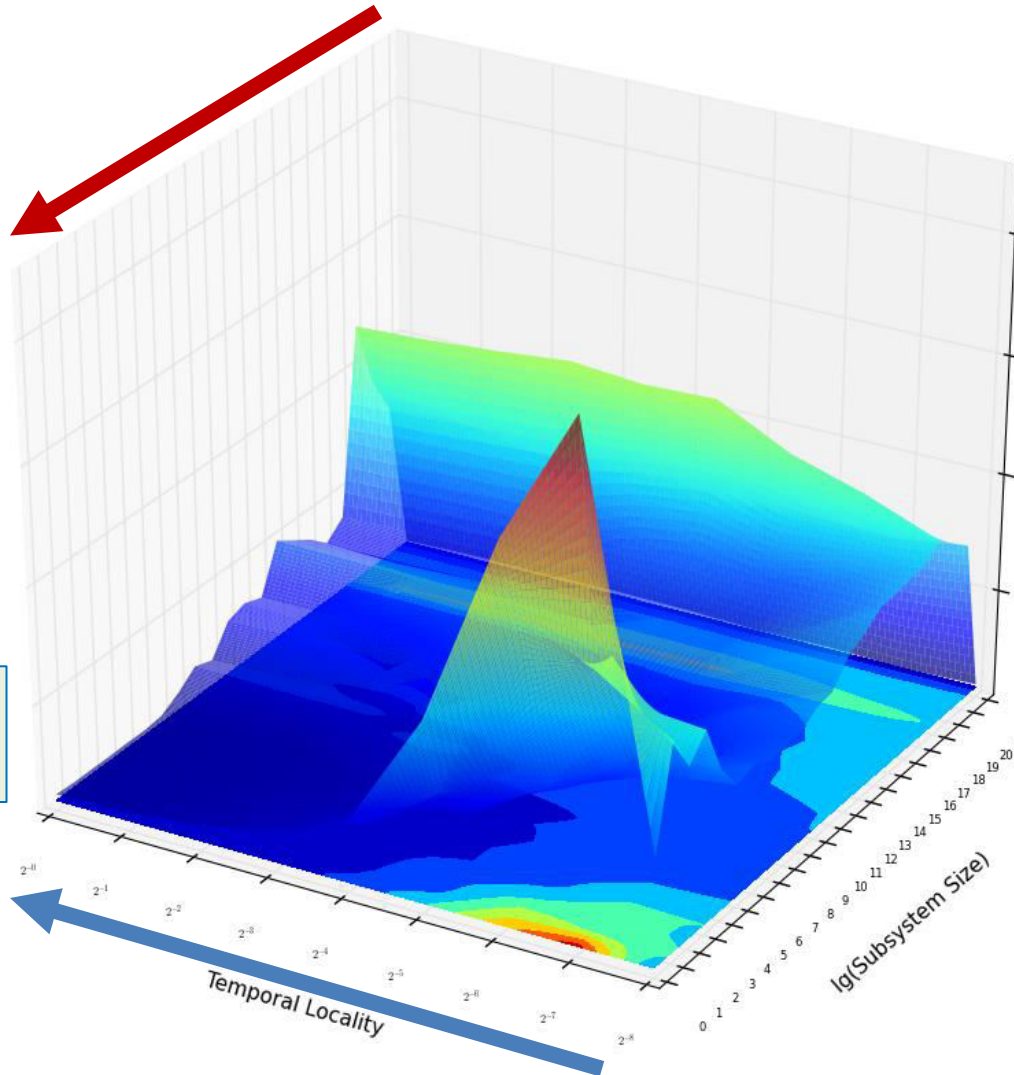
sf = 5

Diffusion

*Physical
Locality*

Max *Temporal
Locality* = 256

*Temporal
Locality*



*Degradation
Ratio (DR)*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21} Without/With Local Allocators

sf = 5
Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 21 | 0.95 | 1.03 | 1.03 | 1.07 | 1.02 | 0.92 | 0.97 | 0.87 | 0.98 |
| 20 | 7.40 | 7.56 | 6.97 | 6.96 | 7.27 | 6.94 | 7.15 | 7.10 | 7.56 |
| 19 | 9.02 | 8.56 | 8.95 | 8.99 | 8.92 | 8.92 | 8.61 | 7.82 | 8.17 |
| 18 | 11.90 | 12.10 | 12.30 | 12.60 | 12.40 | 12.50 | 10.90 | 10.00 | 8.80 |
| 17 | 4.07 | 4.16 | 4.26 | 4.31 | 5.85 | 6.48 | 5.78 | 6.97 | 8.27 |
| 16 | 3.43 | 3.34 | 3.45 | 3.45 | 4.61 | 4.63 | 4.82 | 6.49 | 8.19 |
| 15 | 4.11 | 4.11 | 4.16 | 4.06 | 3.56 | 4.71 | 4.84 | 6.14 | 8.09 |
| 14 | 4.59 | 4.61 | 4.59 | 4.47 | 4.15 | 4.69 | 4.81 | 6.34 | 8.02 |
| 13 | 5.11 | 5.08 | 4.96 | 4.90 | 4.52 | 4.76 | 4.82 | 6.03 | 7.47 |
| 12 | 3.12 | 3.16 | 5.01 | 4.89 | 4.51 | 4.41 | 4.40 | 5.96 | 7.08 |
| 11 | 3.41 | 3.27 | 2.09 | 4.31 | 3.90 | 3.54 | 3.45 | 4.91 | 6.15 |
| 10 | 3.16 | 3.26 | 3.27 | 1.89 | 3.63 | 3.53 | 3.28 | 5.08 | 6.04 |
| 9 | 1.98 | 2.15 | 2.24 | 3.68 | 2.48 | 4.43 | 3.66 | 4.51 | 5.56 |
| 8 | 2.24 | 2.29 | 2.42 | 1.83 | 2.97 | 3.43 | 3.48 | 4.24 | 5.59 |
| 7 | 1.64 | 1.67 | 1.77 | 2.07 | 1.85 | 2.45 | 3.49 | 4.70 | 5.49 |
| 6 | 1.19 | 1.24 | 1.32 | 1.83 | 2.23 | 2.91 | 3.59 | 4.78 | 5.91 |
| 5 | 1.10 | 1.20 | 1.29 | 1.55 | 1.97 | 2.50 | 3.96 | 5.17 | 5.61 |
| 4 | 1.11 | 1.18 | 1.30 | 1.55 | 2.09 | 3.00 | 4.31 | 6.73 | 6.82 |
| 3 | 1.09 | 1.18 | 1.33 | 1.60 | 2.23 | 3.02 | 4.99 | 9.30 | 9.03 |
| 2 | 1.10 | 1.21 | 1.40 | 1.76 | 2.42 | 4.43 | 8.19 | 11.80 | 8.09 |
| 1 | 1.09 | 1.24 | 1.41 | 1.85 | 2.73 | 5.00 | 13.00 | 11.70 | 9.70 |
| 0 | 1.14 | 1.26 | 1.56 | 2.14 | 3.47 | 8.54 | 16.70 | 22.40 | 5.46 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{21} Without/With Local Allocators

sf = 5

Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 21 | 0.95 | 1.03 | 1.03 | 1.07 | 1.02 | 0.92 | 0.97 | 0.87 | 0.98 |
| 20 | 7.40 | 7.56 | 6.97 | 6.96 | 7.27 | 6.94 | 7.15 | 7.10 | 7.56 |
| 19 | 9.02 | 8.56 | 8.95 | 8.99 | 8.92 | 8.92 | 8.61 | 7.82 | 8.17 |
| 18 | 11.90 | 12.10 | 12.30 | 12.60 | 12.40 | 12.50 | 10.90 | 10.00 | 8.80 |
| 17 | 4.07 | 4.16 | 4.26 | 4.31 | 5.85 | 6.48 | 5.78 | 6.97 | 8.27 |
| 16 | 3.43 | 3.34 | 3.45 | 3.45 | 4.61 | 4.63 | 4.82 | 6.49 | 8.19 |
| 15 | 4.11 | 4.11 | 4.16 | 4.06 | 3.56 | 4.71 | 4.84 | 6.14 | 8.09 |
| 14 | 4.59 | 4.61 | 4.59 | 4.47 | 4.15 | 4.69 | 4.81 | 6.34 | 8.02 |
| 13 | 5.11 | 5.08 | 4.96 | 4.90 | 4.52 | 4.76 | 4.82 | 6.03 | 7.47 |
| 12 | 3.12 | 3.16 | 5.01 | 4.89 | 4.51 | 4.41 | 4.40 | 5.96 | 7.08 |
| 11 | 3.41 | 3.27 | 2.09 | 4.31 | 3.90 | 3.54 | 3.45 | 4.91 | 6.15 |
| 10 | 3.16 | 3.26 | 3.27 | 1.89 | 3.63 | 3.53 | 3.28 | 5.08 | 6.04 |
| 9 | 1.98 | 2.15 | 2.24 | 3.68 | 2.48 | 4.43 | 3.66 | 4.51 | 5.56 |
| 8 | 2.24 | 2.29 | 2.42 | 1.83 | 2.97 | 3.43 | 3.48 | 4.24 | 5.59 |
| 7 | 1.64 | 1.67 | 1.77 | 2.07 | 1.85 | 2.45 | 3.49 | 4.70 | 5.49 |
| 6 | 1.19 | 1.24 | 1.32 | 1.83 | 2.23 | 2.91 | 3.59 | 4.78 | 5.91 |
| 5 | 1.10 | 1.20 | 1.29 | 1.55 | 1.97 | 2.50 | 3.96 | 5.17 | 5.61 |
| 4 | 1.11 | 1.18 | 1.30 | 1.55 | 2.09 | 3.00 | 4.31 | 6.73 | 6.82 |
| 3 | 1.09 | 1.18 | 1.33 | 1.60 | 2.23 | 3.02 | 4.99 | 9.30 | 9.03 |
| 2 | 1.10 | 1.21 | 1.40 | 1.76 | 2.42 | 4.43 | 8.19 | 11.80 | 8.09 |
| 1 | 1.09 | 1.24 | 1.41 | 1.85 | 2.73 | 5.00 | mask | mask | 9.70 |
| 0 | 1.14 | 1.26 | 1.56 | 2.14 | 3.47 | 8.54 | mask | mask | 5.46 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25} Without/With Local Allocators

