



Enabling Science

ACCU
2012

Variance in Generic Types in Java and C#

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Variance in Generic Types in Java and C#

List<Cat>

Variance in Generic Types in Java and C#

List<? extends Cat>



List<? super Cat>

```
interface List<out T>
{
    ...
}
```

```
interface Collector<in T>
{
    ...
}
```



Variance in Generic Types in Java and C#

```
package java.util;
public class Collections {

    public static <T>
    int binarySearch(
        List<? extends Comparable<? super T>> list,
        T key)
    {...}
}
```

Variance in Generic Types in Java and C#

- ▶ What do they mean?
- ▶ What problem do they solve?
- ▶ Why do they look so different in Java and C#?

```
List<? extends Cat>
```

```
List<? super Cat>
```

```
interface List<out T>
```

```
{
```

```
interface Collector<in T>
```

```
{
```

```
...
```

```
}
```

Motivation for Covariance

- ▶ If an API expects a cat ...

```
void writeToXml(Cat cat);
```

- ▶ ... then we can give it a tiger.

```
Tiger tiger = ...;  
writeToXml(tiger);
```

Motivation for Covariance

- ▶ If an API expects a list of cats ...

```
void writeToXml(List<Cat> cats);
```

- ▶ ... then we'd expect it to accept a list of tigers ...

```
List<Tiger> tigers = ...;  
writeToXml(tigers);
```

Motivation for Covariance

- ▶ If an API expects a list of cats ...

```
void writeToXml(List<Cat> cats);
```

- ▶ ... then we'd expect it to accept a list of tigers ...

```
List<Tiger> tigers = ...;  
writeToXml(tigers);
```

- ▶ ... but it doesn't.

Why not?

Motivation for Covariance

- ▶ Expect an implementation like this ...

```
void writeToXml(List<Cat> cats)
{
    foreach (Cat cat in cats)
        process(cat);
}
```

```
List<Tiger> tigers = ...;
writeToXml(tigers);
```

Motivation for Covariance

- ▶ ... but it could be this ...

```
void writeToXml(List<Cat> cats)
{
    cats.add(new Lion());
}
```

```
List<Tiger> tigers = ...;
writeToXml(tigers);
```

Motivation for Covariance

- ▶ ... but it could be this ...

```
void writeToXml(List<Cat> cats)
{
    cats.add(new Lion());
}
```

- ▶ ... which would cause a type violation.

```
List<Tiger> tigers = ...;
writeToXml(tigers);
tigers.get(n).countStripes();
```


Motivation for Covariance

- ▶ We want to declare that `List<Tiger>` subtypes `List<Cat>`

```
void writeToXml(List<Cat> cats)
{
    foreach (Cat cat in cats)
        process(cat);
}
```

```
void writeToXml(List<Cat> cats)
{
    cats.add(new Lion());
}
```

```
List<Tiger> tigers = ...;
writeToXml(tigers);
```



Motivation for Contravariance

- ▶ We want to declare that `Collector<Cat>` subtypes `Collector<Tiger>`

```
void donateMyTigers(Collector<Tiger> tigerCollector)
{
    foreach (Tiger tiger in this.tigers)
        tigerCollector.accept(tiger);
}
```

```
void donateMyTigers(Collector<Tiger> tigerCollector)
{
    Tiger tiger = tigerCollector.mostRecentItem();
    tiger.countStripes();
}
```

```
Collector<Cat> catCollector = ...;
catCollector.accept(new Lion());
```

```
donateMyTigers(catCollector);
```



Covariance in Traditional Java/C#

Covariance in Traditional Java/C#

- ▶ Tiger[] convertible to Cat[]

```
void writeToXml(Cat[] cats)
{
    for (int i = 0; i < cats.Length; i ++
        process(cats[i]);
}
```

```
void writeToXml(Cat[] cats)
{
    cats[0] = new Lion();
}
```

```
Tiger[] tigers = ...;
writeToXml(tigers);
```



Covariance in Traditional Java/C#

- ▶ Tiger[] convertible to Cat[]
- ▶ Not statically type-safe – check at run-time

```
void writeToXml(Cat[] cats)
{
    for (int i = 0; i < cats.Length; i ++
        process(cats[i]);
}
```

```
void writeToXml(Cat[] cats)
{
    cats[0] = new Lion();
}
```

ArrayTypeMismatchException

```
Tiger[] tigers = ...;
writeToXml(tigers);
```



Covariance in Traditional Java/C#

- ▶ Tiger[] convertible to Cat[]
- ▶ Not statically type-safe – check at run-time

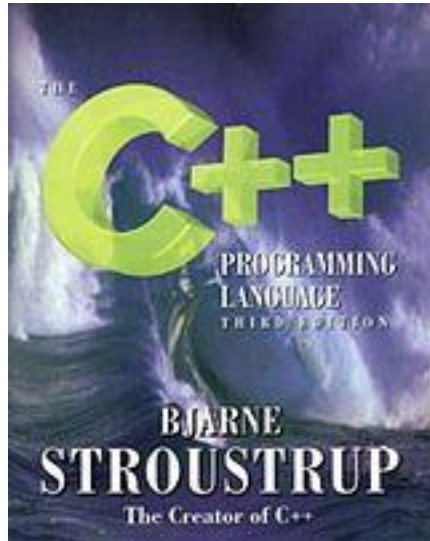
```
void writeToXml(Cat[] cats)
{
    for (int i = 0; i < cats.Length; i ++
        process(cats[i]);
}
```

```
void writeToXml(Cat[] cats)
{
    cats[0] = new Lion();
}
```

ArrayTypeMismatchException
ArrayStoreException

```
Tiger[] tigers = ...;
writeToXml(tigers);
```