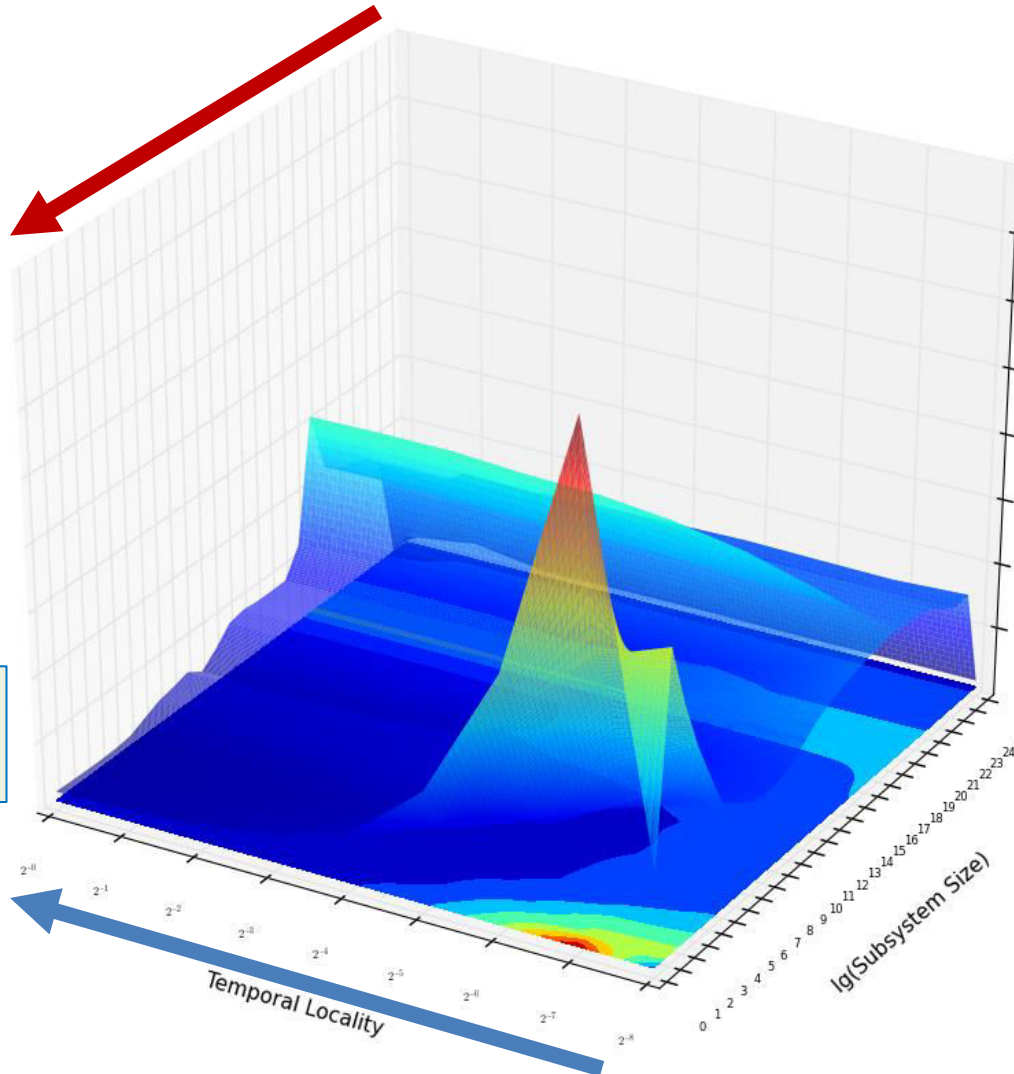
sf = 5

Diffusion

*Physical
Locality*

Max *Temporal
Locality* = 256

*Temporal
Locality*



30.0
25.0
20.0
15.0
10.0
5.0

*Degradation
Ratio (DR)*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25} **Without/With** Local Allocators

sf = 5
Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 25 | 0.97 | 1.77 | 0.97 | 1.02 | 1.04 | 0.99 | 0.96 | 1.01 | 1.00 |
| 24 | 0.50 | 8.26 | 8.17 | 8.38 | 8.43 | 8.52 | 8.40 | 8.30 | 8.57 |
| 23 | 8.30 | 8.41 | 8.30 | 8.35 | 8.40 | 8.36 | 8.36 | 8.37 | 8.44 |
| 22 | 9.53 | 9.57 | 9.40 | 9.43 | 9.41 | 9.65 | 9.42 | 9.41 | 9.04 |
| 21 | 9.99 | 10.00 | 10.00 | 9.87 | 9.98 | 10.20 | 9.90 | 9.88 | 9.93 |
| 20 | 10.40 | 10.30 | 10.30 | 10.20 | 10.20 | 10.20 | 10.20 | 10.30 | 10.30 |
| 19 | 11.20 | 11.30 | 11.20 | 11.00 | 11.00 | 10.90 | 10.70 | 10.50 | 10.40 |
| 18 | 15.90 | 16.00 | 16.00 | 15.60 | 15.40 | 14.80 | 13.90 | 12.30 | 10.60 |
| 17 | 6.58 | 6.70 | 6.73 | 6.87 | 7.06 | 7.50 | 8.19 | 9.30 | 10.50 |
| 16 | 4.53 | 4.57 | 4.56 | 4.76 | 5.04 | 5.56 | 6.47 | 8.11 | 10.30 |
| 15 | 4.51 | 4.56 | 4.62 | 4.73 | 4.99 | 5.52 | 6.38 | 7.86 | 10.10 |
| 14 | 4.51 | 4.54 | 4.62 | 4.72 | 4.98 | 5.43 | 6.28 | 7.70 | 9.75 |
| 13 | 4.64 | 4.67 | 4.73 | 4.82 | 5.07 | 5.49 | 6.31 | 7.56 | 9.34 |
| 12 | 4.38 | 4.38 | 4.48 | 4.58 | 4.80 | 5.18 | 5.86 | 7.10 | 8.78 |
| 11 | 3.16 | 3.19 | 3.27 | 3.42 | 3.67 | 4.15 | 4.90 | 6.25 | 7.88 |
| 10 | 2.18 | 2.25 | 2.37 | 2.58 | 2.91 | 3.39 | 4.28 | 5.48 | 7.00 |
| 9 | 2.95 | 3.04 | 3.17 | 3.32 | 3.59 | 4.08 | 4.42 | 5.57 | 6.63 |
| 8 | 2.60 | 2.62 | 2.80 | 3.00 | 3.40 | 3.84 | 4.40 | 5.42 | 6.50 |
| 7 | 2.36 | 2.51 | 2.65 | 2.95 | 3.31 | 3.83 | 4.49 | 5.45 | 6.79 |
| 6 | 1.82 | 1.99 | 2.26 | 2.62 | 3.10 | 3.74 | 4.59 | 5.97 | 7.62 |
| 5 | 1.27 | 1.40 | 1.64 | 2.05 | 2.64 | 3.42 | 4.65 | 6.67 | 8.21 |
| 4 | 1.13 | 1.22 | 1.42 | 1.76 | 2.32 | 3.18 | 4.79 | 8.02 | 11.30 |
| 3 | 1.09 | 1.21 | 1.39 | 1.75 | 2.37 | 3.49 | 6.03 | 11.40 | 14.50 |
| 2 | 1.11 | 1.22 | 1.45 | 1.86 | 2.66 | 4.51 | 9.49 | 18.30 | 18.40 |
| 1 | 1.14 | 1.29 | 1.54 | 1.98 | 3.10 | 5.76 | 15.30 | 21.20 | 23.40 |
| 0 | 1.19 | 1.38 | 1.70 | 2.50 | 4.18 | 8.99 | 19.30 | 39.20 | 7.66 |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data

Benchmark II: LOCALITY

System Size = 2^{25} **Without/With Local Allocators**

sf = 5
Diffusion

*Physical
Locality*

| | 2^{-0} | 2^{-1} | 2^{-2} | 2^{-3} | 2^{-4} | 2^{-5} | 2^{-6} | 2^{-7} | 2^{-8} |
|----|----------|----------|----------|----------|----------|----------|-------------|--------------|----------|
| 25 | 0.97 | 1.77 | 0.97 | 1.02 | 1.04 | 0.99 | 0.96 | 1.01 | 1.00 |
| 24 | 0.50 | 8.26 | 8.17 | 8.38 | 8.43 | 8.52 | 8.40 | 8.30 | 8.57 |
| 23 | 8.30 | 8.41 | 8.30 | 8.35 | 8.40 | 8.36 | 8.36 | 8.37 | 8.44 |
| 22 | 9.53 | 9.57 | 9.40 | 9.43 | 9.41 | 9.65 | 9.42 | 9.41 | 9.04 |
| 21 | 9.99 | 10.00 | 10.00 | 9.87 | 9.98 | 10.20 | 9.90 | 9.88 | 9.93 |
| 20 | 10.40 | 10.30 | 10.30 | 10.20 | 10.20 | 10.20 | 10.20 | 10.30 | 10.30 |
| 19 | 11.20 | 11.30 | 11.20 | 11.00 | 11.00 | 10.90 | 10.70 | 10.50 | 10.40 |
| 18 | 15.90 | 16.00 | 16.00 | 15.60 | 15.40 | 14.80 | 13.90 | 12.30 | 10.60 |
| 17 | 6.58 | 6.70 | 6.73 | 6.87 | 7.06 | 7.50 | 8.19 | 9.30 | 10.50 |
| 16 | 4.53 | 4.57 | 4.56 | 4.76 | 5.04 | 5.56 | 6.47 | 8.11 | 10.30 |
| 15 | 4.51 | 4.56 | 4.62 | 4.73 | 4.99 | 5.52 | 6.38 | 7.86 | 10.10 |
| 14 | 4.51 | 4.54 | 4.62 | 4.72 | 4.98 | 5.43 | 6.28 | 7.70 | 9.75 |
| 13 | 4.64 | 4.67 | 4.73 | 4.82 | 5.07 | 5.49 | 6.31 | 7.56 | 9.34 |
| 12 | 4.38 | 4.38 | 4.48 | 4.58 | 4.80 | 5.18 | 5.86 | 7.10 | 8.78 |
| 11 | 3.16 | 3.19 | 3.27 | 3.42 | 3.67 | 4.15 | 4.90 | 6.25 | 7.88 |
| 10 | 2.18 | 2.25 | 2.37 | 2.58 | 2.91 | 3.39 | 4.28 | 5.48 | 7.00 |
| 9 | 2.95 | 3.04 | 3.17 | 3.32 | 3.59 | 4.08 | 4.42 | 5.57 | 6.63 |
| 8 | 2.60 | 2.62 | 2.80 | 3.00 | 3.40 | 3.84 | 4.40 | 5.42 | 6.50 |
| 7 | 2.36 | 2.51 | 2.65 | 2.95 | 3.31 | 3.83 | 4.49 | 5.45 | 6.79 |
| 6 | 1.82 | 1.99 | 2.26 | 2.62 | 3.10 | 3.74 | 4.59 | 5.97 | 7.62 |
| 5 | 1.27 | 1.40 | 1.64 | 2.05 | 2.64 | 3.42 | 4.65 | 6.67 | 8.21 |
| 4 | 1.13 | 1.22 | 1.42 | 1.76 | 2.32 | 3.18 | 4.79 | 8.02 | 11.30 |
| 3 | 1.09 | 1.21 | 1.39 | 1.75 | 2.37 | 3.49 | 6.03 | 11.40 | 14.50 |
| 2 | 1.11 | 1.22 | 1.45 | 1.86 | 2.66 | 4.51 | 9.49 | 18.30 | 18.40 |
| 1 | 1.14 | 1.29 | 1.54 | 1.98 | 3.10 | 5.76 | mask | 23.40 | |
| 0 | 1.19 | 1.38 | 1.70 | 2.50 | 4.18 | 8.99 | | 7.66 | |

*Degradation
Ratio (DR)*

*Temporal
Locality*

3. Analyzing the Benchmark Data
Benchmark II: LOCALITY

Questions
and/or
Discussion?

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

I. Short Running: Build Up, Use, Tear Down

- Allocation **D**ENSITY and **V**ARIATION in Allocated Sizes

II. Long Running: Time-Multiplexed Subsystems

- Access **L**OCALITY – both *Physical* and *Temporal*

III. Short Running: Varying Memory Reusability

- Memory **U**TILIZATION

IV. Multithreaded: Varying Numbers of Threads

- Allocator **C**ONTENTION

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Considerations:

- Investigate memory **U**TILIZATION.
 - Focus on allocation/deallocation costs themselves.
- Access **L**OCALITY should NOT dominate results.
 - Write to just first byte of each newly allocated element.
- Identify sub-dimensions of $\mathbf{U} = \mathbf{M}/\mathbf{T}$
 - **T** is the total memory allocated.
 - **M** is the maximum concurrently active memory.
 - **S** is the (atomic) memory “chunk” size.

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Plan:

- Allocate chunks of memory of size S until memory of size M is concurrently allocated.
- Deallocate Least Recently Used chunk and reallocate it until the total memory of size T has been allocated.
- Deallocate the remaining allocated memory (of size M), one chunk (of size S) at a time.
- The results of this experiment are absolute runtimes.
 - The entries in each row, other than AS1, are relative to AS1.

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Two more Considerations:

- We chose to omit **ASs** that “winking-out” memory.
 - I.e., we omitted **AS4, AS6, AS8, AS10, AS12, and AS14**.
 - Virtually all of the memory deallocated individually.
 - (No mathematical possibility of any noticeable effect.)
- We anticipated trouble with any use of **monotonic**.
 - Total memory allocated (T) is large (2^{35} bytes).
 - Artificial limit of 2^{12} for pooled memory chunks (**AS6-AS14**).
 - Memory larger than that passes through to the backing allocator.

These
are all
exponents
of 2.

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

$$\text{Total Allocated Memory (T)} = 2^{30}$$

| Inputs | | | Global | Virtual | Monotonic | Virtual | Multipool | Virtual | Multi<Mono> | Virtual |
|--------|----|----|--------|---------|-----------|---------|-----------|---------|-------------|---------|
| T | M | S | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 30 | 15 | 10 | 0.063s | 103 | 440 | 435 | 46 | 43 | 46 | 47 |
| 30 | 16 | 10 | 0.069s | 102 | 401 | 395 | 42 | 42 | 41 | 45 |
| 30 | 17 | 10 | 0.064s | 110 | 435 | 428 | 46 | 44 | 47 | 46 |
| 30 | 18 | 10 | 0.063s | 102 | 440 | 434 | 46 | 39 | 54 | 47 |
| 30 | 19 | 10 | 0.063s | 104 | 439 | 434 | 51 | 46 | 47 | 47 |
| 30 | 20 | 10 | 0.064s | 110 | 433 | 430 | 46 | 42 | 46 | 52 |
| 30 | 20 | 11 | 0.035s | 125 | 758 | 747 | 54 | 37 | 49 | 37 |
| 30 | 20 | 12 | 0.022s | 101 | 1216 | 1206 | 51 | 31 | 52 | 32 |
| 30 | 20 | 13 | 0.013s | 60 | 1985 | 1961 | 110 | 67 | 1996 | 1979 |
| 30 | 20 | 14 | 0.008s | 77 | 3356 | 3304 | 110 | 58 | 3276 | 3314 |
| 30 | 20 | 15 | 0.004s | 74 | 5985 | 6288 | 60 | 111 | 6016 | 6057 |

Maximum Active Memory (M)

Size of Each Allocation (S)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Total Allocated Memory (T) = 2^{31}

| Inputs | | | Global | Virtual | Monotonic | Virtual | Multipool | Virtual | Multi<Mono> | Virtual |
|--------|----|----|--------|---------|-----------|---------|-----------|---------|-------------|---------|
| T | M | S | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 31 | 15 | 10 | 0.127s | 104 | 428 | 434 | 39 | 38 | 39 | 41 |
| 31 | 16 | 10 | 0.123s | 102 | 442 | 446 | 42 | 42 | 41 | 40 |
| 31 | 17 | 10 | 0.124s | 102 | 439 | 442 | 45 | 45 | 42 | 45 |
| 31 | 18 | 10 | 0.123s | 102 | 442 | 447 | 47 | 46 | 41 | 42 |
| 31 | 19 | 10 | 0.123s | 107 | 441 | 446 | 42 | 41 | 46 | 43 |
| 31 | 20 | 10 | 0.127s | 99 | 431 | 434 | 44 | 42 | 41 | 41 |
| 31 | 20 | 11 | 0.064s | 102 | 815 | 824 | 48 | 40 | 52 | 48 |
| 31 | 20 | 12 | 0.038s | 93 | 1369 | 1387 | 57 | 51 | 47 | 54 |
| 31 | 20 | 13 | 0.021s | 102 | 2368 | 2392 | 108 | 80 | 2376 | 2401 |
| 31 | 20 | 14 | 0.013s | 61 | 3787 | 3833 | 109 | 67 | 3797 | 3844 |
| 31 | 20 | 15 | 0.007s | 54 | 6621 | 6706 | 112 | 59 | 6651 | 6708 |

Maximum Active Memory (M)

Size of Each Allocation (S)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Total Allocated Memory (T) = 2^{32}

| Inputs | | | Global | Virtual | Monotonic | Virtual | Multipool | Virtual | Multi<Mono> | Virtual |
|--------|----|----|--------|---------|-----------|---------|-----------|---------|-------------|---------|
| T | M | S | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 32 | 15 | 10 | 0.248s | 103 | FAIL | FAIL | 38 | 39 | 38 | 41 |
| 32 | 16 | 10 | 0.248s | 102 | FAIL | FAIL | 38 | 41 | 38 | 39 |
| 32 | 17 | 10 | 0.246s | 102 | FAIL | FAIL | 40 | 39 | 39 | 39 |
| 32 | 18 | 10 | 0.246s | 102 | FAIL | FAIL | 40 | 40 | 39 | 40 |
| 32 | 19 | 10 | 0.246s | 102 | FAIL | FAIL | 40 | 42 | 40 | 40 |
| 32 | 20 | 10 | 0.246s | 102 | FAIL | FAIL | 40 | 41 | 41 | 41 |
| 32 | 20 | 11 | 0.124s | 102 | FAIL | FAIL | 46 | 44 | 41 | 47 |
| 32 | 20 | 12 | 0.062s | 102 | FAIL | FAIL | 44 | 45 | 46 | 56 |
| 32 | 20 | 13 | 0.034s | 108 | FAIL | FAIL | 127 | 110 | FAIL | FAIL |
| 32 | 20 | 14 | 0.022s | 72 | FAIL | FAIL | 105 | 78 | FAIL | FAIL |
| 32 | 20 | 15 | 0.015s | 87 | FAIL | FAIL | 99 | 60 | FAIL | FAIL |

Maximum Active Memory (M)

Size of Each Allocation (S)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Total Allocated Memory (T) = 2^{33}

| Inputs | | | Global | Virtual | Monotonic | Virtual | Multipool | Virtual | Multi<Mono> | Virtual |
|--------|----|----|--------|---------|-----------|---------|-----------|---------|-------------|---------|
| T | M | S | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 33 | 15 | 10 | 0.495s | 102 | FAIL | FAIL | 41 | 39 | 39 | 39 |
| 33 | 16 | 10 | 0.493s | 102 | FAIL | FAIL | 38 | 39 | 38 | 41 |
| 33 | 17 | 10 | 0.492s | 102 | FAIL | FAIL | 38 | 41 | 38 | 40 |
| 33 | 18 | 10 | 0.492s | 102 | FAIL | FAIL | 40 | 41 | 39 | 40 |
| 33 | 19 | 10 | 0.492s | 102 | FAIL | FAIL | 40 | 41 | 40 | 41 |
| 33 | 20 | 10 | 0.492s | 102 | FAIL | FAIL | 40 | 40 | 40 | 41 |
| 33 | 20 | 11 | 0.248s | 102 | FAIL | FAIL | 42 | 43 | 41 | 42 |
| 33 | 20 | 12 | 0.122s | 101 | FAIL | FAIL | 43 | 47 | 45 | 47 |
| 33 | 20 | 13 | 0.062s | 102 | FAIL | FAIL | 112 | 112 | FAIL | FAIL |
| 33 | 20 | 14 | 0.040s | 89 | FAIL | FAIL | 96 | 88 | FAIL | FAIL |
| 33 | 20 | 15 | 0.022s | 102 | FAIL | FAIL | 107 | 80 | FAIL | FAIL |

Maximum Active Memory (M)

Size of Each Allocation (S)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Total Allocated Memory (T) = 2^{34}

| Inputs | | | Global | Virtual | Monotonic | Virtual | Multipool | Virtual | Multi<Mono> | Virtual |
|--------|----|----|--------|---------|-----------|---------|-----------|---------|-------------|---------|
| T | M | S | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 34 | 15 | 10 | 0.990s | 103 | FAIL | FAIL | 41 | 39 | 41 | 39 |
| 34 | 16 | 10 | 0.986s | 102 | FAIL | FAIL | 38 | 39 | 38 | 40 |
| 34 | 17 | 10 | 0.985s | 102 | FAIL | FAIL | 38 | 39 | 39 | 40 |
| 34 | 18 | 10 | 0.984s | 102 | FAIL | FAIL | 40 | 40 | 39 | 40 |
| 34 | 19 | 10 | 0.983s | 102 | FAIL | FAIL | 40 | 41 | 40 | 40 |
| 34 | 20 | 10 | 0.984s | 102 | FAIL | FAIL | 40 | 41 | 40 | 41 |
| 34 | 20 | 11 | 0.494s | 102 | FAIL | FAIL | 42 | 42 | 41 | 42 |
| 34 | 20 | 12 | 0.241s | 102 | FAIL | FAIL | 43 | 42 | 47 | 44 |
| 34 | 20 | 13 | 0.120s | 107 | FAIL | FAIL | 114 | 113 | FAIL | FAIL |
| 34 | 20 | 14 | 0.064s | 102 | FAIL | FAIL | 117 | 112 | FAIL | FAIL |
| 34 | 20 | 15 | 0.038s | 96 | FAIL | FAIL | 103 | 95 | FAIL | FAIL |

Maximum Active Memory (M)

Size of Each Allocation (S)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Total Allocated Memory (T) = 2^{35}

| Inputs | | | Global | Virtual | Monotonic | Virtual | Multipool | Virtual | Multi<Mono> | Virtual |
|--------|----|----|--------|---------|-----------|---------|-----------|---------|-------------|---------|
| T | M | S | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 35 | 15 | 10 | 1.981s | 102 | FAIL | FAIL | 38 | 41 | 39 | 39 |
| 35 | 16 | 10 | 1.975s | 102 | FAIL | FAIL | 39 | 40 | 38 | 39 |
| 35 | 17 | 10 | 1.970s | 102 | FAIL | FAIL | 39 | 40 | 39 | 40 |
| 35 | 18 | 10 | 1.967s | 102 | FAIL | FAIL | 39 | 39 | 39 | 40 |
| 35 | 19 | 10 | 1.967s | 102 | FAIL | FAIL | 39 | 41 | 40 | 41 |
| 35 | 20 | 10 | 1.968s | 102 | FAIL | FAIL | 40 | 41 | 40 | 40 |
| 35 | 20 | 11 | 0.988s | 102 | FAIL | FAIL | 41 | 42 | 41 | 41 |
| 35 | 20 | 12 | 0.481s | 102 | FAIL | FAIL | 42 | 42 | 44 | 44 |
| 35 | 20 | 13 | 0.240s | 102 | FAIL | FAIL | 113 | 113 | FAIL | FAIL |
| 35 | 20 | 14 | 0.125s | 102 | FAIL | FAIL | 113 | 112 | FAIL | FAIL |
| 35 | 20 | 15 | 0.070s | 94 | FAIL | FAIL | 103 | 110 | FAIL | FAIL |

Maximum Active Memory (M)

Size of Each Allocation (S)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Questions
and/or
Discussion?