Covariance in C++

Covariance in C++

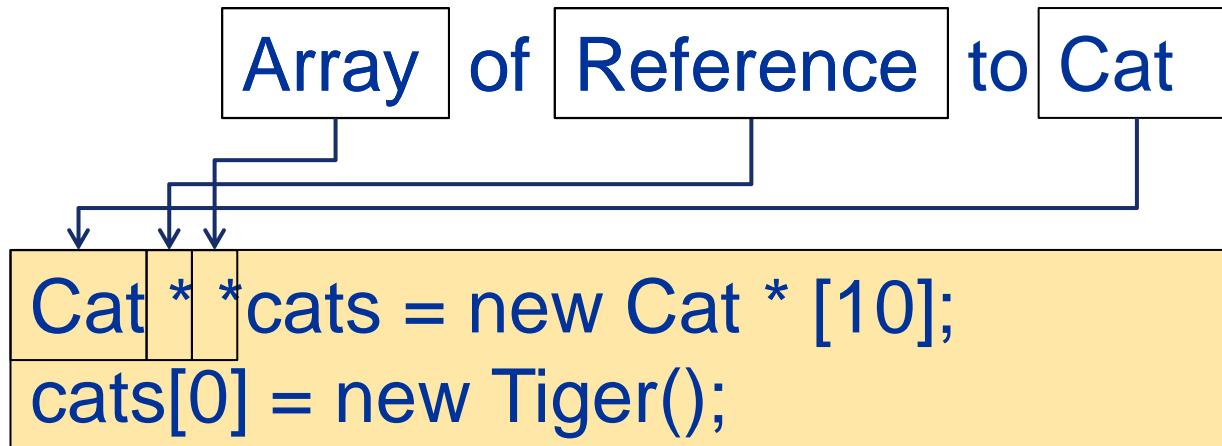
- ▶ C++ templates are always non-variant

```
std::list<Tiger *>
```

```
std::list<Cat *>
```

Covariance in C++

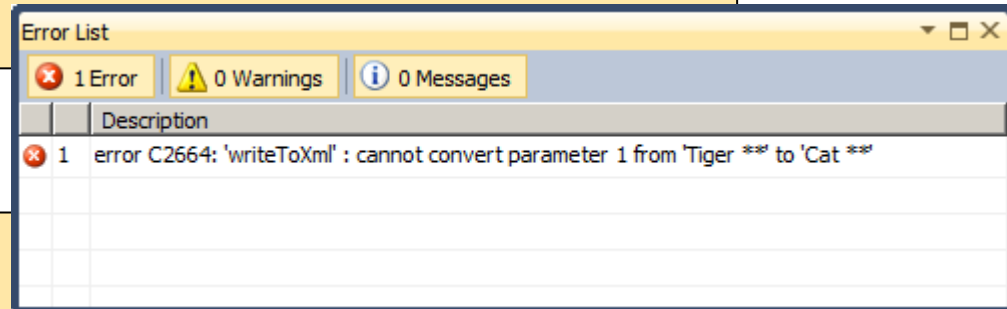
- ▶ Pointers to pointers



Covariance in C++

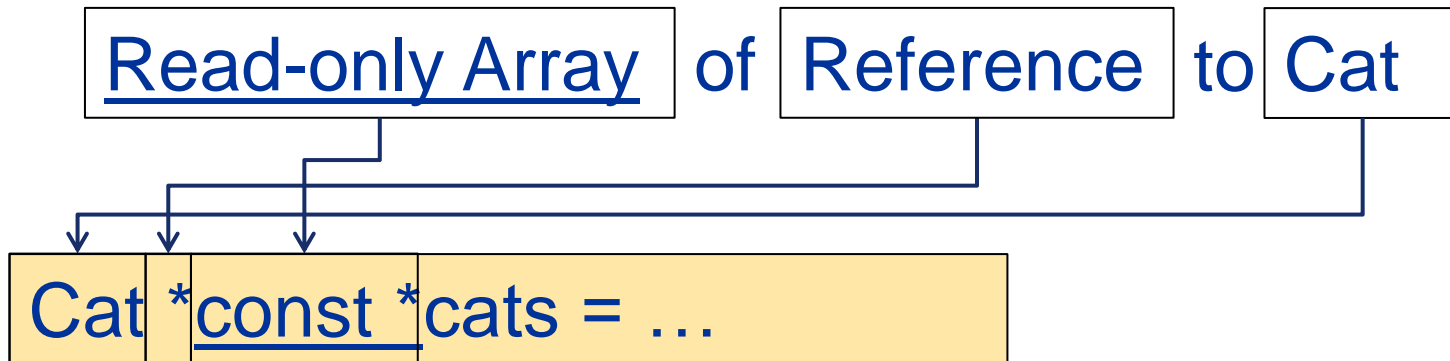
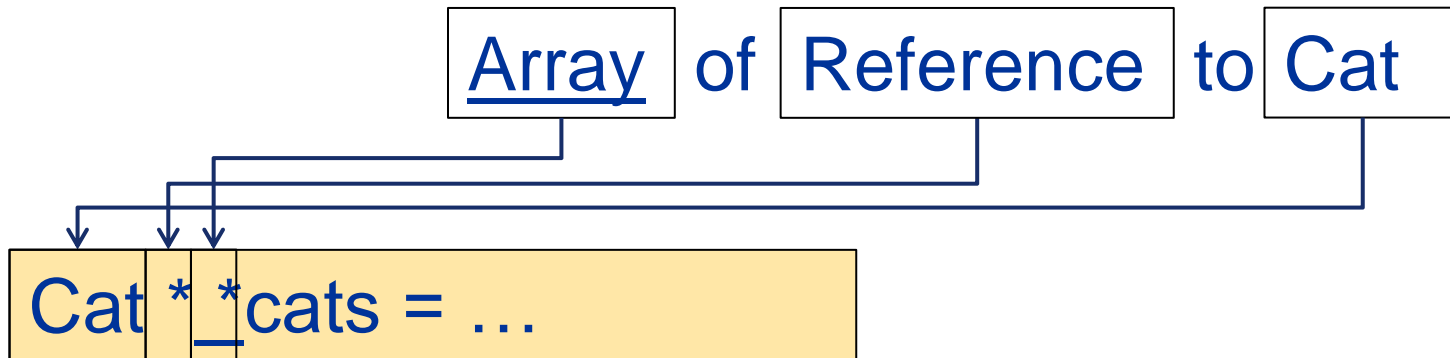
- ▶ 'T * *' is not covariant

```
void writeToXml(Cat * *cats, size_t num)
{
    cats[0] = new Lion();
}
```



```
Tiger * *tigers = ...;
writeToXml(tigers, numTigers);
tigers[0]->countStripes();
```