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

I. Short Running: Build Up, Use, Tear Down

- Allocation **D**ENSITY and **V**ARIATION in Allocated Sizes

II. Long Running: Time-Multiplexed Subsystems

- Access **L**OCALITY – both *Physical* and *Temporal*

III. Short Running: Varying Memory Reusability

- Memory **U**TILIZATION

IV. Multithreaded: Varying Numbers of Threads

- Allocator **C**ONTENTION

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Considerations:

- Investigate allocator **C**ONTENSION.
 - Focus on allocation/deallocation costs themselves.
- Access **L**OCALITY should NOT dominate results.
 - Increment just first byte of each newly allocated element.
- Identify sub-dimensions of **C**:
 - **C**: Expected number of concurrent allocations per thread.
 - **I**: Number of alloc/access/dealloc sequences per thread.
 - **S**: Atomic memory “chunk” size (in bytes).
 - **W**: Number of active threads.

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Plan:

- For each of W threads:
 - Start the thread.
- For a total of I iterations.
 - Allocate a chunk of memory of size S bytes.
 - Increment the first byte of the allocated memory.
 - Deallocate the chunk of memory (of size S).
 - Join all threads.
- The results of this experiment are absolute runtimes.
 - The entries in each row, other than AS1, are relative to AS1.

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Additional Considerations:

- The allocation **DENSITY (D)** is very high.
- Each thread has access to its own private unsynchronized allocator.
- No contention occurs unless the local allocator goes to its backing (e.g., global) allocator.
- Unlike other targeted benchmarks, this experiment doesn't vary **CONTENTION** over the range from 0 to 1.
 - **CONTENTION** was kept high (versus 0 for other benchmarks).
- # processors was greater than the max **W = 8**.

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{15}

Allocation Size (S) = 2^6

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|--------|-----|-----------|-----|-----------|-----|-------------|------|
| I | S | W | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 15 | 6 | 1 | 0.041s | 91 | 40 | 39 | 26 | 26 | 24 | 24 |
| 15 | 6 | 2 | 0.037s | 100 | 42 | 43 | 27 | 26 | 26 | 29 |
| 15 | 6 | 3 | 0.038s | 105 | 41 | 43 | 15 | 16 | 17 | 16 |
| 15 | 6 | 4 | 0.032s | 93 | 56 | 58 | 31 | 32 | 25 | 24 |
| 15 | 6 | 5 | 0.032s | 91 | 46 | 52 | 26 | 23 | 22 | 24 |
| 15 | 6 | 6 | 0.030s | 95 | 51 | 53 | 24 | 27 | 26 | 27 |
| 15 | 6 | 7 | 0.033s | 96 | 47 | 49 | 23 | 28 | 21 | 26 |
| 15 | 6 | 8 | 0.029s | 96 | 71 | 63 | 33 | 30 | 31 | 25 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{15}

Allocation Size (S) = 2^7

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|--------|-----|-----------|-----|-----------|-----|-------------|------|
| | | | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| I | S | W | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 15 | 7 | 1 | 0.023s | 100 | 114 | 116 | 44 | 47 | 47 | 48 |
| 15 | 7 | 2 | 0.043s | 101 | 46 | 69 | 26 | 26 | 26 | 26 |
| 15 | 7 | 3 | 0.041s | 103 | 51 | 68 | 25 | 25 | 22 | 25 |
| 15 | 7 | 4 | 0.033s | 121 | 78 | 95 | 26 | 19 | 20 | 23 |
| 15 | 7 | 5 | 0.031s | 102 | 81 | 86 | 20 | 26 | 26 | 25 |
| 15 | 7 | 6 | 0.032s | 99 | 84 | 84 | 18 | 23 | 19 | 25 |
| 15 | 7 | 7 | 0.029s | 114 | 111 | 110 | 23 | 27 | 21 | 31 |
| 15 | 7 | 8 | 0.029s | 117 | 114 | 120 | 27 | 35 | 31 | 29 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{15}

Allocation Size (S) = 2^8

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|--------|-----|-----------|-----|-----------|-----|-------------|------|
| I | S | W | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 15 | 8 | 1 | 0.043s | 101 | 87 | 89 | 23 | 23 | 22 | 23 |
| 15 | 8 | 2 | 0.042s | 102 | 61 | 59 | 23 | 23 | 27 | 26 |
| 15 | 8 | 3 | 0.046s | 90 | 85 | 111 | 23 | 25 | 24 | 25 |
| 15 | 8 | 4 | 0.040s | 84 | 100 | 98 | 18 | 18 | 19 | 22 |
| 15 | 8 | 5 | 0.028s | 136 | 190 | 200 | 30 | 30 | 30 | 38 |
| 15 | 8 | 6 | 0.024s | 125 | 209 | 201 | 33 | 33 | 31 | 29 |
| 15 | 8 | 7 | 0.033s | 108 | 162 | 162 | 24 | 29 | 26 | 26 |
| 15 | 8 | 8 | 0.031s | 114 | 184 | 188 | 34 | 33 | 36 | 42 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{16}

Allocation Size (S) = 2^8

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|--------|-----|-----------|-----|-----------|-----|-------------|------|
| I | S | W | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 16 | 8 | 1 | 0.085s | 97 | 109 | 107 | 23 | 23 | 23 | 23 |
| 16 | 8 | 2 | 0.091s | 101 | 104 | 106 | 22 | 21 | 22 | 21 |
| 16 | 8 | 3 | 0.093s | 100 | 105 | 104 | 22 | 21 | 21 | 21 |
| 16 | 8 | 4 | 0.097s | 94 | 93 | 121 | 20 | 20 | 18 | 17 |
| 16 | 8 | 5 | 0.078s | 118 | 108 | 130 | 24 | 18 | 17 | 18 |
| 16 | 8 | 6 | 0.059s | 87 | 138 | 136 | 21 | 26 | 22 | 26 |
| 16 | 8 | 7 | 0.063s | 93 | 137 | 135 | 17 | 27 | 21 | 20 |
| 16 | 8 | 8 | 0.057s | 109 | 162 | 164 | 29 | 28 | 28 | 26 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{17}

Allocation Size (S) = 2^8

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|--------|-----|-----------|-----|-----------|-----|-------------|------|
| I | S | W | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 17 | 8 | 1 | 0.090s | 100 | 206 | 206 | 45 | 42 | 42 | 42 |
| 17 | 8 | 2 | 0.179s | 101 | 107 | 106 | 22 | 22 | 22 | 22 |
| 17 | 8 | 3 | 0.179s | 101 | 104 | 104 | 22 | 23 | 22 | 22 |
| 17 | 8 | 4 | 0.209s | 109 | 89 | 70 | 16 | 15 | 11 | 11 |
| 17 | 8 | 5 | 0.177s | 100 | 85 | 78 | 12 | 15 | 15 | 15 |
| 17 | 8 | 6 | 0.108s | 142 | 147 | 178 | 27 | 28 | 25 | 25 |
| 17 | 8 | 7 | 0.140s | 85 | 116 | 132 | 24 | 22 | 22 | 22 |
| 17 | 8 | 8 | 0.118s | 100 | 142 | 150 | 22 | 21 | 25 | 26 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{18}

Allocation Size (S) = 2^8

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|--------|-----|-----------|-----|-----------|-----|-------------|------|
| I | S | W | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 18 | 8 | 1 | 0.177s | 109 | 177 | 177 | 45 | 45 | 45 | 46 |
| 18 | 8 | 2 | 0.339s | 100 | 95 | 95 | 24 | 24 | 24 | 24 |
| 18 | 8 | 3 | 0.333s | 102 | 99 | 95 | 24 | 25 | 24 | 25 |
| 18 | 8 | 4 | 0.304s | 98 | 93 | 93 | 24 | 21 | 26 | 21 |
| 18 | 8 | 5 | 0.311s | 94 | 97 | 86 | 22 | 24 | 25 | 20 |
| 18 | 8 | 6 | 0.276s | 95 | 118 | 122 | 16 | 17 | 18 | 17 |
| 18 | 8 | 7 | 0.297s | 79 | 109 | 108 | 18 | 18 | 21 | 18 |
| 18 | 8 | 8 | 0.219s | 114 | 176 | 186 | 26 | 21 | 21 | 23 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark IV: CONTENTION

Number of Iterations (I) = 2^{19}

Allocation Size (S) = 2^8

| Inputs | | | Global | | Monotonic | | Multipool | | Multi<Mono> | |
|--------|---|---|---------|-----|-----------|-----|-----------|-----|-------------|------|
| I | S | W | Virtual | | Virtual | | Virtual | | Virtual | |
| | | | AS1 | AS2 | AS3 | AS5 | AS7 | AS9 | AS11 | AS13 |
| 19 | 8 | 1 | 0.421s | 89 | 134 | 134 | 28 | 23 | 21 | 25 |
| 19 | 8 | 2 | 0.615s | 101 | 93 | 93 | 25 | 26 | 26 | 26 |
| 19 | 8 | 3 | 0.631s | 99 | 93 | 93 | 25 | 25 | 25 | 25 |
| 19 | 8 | 4 | 0.565s | 107 | 95 | 103 | 28 | 28 | 29 | 28 |
| 19 | 8 | 5 | 0.575s | 119 | 106 | 101 | 27 | 28 | 27 | 27 |
| 19 | 8 | 6 | 0.499s | 114 | 126 | 113 | 17 | 25 | 28 | 22 |
| 19 | 8 | 7 | 0.558s | 100 | 113 | 115 | 18 | 18 | 15 | 16 |
| 19 | 8 | 8 | 0.460s | 105 | 149 | 148 | 19 | 21 | 18 | 21 |

Number of Active Threads (W)

3. Analyzing the Benchmark Data

Benchmark III: UTILIZATION

Questions
and/or
Discussion?

3. Analyzing the Benchmark Data

Another Use For Local Allocators

- <http://www.drdoobs.com/parallel/eliminate-false-sharing/217500206?pgno=1#>

The Little Parallel Counter That Couldn't

Consider this sequential code to count the number of odd numbers in a matrix:

If our job is to parallelize existing code, this is just what the doctor ordered: An embarrassingly parallel problem where it should be trivial to achieve linear speedups simply by assigning $1/P$ -th of the independent workload to each of P parallel workers. Here's a simple way to do it:

Quick: How well would you expect Example 1 to scale as P increases from 1 to the available hardware parallelism on the machine?

```
1      int odds = 0;
2      for( int i = 0; i < DIM; ++i )
3          for( int j = 0; j < DIM; ++j )
4              if( matrix[i*DIM + j] % 2 != 0 )
5                  ++odds;
```

3. Analyzing the Benchmark Data

Another Use For Local Allocators

```
1 // Example 1: Simple parallel version (flawed)
2 //
3 int result[P];
4 // Each of P parallel workers processes 1/P-th
5 // of the data; the p-th worker records its
6 // partial count in result[p]
7 for( int p = 0; p < P; ++p )
8     pool.run( [&,p] {
9         result[p] = 0;
10        int chunkSize = DIM/P + 1;
11        int myStart = p * chunkSize;
12        int myEnd = min( myStart+chunkSize, DIM );
13        for( int i = myStart; i < myEnd; ++i )
14            for( int j = 0; j < DIM; ++j )
15                if( matrix[i*DIM + j] % 2 != 0 )
16                    ++result[p];
17    });
18 // Wait for the parallel work to complete...
19 pool.join();
20 // Finally, do the sequential "reduction" step
21 // to combine the results
22 odds = 0;
23 for( int p = 0; p < P; ++p )
24     odds += result[p];
```

3. Analyzing the Benchmark Data

Another Use For Local Allocators

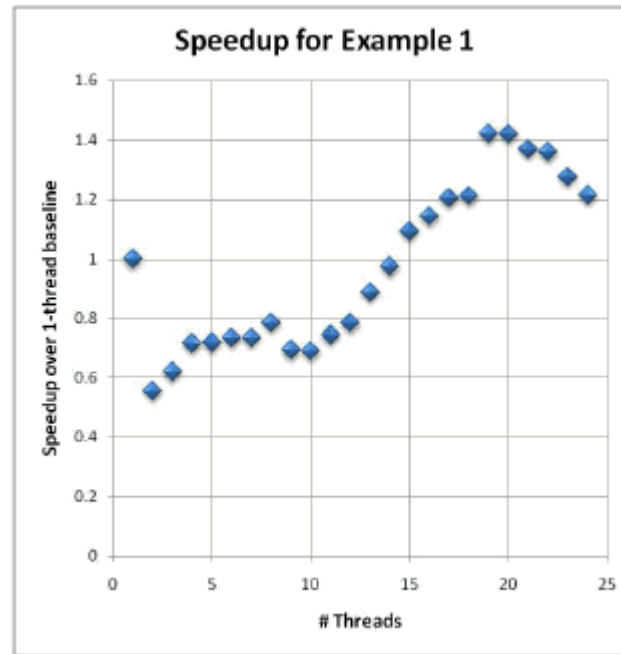


Figure 1: Example 1 seems to be about how to use more cores to get less total work done.

3. Analyzing the Benchmark Data

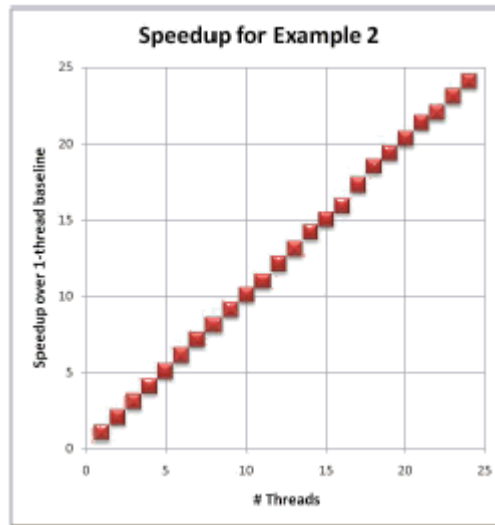
Another Use For Local Allocators

```
1 // Example 2: Simple parallel version
2 // (de-flawed using a local variable)
3 //
4 int result[P];
5
6 // Each of P parallel workers processes 1/P-th
7 // of the data; the p-th worker records its
8 // partial count in result[p]
9 for( int p = 0; p < P; ++p )
10     pool.run( [&,p] {
11         <font color="#FF0000">int count = 0;</font>
12         int chunkSize = DIM/P + 1;
13         int myStart = p * chunkSize;
14         int myEnd = min( myStart+chunkSize, DIM );
15         for( int i = myStart; i < myEnd; ++i )
16             for( int j = 0; j < DIM; ++j )
17                 if( matrix[i*DIM + j] % 2 != 0 )
18                     <font color="#FF0000">++count;
19         result[p] = count;</font>
20     });
21 // ... etc. as before ...
```

3. Analyzing the Benchmark Data

Another Use For Local Allocators

Figure 4: Removing cache line contention on the result array takes us from zero scaling to linear scaling, up to the available hardware parallelism (test run on a 24-core machine).



3. Analyzing the Benchmark Data

Houston, we have a problem!

But there was a problem...

- Some of the original data was unexplainable.
- We needed a strategy to understand why.
- More work was needed.
- We needed to “confirm” the data!
- How we solved the problem (next slide):
 - A revised paper: **Doc No:** P0089R1
 - A new paper: **Doc No:** P0213R0

3. Analyzing the Benchmark Data

The Solution: Graham Bleaney

Enter Graham as Co-Op at Bloomberg (May, 2014).

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- From P0089R1:

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- From P0089R1:

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- *New allocator-use dimension, **F** FRAGMENTABILITY (**F**):*

3. Analyzing the Benchmark Data

The Solution: Graham Bleaney

Enter Graham as Co-Op at Bloomberg (May, 2014).

- From P0089R1: **Joins us as FTE (Summer, 2017)!**

“... a separate effort has recently been made to recreate our experiments in order to confirm these results (P0213 by Graham Bleaney). We anticipate that paper will appear at approximately the same time as this revision.”

- ***New allocator-use dimension, FRAGMENTABILITY (F):***
“A measure of the potential of a subsystem’s allocated memory to become diffused throughout physical memory, as a result of the interference of other subsystems’ memory allocation. If a subsystem is fragmentable (i.e., other subsystems are present in the process and the subsystem allocates more than one chunk of memory), (F) is greater than zero.”

3. Analyzing the Benchmark Data

The C++ Standardization Process

C++ Standards Committee Meeting

- Jacksonville, Florida.
 - February 29 thru March 5, 2016.
- Graham presents his findings to the LEWG.
- Polymorphic Memory Resources (PMR) was adopted into C++17 on March 5, 2016!
 - Along with **both** of **our** local (“arena”) allocators:
 - **Monotonic**
 - **Multipool**

3. Analyzing the Benchmark Data

References

- **References**
- [1] The Bloomberg BDE Library [open source distribution](https://github.com/bloomberg/bde), <https://github.com/bloomberg/bde>
- [2] John Lakos, *Large Scale C++ Software Design*, Addison-Wesley, 1996.
- [3] Pablo Halpern, *N3916: Polymorphic Memory Resources*.
- [4] Memory Allocator Benchmark [Data](https://github.com/bloomberg/bde-allocator-benchmarks), <https://github.com/bloomberg/bde-allocator-benchmarks>
- [5] Graham Bleaney, *P0213R0: Reexamining the Performance of Memory-Allocation Strategies*.
- [6] John Lakos, Jeffrey Mendelsohn, Alisdair Meredith, Nathan Myers, *P0089R1: On Quantifying Memory-Allocation Strategies (Revision 2)*.

3. Analyzing the Benchmark Data

References

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Outline

1. Introduction and Background

What are memory allocators, and why are they useful?

2. Understanding the Problem

What aspects of software affect allocation strategy?

3. Analyzing the Benchmark Data

When and how do you use which allocator, and why?

4. Conclusions

What must we remember about memory allocators?

Outline

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4. Conclusion

Important Recurring Questions

Are memory
allocators really
worth the trouble?

4. Conclusion

What situations merit their use?

There are a few qualitatively different use cases:

A. To improve and/or preserve performance:

- Ensure physical locality of allocated memory.
- Avoid memory diffusion in long-running systems.
- Obviate deallocation of individual objects.
- Sidestep contention during concurrent allocations.
- Separate unrelated data to avoid false sharing.
- Compose effective allocation strategies.

4. Conclusion

What situations merit their use?

There are a few qualitatively different use cases:

B. To place objects in a specific kind of memory:

- Static memory
- Memory-mapped memory
- Read/write protectable memory
- Fast memory (special architectures)
- Shared memory (special allocators)

4. Conclusion

What situations merit their use?

There are a few qualitatively different use cases:

C. To measure, test, control, or debug memory:

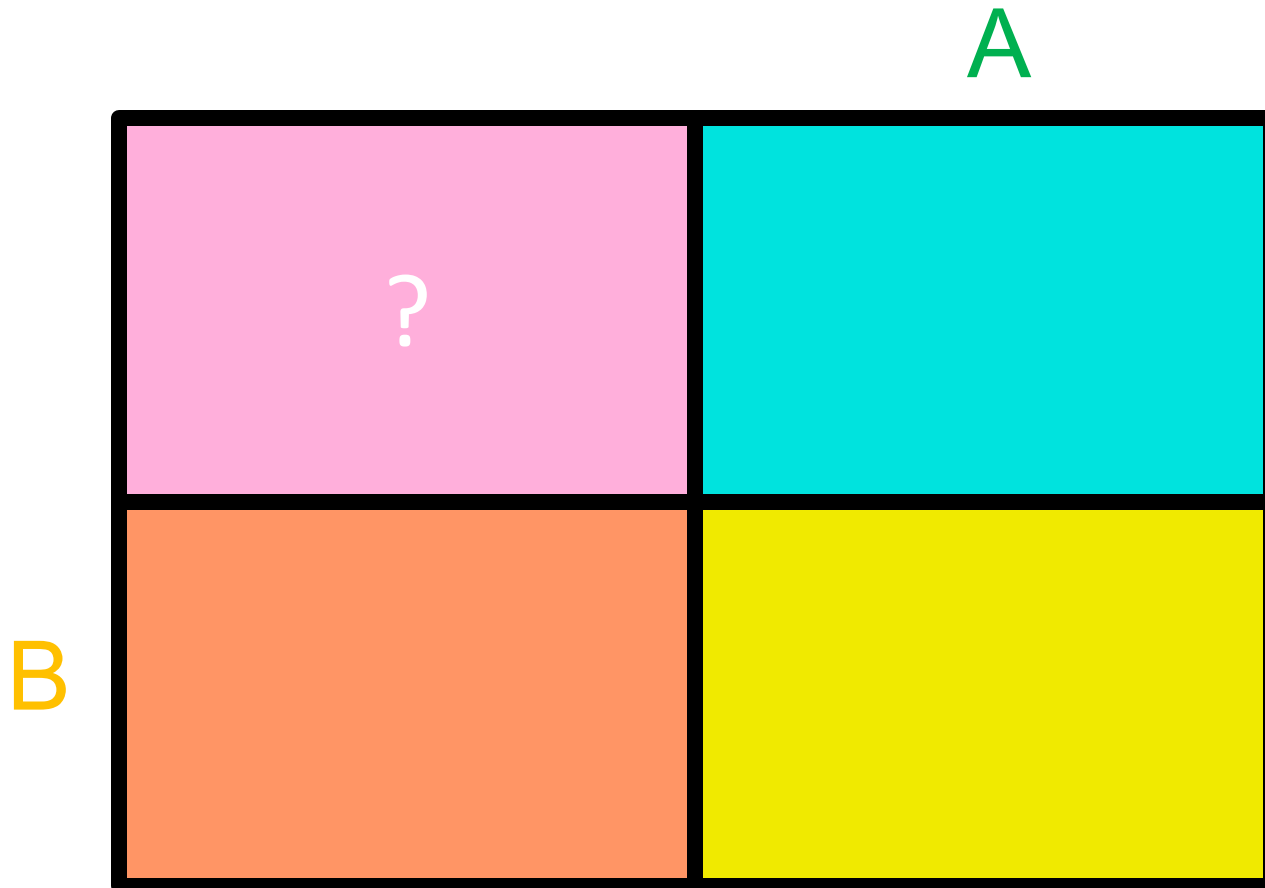
- Counting (auditing) allocator
- Test allocator
- Limit allocator
- Read/write protectable memory allocator

4. Conclusion

How are they applied effectively?