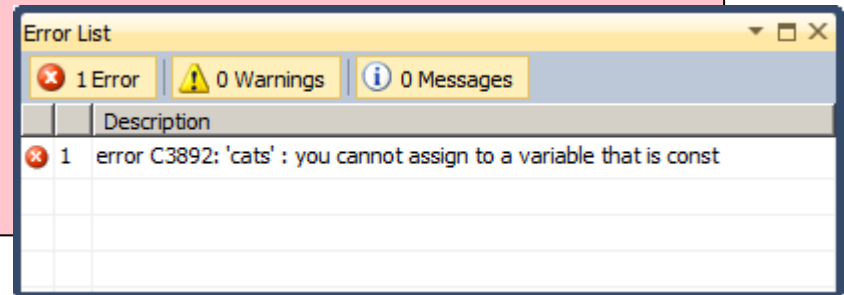
Covariance in C++



Covariance in C++

- ▶ 'T *const *' should be covariant ...

```
void writeToXml(Cat *const *cats, size_t num)
{
    cats[0] = new Lion();
}
```



```
Tiger *const *tigers = ...;
writeToXml(tigers, numTigers);
tigers[0]->countStripes();
```



Covariance in C++

- ▶ 'T *const *' should be covariant ...

```
void writeToXml(Cat *const *cats, size_t num)
{
    for (size_t j = 0; j < num; j++)
    {
        Cat *cat = cats[j];
        process(cat);
    }
}
```

```
Tiger *const *tigers = ...;
writeToXml(tigers, numTigers);
```

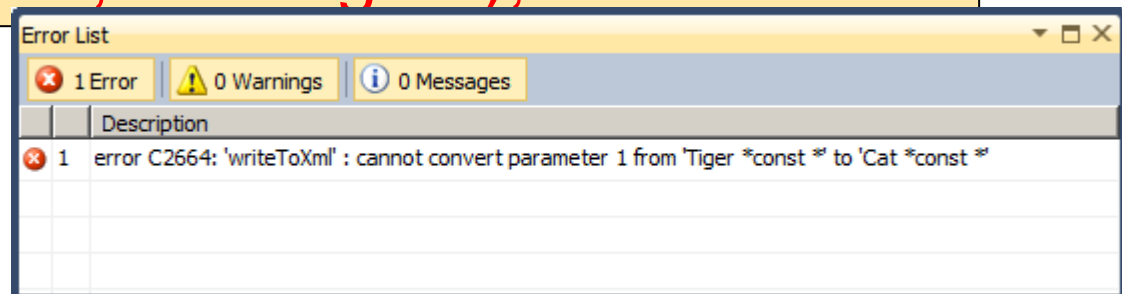

Covariance in C++

- ▶ 'T *const *' should be covariant ...

```
void writeToXml(Cat *const *cats, size_t num);
```

- ▶ ... but it isn't.

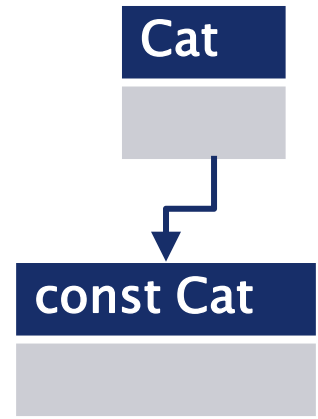
```
Tiger *const *tigers = ...;  
writeToXml(tigers, numTigers);
```



Covariance in C++

Read-only Array of Reference to Cat

```
Cat *const *cats = ...
```



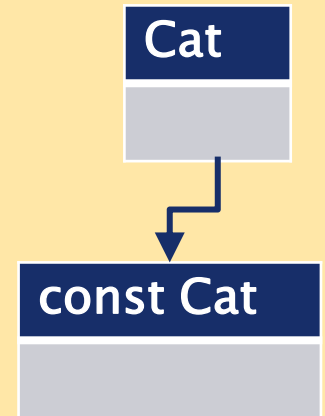
Read-only Array of Reference to Immutable Cat

```
Cat const *const *cats = ...
```

Covariance in C++

- ▶ 'T *const *' is covariant w.r.t. const/volatile...

```
void writeToXml(Cat const *const *cats, size_t num)
{
    for (size_t j = 0; j < num; j++)
    {
        Cat const *cat = cats[j];
        cat->serialise(std::cout);
    }
}
```



```
Cat *const *cats = ...;
writeToXml(cats, num);
```

Covariance in C++

```
class Cat : public Animal
```

```
{
```

```
public:
```

```
int age() const = 0;
```

```
void serialise(std::ostream &) const = 0;
```

```
void feed() = 0;
```

```
};
```

Cat

void feed();

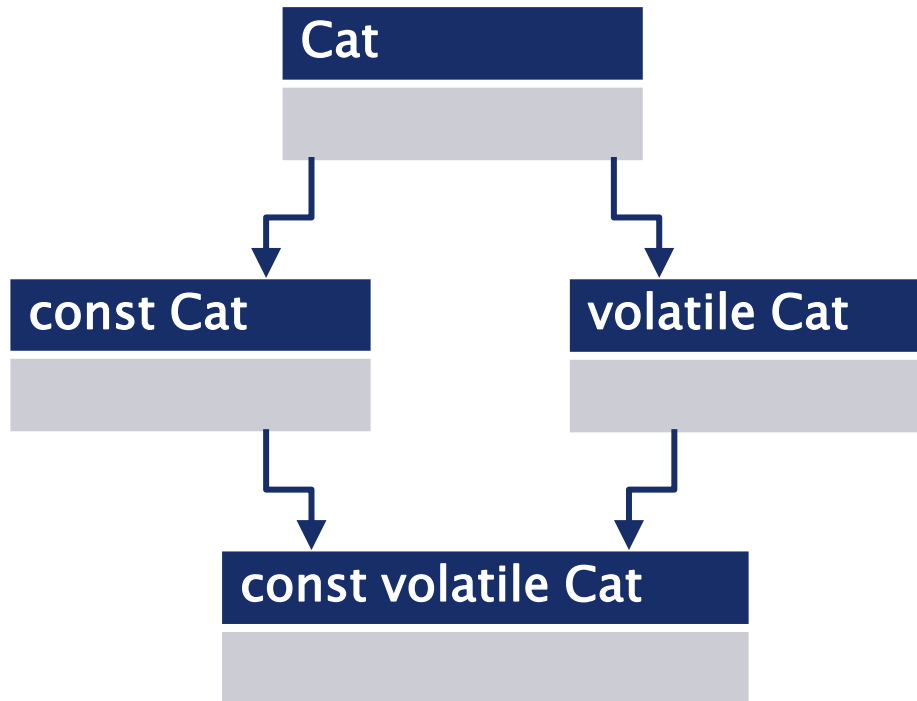
const Cat

int age();

void serialise(std::ostream &os);

Covariance in C++

- ▶ The limit of its extensibility:



A Type System with Variance

A Type System with Variance

- ▶ Requirements:
 - List<Tiger> is a sub-type of List<Cat>
 - Type-safe

```
List<Cat> cats = ...;
```

```
a = cats.f(b); // cats may be List<Tiger>.
```

- ▶ Deduce conditions on List, for this to be valid

Method Variance

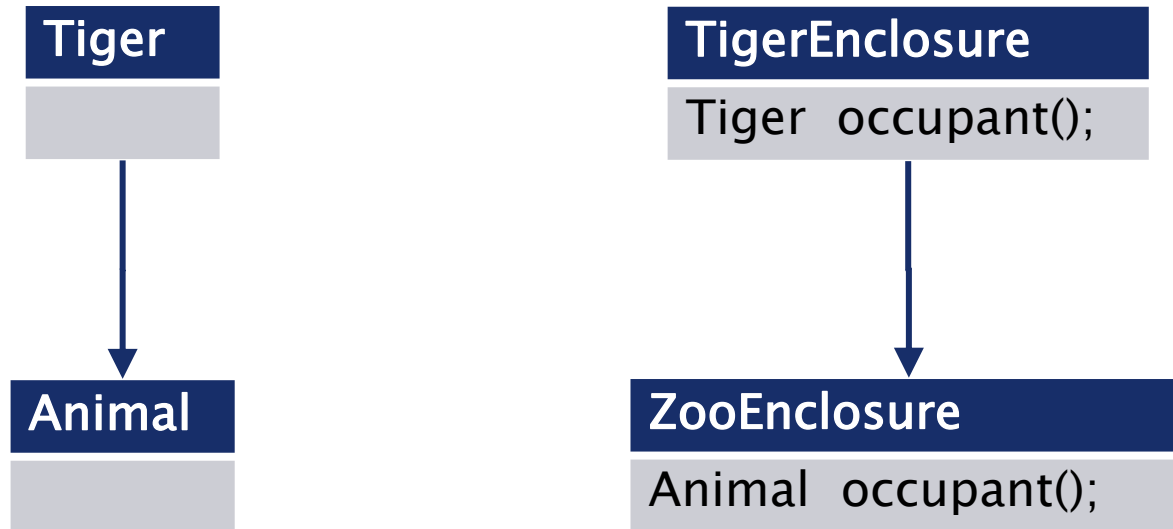
```
List<Cat> cats = ...;

try {
    a = cats.f(b); // cats may be List<Tiger>
} catch (E) {...}
```

- ▶ Invoking a method without complete knowledge of its run-time implementation's:
 - Return type
 - Argument types
 - Checked exception types