A: Program is large, long running.

B: Subsystems are accessed disproportionately often (L).

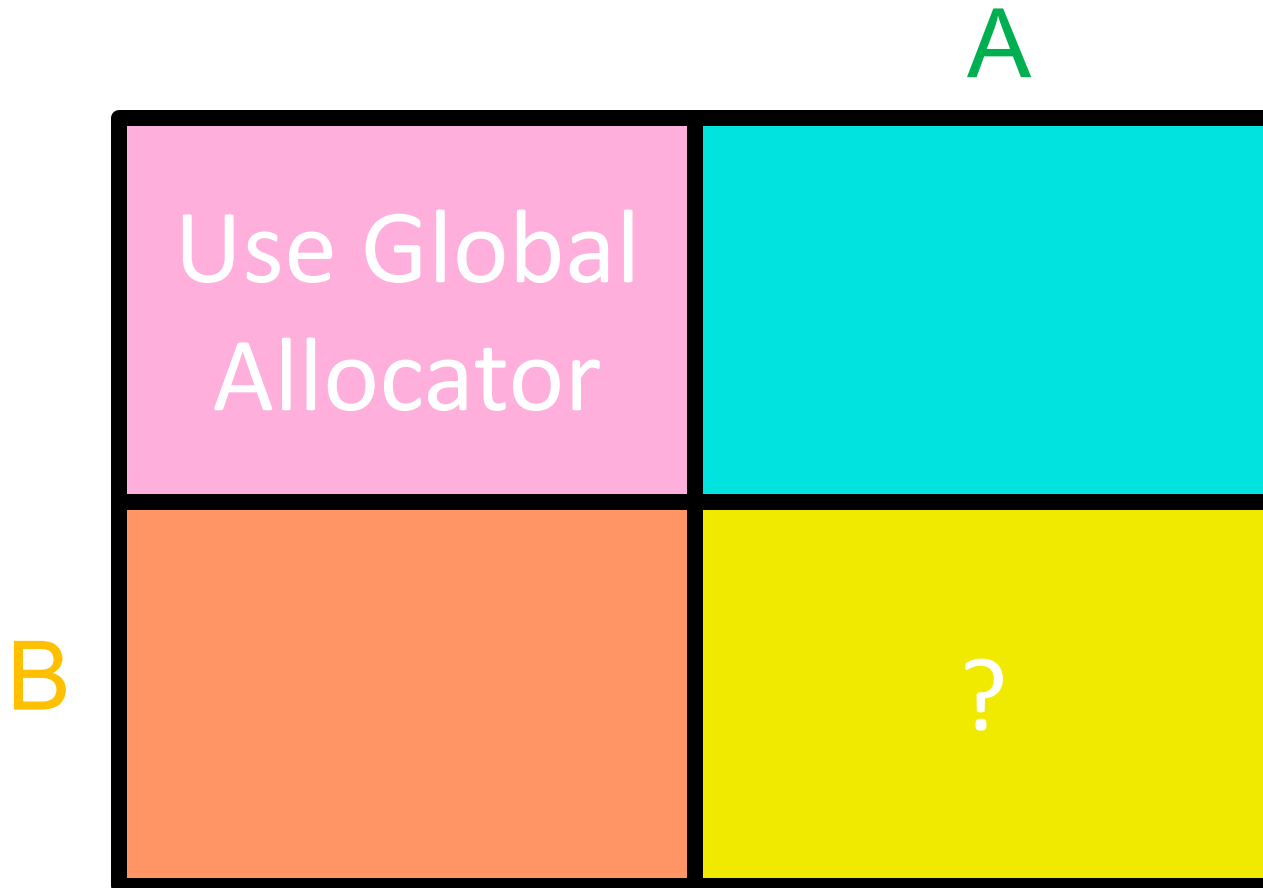


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| | | |
|---|------------------------------|------------------------------|
| | Use Global Allocator | ? |
| B | Use <u>Local</u> Allocators? | Use <u>Local</u> Allocators! |

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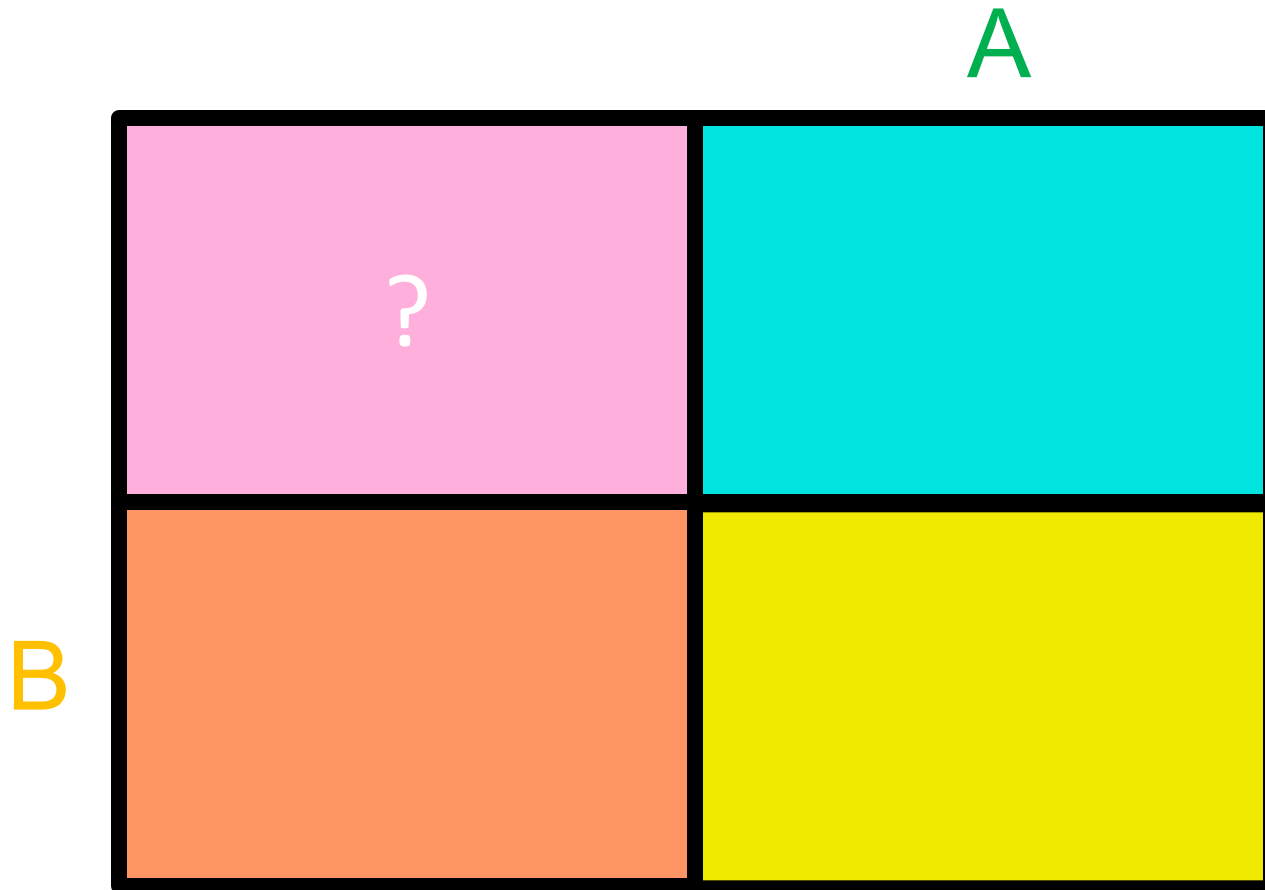
| | | |
|----------|------------------------------|-------------------------------------|
| | Use Global Allocator | Find a <u>new Job!</u> |
| B | Use <u>Local</u> Allocators? | Use <u>Local</u> Allocators! |

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How are they applied effectively?

A: Program is large, long running.