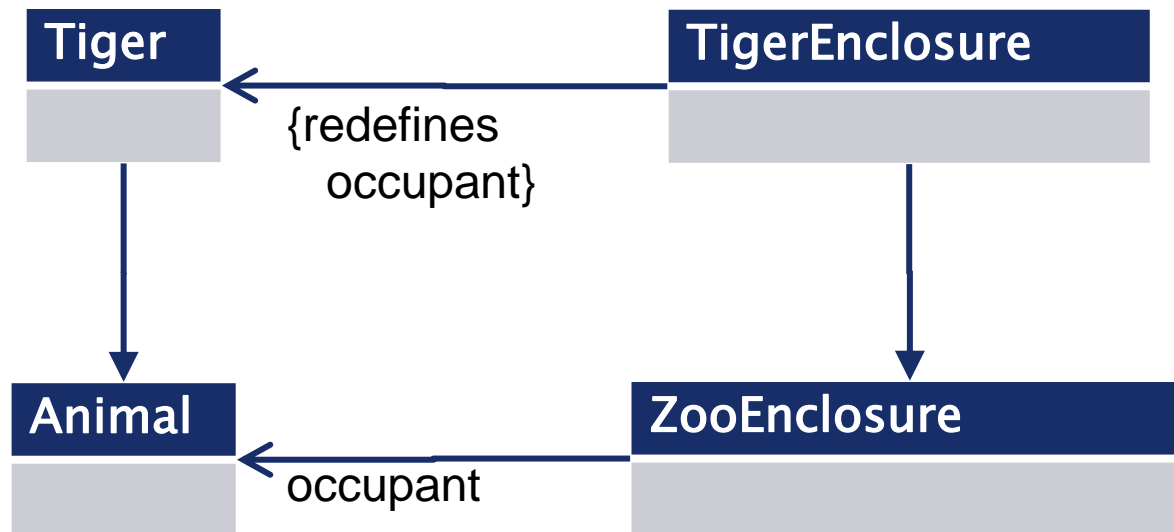
Method Variance

- ▶ Precedent: Covariant return type



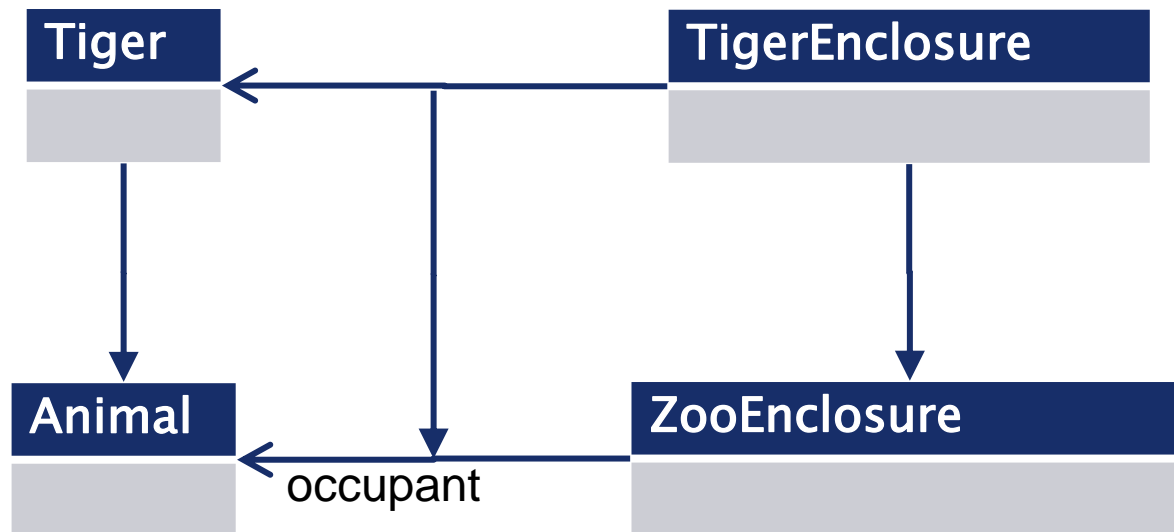
Method Variance

- ▶ Covariant return type in UML



Method Variance

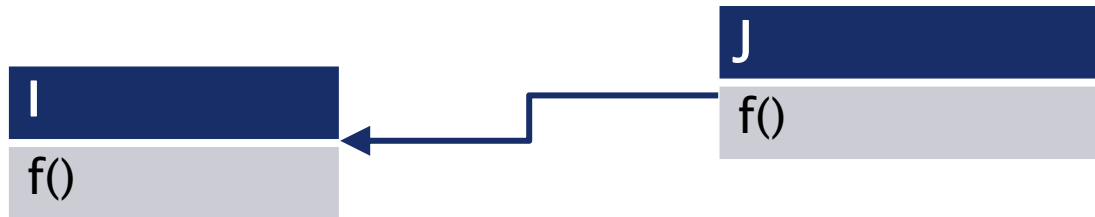
- ▶ Covariant return type in UML
 - Association specialisation



Method Variance

▶ Under-promise

▶ Over-deliver

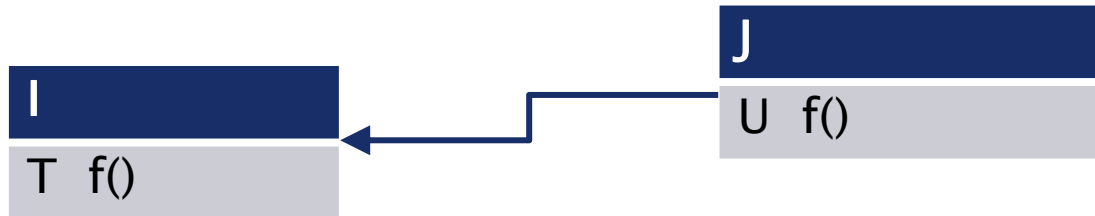


```
I i = ...;  
  
try {  
    a = i.f(b); // i may be a J.  
} catch (E) {...}
```

Covariance of Return Type

▶ Under-promise

▶ Over-deliver



```
I i = ...;
```

```
T a = i.f();
```

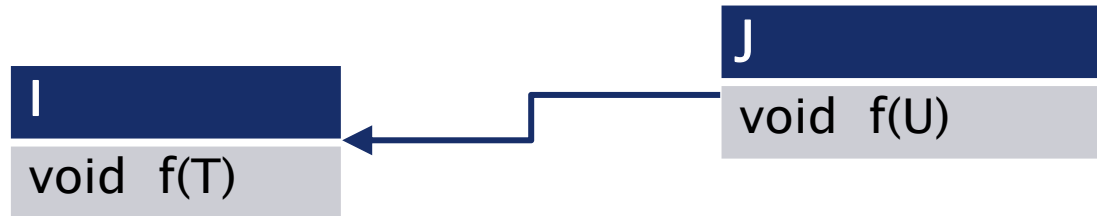
```
if  
  J <: I  
then  
  ret-type(J.f) <: ret-type(I.f)
```

```
ret-type(J.f) covariant w.r.t. J
```

Contravariance of Argument Type

▶ Under-promise

▶ Over-deliver



```
I i = ...;
```

```
T b = ...;  
i.f(b);
```

if

$J <: I$

then

$\text{arg-type}_n(J.f) \text{ :> } \text{arg-type}_n(I.f)$

$\text{arg-type}_n(J.f)$ contravariant w.r.t. J

Covariance of Checked Exception Type

▶ Under-promise

```
I  
void f() throws E
```

▶ Over-deliver

```
J  
void f() throws F
```

```
I i = ...;  
  
try {  
    i.f();  
} catch (E) {...}
```

```
if  
    J <: I  
then  
    throws-type(J.f) <: throws-type(I.f)
```

```
throws-type(J.f) covariant w.r.t. J
```

Method Variance Examples

▶ Under-promise

ZooEnclosure
Animal occupant()

TigerVeterinarian
void treat(Tiger)

InputStream
int read()
throws IOException

▶ Over-deliver

TigerEnclosure
Tiger occupant()

ÜberVeterinarian
void treat(Animal)

ByteArrayInputStream
int read()

Back to Generics ...

Covariant Interface

- ▶ List<T> covariant w.r.t. T
- ▶ For each method f:

```
if  
  U <: T  
then  
  List[U] <: List[T]  
so  
  ret-type(List[U].f) <: ret-type(List[T].f)
```

```
ret-type(List[T].f) covariant w.r.t. T
```

Covariant Interface

- ▶ List<T> covariant w.r.t. T
- ▶ For each method f, for the n^{th} argument:

```
if  
  U <: T  
then  
  List[U] <: List[T]  
so  
  arg-typen(List[U].f) :=> arg-typen(List[T].f)
```

```
arg-typen(List[T].f) contravariant w.r.t. T
```

Covariant Interface

When declaring List[T] to be covariant w.r.t. T:

for each method f in List

ret-type(f) covariant w.r.t. T

arg-type_n(f) contravariant w.r.t. T

for each immediate super-type J of List[T]

J covariant w.r.t. T

Covariant Interface

```
interface List<co T>
{
    int size();
    T elementAt(int index);
    List<T> clone();
    List<List<T>> chunks(int chunkSize);
    void sendTo(Collector<T> collector);
    void set(int index, T value);
    void appendAll(List<T> values);
    Collector<T> appender();
}
```

for each method f in List
ret-type(f) covariant w.r.t. T
arg-type _{n} (f) contravariant w.r.t. T

for each immediate super-type J of List[T]
 J covariant w.r.t. T

Contravariant Interface

- ▶ `Collector<T>` contravariant w.r.t. `T`
- ▶ For each method `f`:

```
if  
  U <: T  
then  
  Collector[U] :=> Collector[T]  
so  
  ret-type(Collector[U].f) :=> ret-type(Coll'r[T].f)
```

```
ret-type(Collector[T].f) contravariant w.r.t. T
```

Contravariant Interface

- ▶ $\text{Collector}\langle T \rangle$ contravariant w.r.t. T
- ▶ For each method f :

```
if  
   $U <: T$   
then  
   $\text{Collector}[U] := \text{Collector}[T]$   
so  
   $\text{arg-type}_n(\text{Collector}[U].f) <: \text{arg-type}_n(\text{Coll'r}[T].f)$ 
```

```
 $\text{arg-type}_n(\text{Collector}[T].f)$  covariant w.r.t.  $T$ 
```

Contravariant Interface

When declaring Collector[T] to be contravariant w.r.t. T:

for each method f in Collector
ret-type(f) contravariant w.r.t. T
arg-type_n(f) covariant w.r.t. T

for each immediate super-type J of Collector[T]
J contravariant w.r.t. T

Contravariant Interface

```
interface Collector<contra T>
{
    void accept(T item);
    void accept(List<T> items);
    Collector<T> clone();
    void donate(Collector<T> collector);
    T mostRecentItem();
    List<T> allItems();
}
```

for each method f in Collector
ret-type(f) contravariant w.r.t. T
arg-type_n(f) covariant w.r.t. T

for each immediate super-type J of Collector[T]
J contravariant w.r.t. T

Implementation in C#

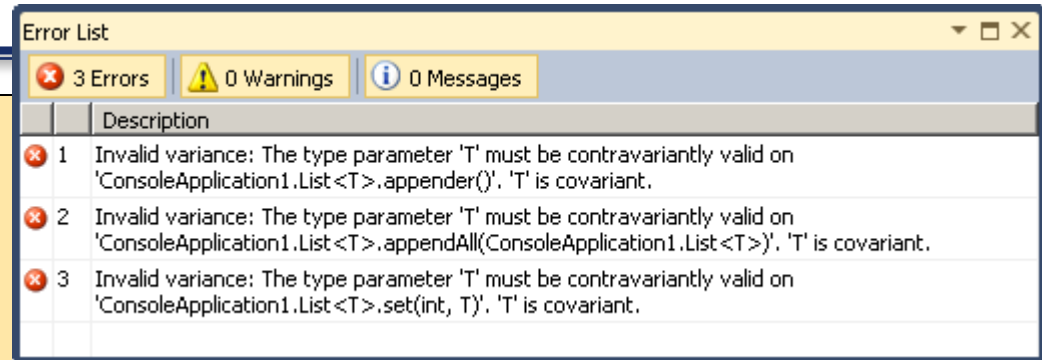
Implementation in C#

```
interface IEnumerator<out T>
{
    T Current { get; }
    void MoveNext();
}
```

```
interface IComparable<in T>
{
    int CompareTo(T other);
}
```

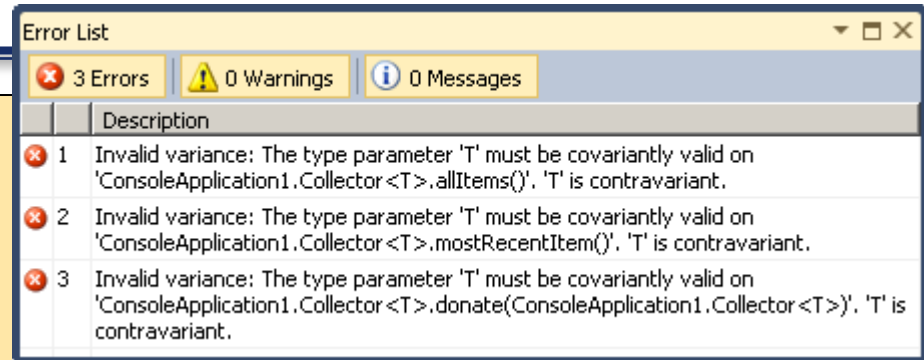
Implementation in C#

```
interface List<out T>
{
    int size();
    T elementAt(int index);
    List<T> clone();
    List<List<T>> chunks(int chunkSize);
    void sendTo(Collector<T> collector);
    void set(int index, T value);
    void appendAll(List<T> values);
    Collector<T> appender();
}
```