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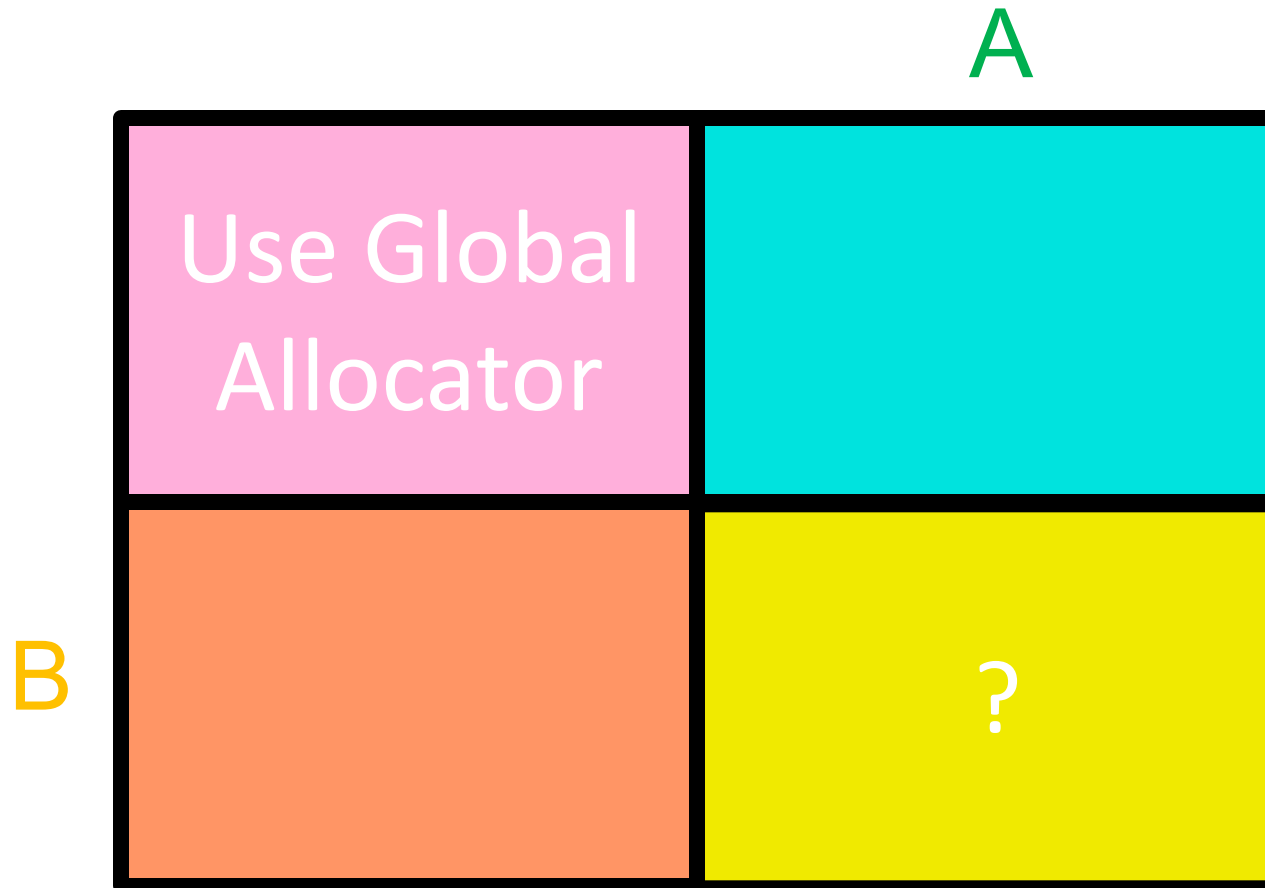


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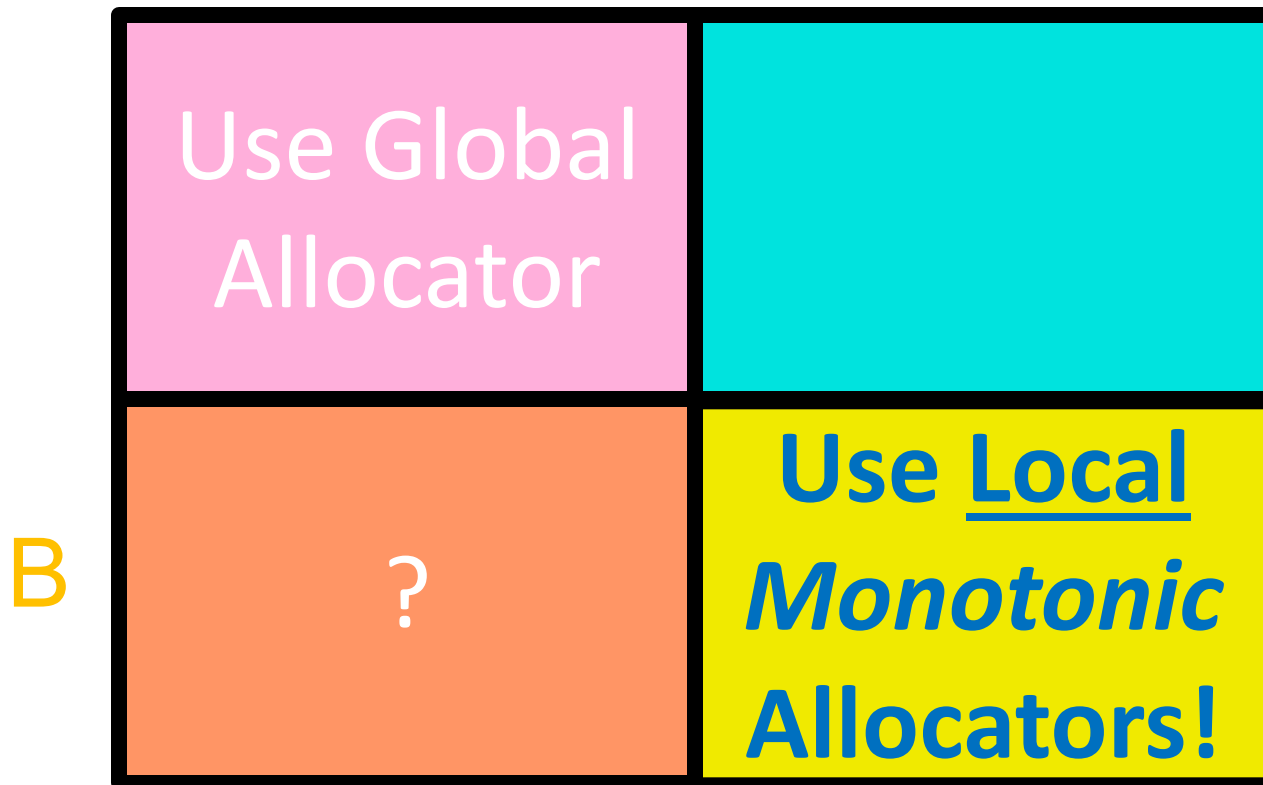
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| | | |
|---|--|--|
| | Use Global Allocator | ? |
| B | Use <u>Local Monotonic</u> Allocators? | Use <u>Local Monotonic</u> Allocators! |

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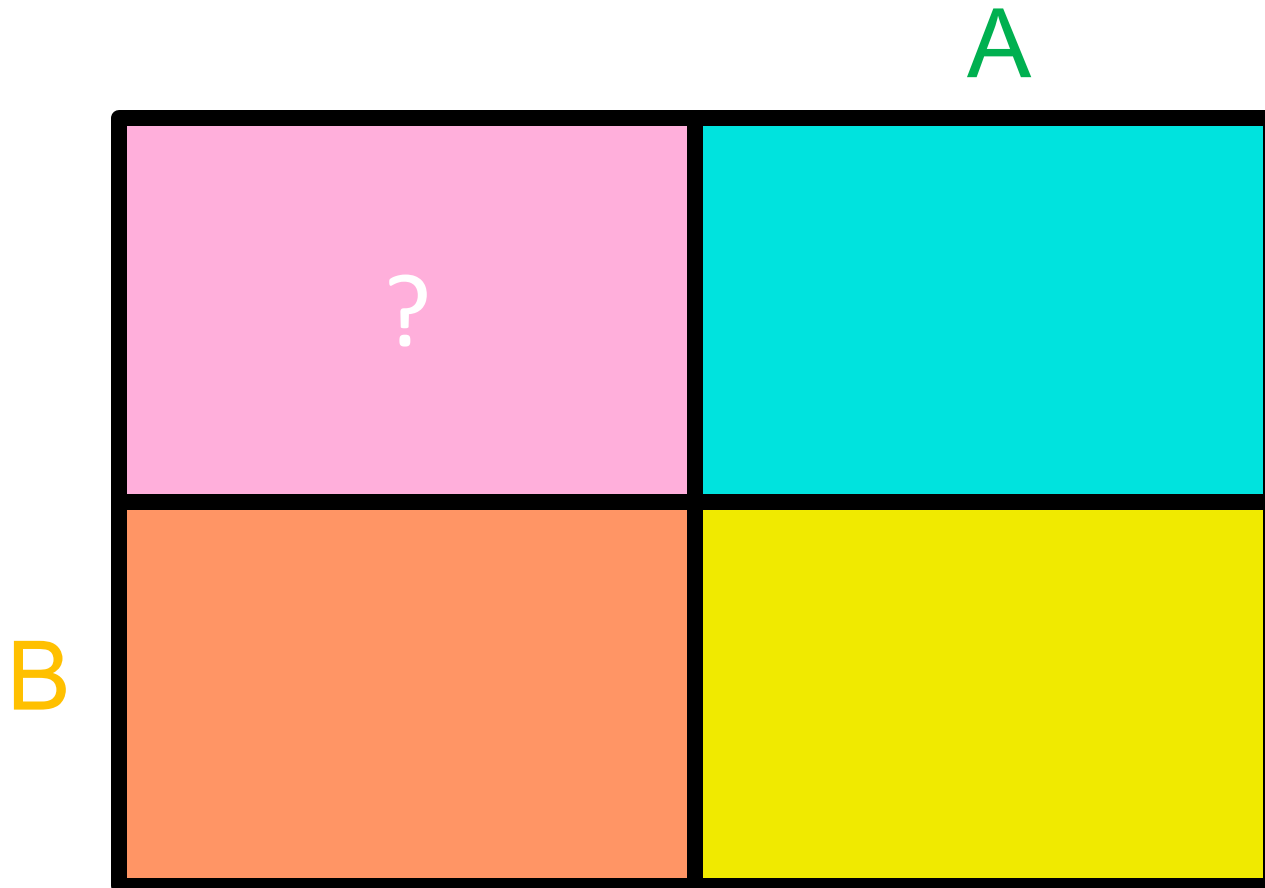
| | | |
|----------|--|---|
| | Use Global Allocator | Use <u>Local</u> Multipool Allocators! |
| B | Use <u>Local</u> Monotonic Allocators? | Use <u>Local</u> Monotonic Allocators! |

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How are they applied effectively?

A: Program is large, long running.

B: Subsystems run concurrently (C).