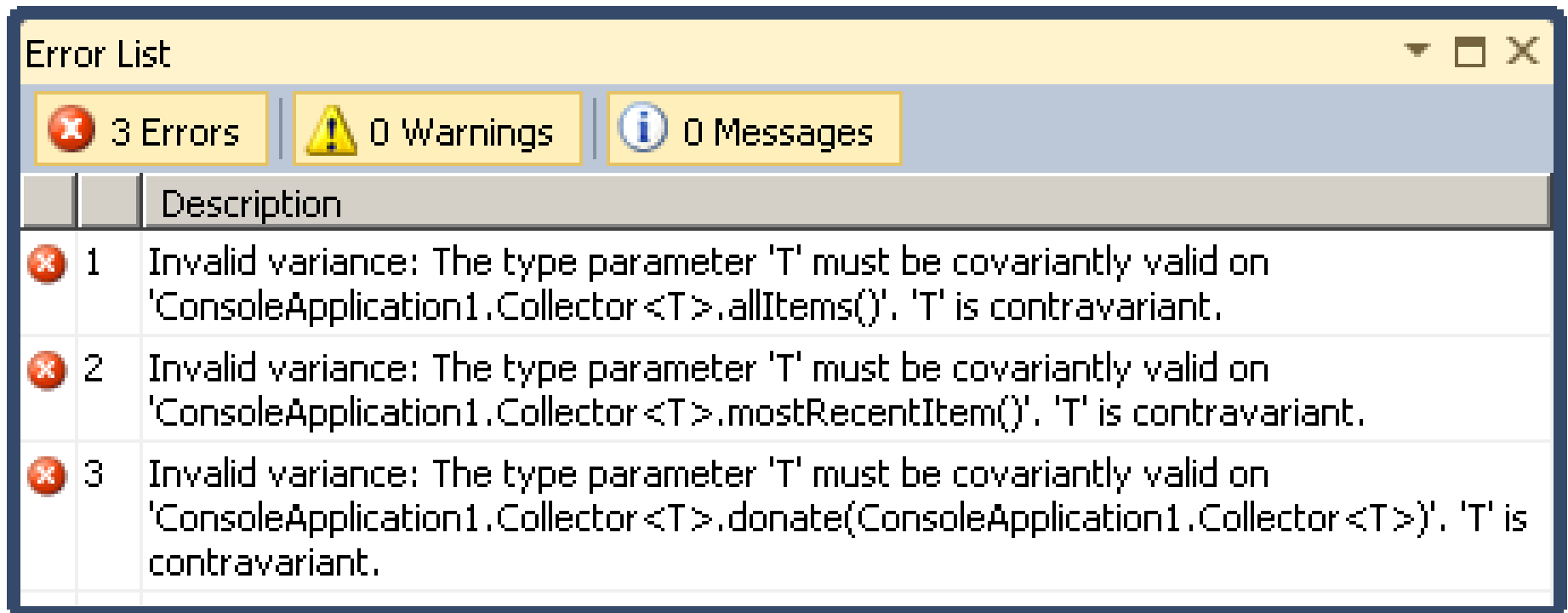


Implementation in C#

```
interface Collector<in T>
{
    void accept(T item);
    void accept(List<T> items);
    Collector<T> clone();
    void donate(Collector<T> collector);
    T mostRecentItem();
    List<T> allItems();
}
```



Implementation in C#



The screenshot shows an IDE window titled "Error List" with a yellow header bar. Below the header, there are three summary boxes: "3 Errors" (with a red 'x' icon), "0 Warnings" (with a yellow warning triangle icon), and "0 Messages" (with a blue information 'i' icon). The main area is a table with a "Description" column. It contains three error entries, each with a red 'x' icon in the first column.

	Description
1	Invalid variance: The type parameter 'T' must be covariantly valid on 'ConsoleApplication1.Collector<T>.allItems()'. 'T' is contravariant.
2	Invalid variance: The type parameter 'T' must be covariantly valid on 'ConsoleApplication1.Collector<T>.mostRecentItem()'. 'T' is contravariant.
3	Invalid variance: The type parameter 'T' must be covariantly valid on 'ConsoleApplication1.Collector<T>.donate(ConsoleApplication1.Collector<T>)'. 'T' is contravariant.

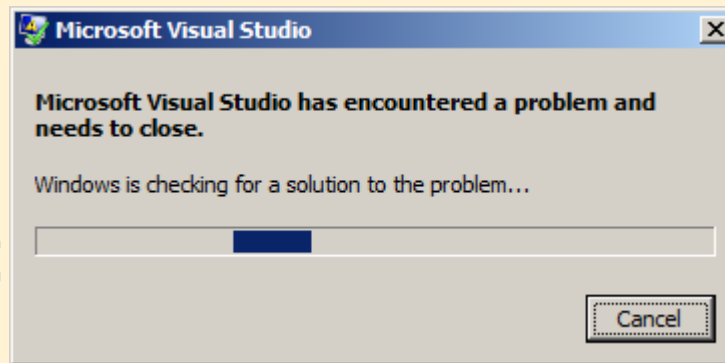
Determinism of Sub-Type

```
interface N<in Z> {}  
interface C : N<N<C>> {}  
...  
void f(C c)  
{  
    N<C> nc = c;  
}
```

Kennedy, A.J., Pierce, B.C. (2006). On Decidability of Nominal Subtyping with Variance, FOOL-WOOD '07.