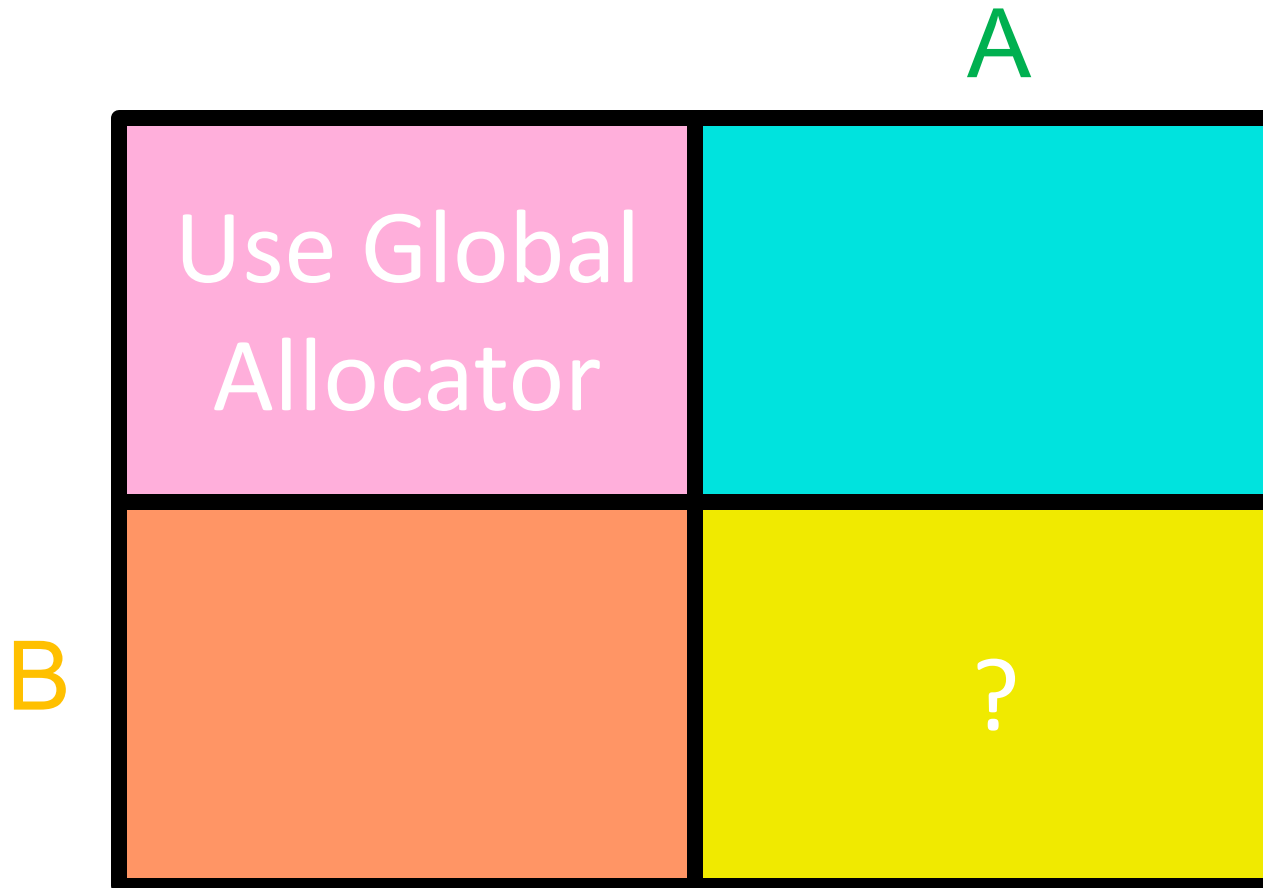


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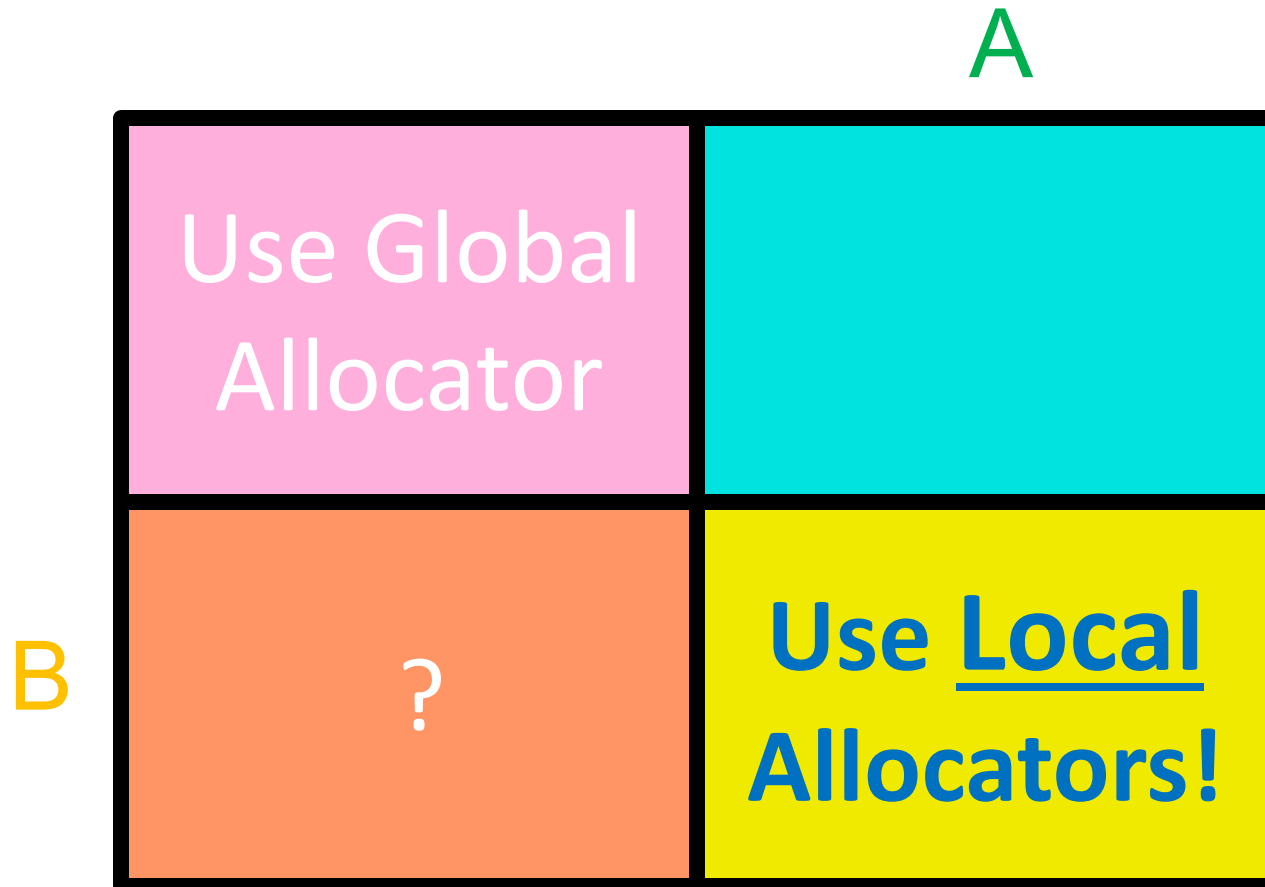


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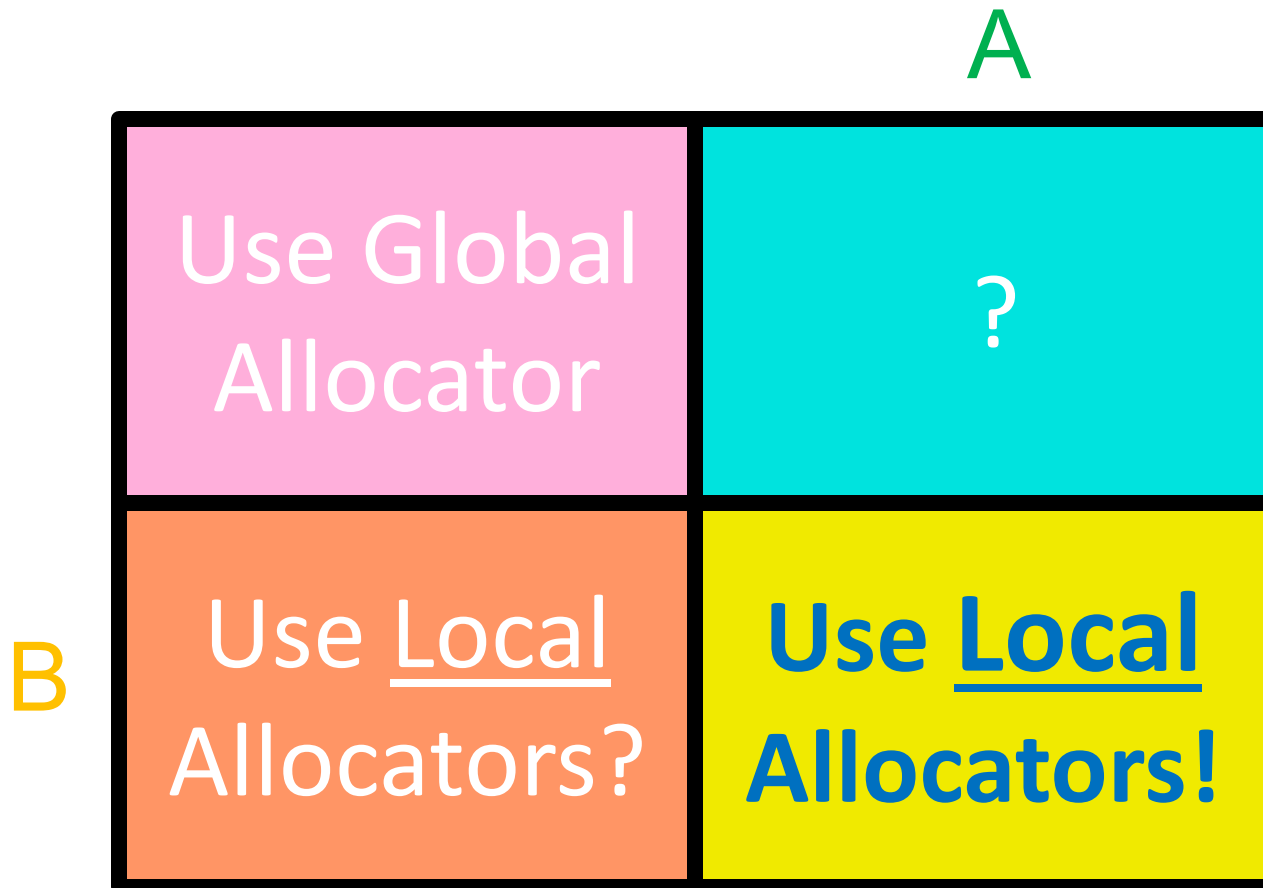


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A

| | | |
|---|------------------------------|------------------------------|
| | Use Global Allocator | Use <u>Local</u> Allocators! |
| B | Use <u>Local</u> Allocators? | Use <u>Local</u> Allocators! |

4. Conclusion

What's the performance impact?

The performance impact can be substantial:

1. In every benchmark, use of some (if not all) of the **local allocators** performed *no worse*, and typically *much better* than the default allocator.
2. For long-running programs, **improvements** of as much as an *order of magnitude* were observed.
3. The **overhead** of using the **virtual-function** interface and (in the default case) holding an **extra address** was *minimal to non-existent*.

4. Conclusion

Final Thoughts

Object-level control over memory allocation is intrinsic to C++, and must always be so if we hope to maintain this language's supremacy as the best-performing high-level "systems" language.

4. Conclusion

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Supporting object-specific memory allocation is admittedly an added burden – exacerbated by an initially difficult-to-use model – which is finally being addressed in C++17 by *Polymorphic Memory Resources*.

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Object-level control over memory allocation is intrinsic to C++, and must always be so if we hope to maintain this language's supremacy as the best-performing high-level "systems" language.

Supporting object-specific memory allocation is admittedly an added burden – exacerbated by an initially difficult-to-use model – which is finally being addressed in C++17 by *Polymorphic Memory Resources*. Any future incarnation of STL should incorporate the lessons elucidated here.

4. Conclusion

The End

DENSITY
VARIATION
LOCALITY
UTILIZATION
CONTENTION

D V L U C

4. Conclusion

The End

F* **D V L U C**

RAGMENTABILITY
DENSITY
VARIATION
LOCALITY
UTILIZATION
CONTENTION

* Graham Bleaney

4. Conclusion

The End

RAGMENTABILITY
ENSITY
ARIATION
OCALITY
TILIZATION
ONTENTION

F* DVLU C!

* Graham Bleaney

**But don't
mess with
the duck!**