Determinism of Sub-Type

```
interface N<in Z> {}  
interface C : N<N<C>> {}  
  
...  
void f(C c)  
{  
    N<C> nc = c;  
}
```



Kennedy, A.J., Pierce, B.C. (2006). On Decidability of Nominal Subtyping with Variance, FOOL-WOOD '07.

Determinism of Sub-Type

```
interface N[contra Z]  
interface C <: N[N[C]]
```

```
C <: N[C] ?
```

Kennedy, A.J., Pierce, B.C. (2006). On Decidability of Nominal Subtyping with Variance, FOOL-WOOD '07.

Determinism of Sub-Type

```
interface N[contra Z]  
interface C <: N[N[C]]
```

```
C <: N[C]  
is implied by  
N[N[C]] <: N[C]
```

Kennedy, A.J., Pierce, B.C. (2006). On Decidability of Nominal Subtyping with Variance, FOOL-WOOD '07.

Determinism of Sub-Type

```
interface N[contra Z]  
interface C <: N[N[C]]
```

```
C <: N[C]  
is implied by  
N[N[C]] <: N[C]  
is implied by  
N[C] :> C
```

Kennedy, A.J., Pierce, B.C. (2006). On Decidability of Nominal Subtyping with Variance, FOOL-WOOD '07.

A large, dark blue curved shape that starts from the bottom left and curves upwards and to the right, filling the bottom right portion of the slide.

Implementation in Java

Covariance in Java

- ▶ If an API expects a list of cats ...

```
void writeToXml(List<Cat> cats);
```

- ▶ ... then we'd expect it to accept a list of tigers ...

```
List<Tiger> tigers = ...;  
writeToXml(tigers);
```

Covariance in Java

- ▶ How can we make the API general?

```
void writeToXml(List<Cat> cats);
```

Covariance in Java

- ▶ How can we make the API general?

```
void writeToXml(List<Cat> cats);  
void writeToXml(List<Tiger> cats);
```

Covariance in Java

- ▶ How can we make the API general?

```
void writeToXml(List<Cat> cats);  
void writeToXml(List<Tiger> cats);  
void writeToXml(List<Lion> cats);  
...  
void writeToXml(List<Ocelot> cats);
```


Covariance in Java

- ▶ How can we make the API general?

```
<T extends Cat>  
void writeToXml(List<T> cats);
```

Covariance in Java

- ▶ How can we make the API general?

```
<T extends Cat>  
void writeToXml(List<T> cats);
```

- ▶ Unsatisfactory: we don't do this:

```
<T extends Cat>  
void writeToXml(T cat);
```

Covariance in Java

- ▶ How can we make the API general?

```
void writeToXml(List<? extends Cat> cats);
```

- ▶ List<? extends T> is covariant w.r.t. T

Wildcard Types (Covariant)

```
void writeToXml(List<? extends Cat> cats);
```

- ▶ The Java compiler:
 - ▶ *allows* us to obtain Cat instances from “cats”
 - ▶ This is safe even if “cats” is List<Tiger>

```
Cat firstCat = cats.get(0);
```

- ▶ *forbids* us to give Cat instances to “cats”
 - ▶ This would be unsafe if “cats” is List<Tiger>

```
cats.add(new Lion());
```

Contravariance in Java

- ▶ How can we make the API general?

```
void donateMyTigers(List<Tiger> tigerCollector);  
void donateMyTigers(List<Cat> tigerCollector);  
void donateMyTigers(List<Animal> tigerCollector);  
void donateMyTigers(List<HasStripes> tigerCollector);  
void donateMyTigers(List<Object> tigerCollector);
```

Contravariance in Java

- ▶ How can we make the API general?

```
void donateMyTigers(List<? super Tiger> tigerCollector);
```

- ▶ List<? super T> is contravariant w.r.t. T

Wildcard Types (Contravariant)

```
void donateMyTigers(List<? super Tiger> tigerCollector);
```

- ▶ The Java compiler:
 - ▶ *allows* us to give Tiger instances to “tigerCollector”
 - ▶ This is safe even if “tigerCollector” is List<Cat>

```
tigerCollector.add(new Tiger());
```

- ▶ *forbids* us to obtain Cat instances from “cats”
 - ▶ This would be unsafe if “cats” is List<Animal>

```
Tiger firstTiger = tigerCollector.get(0);
```

Available Methods (Covariant)

```
interface List<T>
    extends Collection<T>
{
    int size();
    T get(int index);
    void add(int index, T item);
    Iterator<T> iterator();
    List<List<T>> chunks(int chunkSize);
}
```


Available Methods (Covariant)

```
interface List<? extends T>
    extends Collection<T>
{
    int size();
    T get(int index);
    void add(int index, T item);
    Iterator<T> iterator();
    List<List<T>> chunks(int chunkSize);
}
```

Available Methods (Covariant)

```
interface List$co<T> // List<? extends T>
    extends Collection<? extends T>
{
    int size();
    T get(int index);
    void add(int index, null-type item);
    Iterator<? extends T> iterator();
    List<List<capture#1-of-? extends T>>
        chunks(int chunkSize);
}
```

Available Methods (Contravariant)

```
interface List$contra<T> // List<? super T>
    extends Collection<? super T>
{
    int size();
    Object get(int index);
    void add(int index, T item);
    Iterator<? super T> iterator();
    List<List<capture#1-of-? super T>>
        chunks(int chunkSize);
}
```

Implicit Interfaces

ArrayList<T>

constructors



List<T>

int size();
T get(int index);
void add(int index, T item);
Iterator<T> iterator();



List\$co<T> // List<? extends T>

int size();
T get(int index);
Iterator<? extends T> iterator();



List\$contra<T> // List<? super T>

int size();
void add(int index, T item);

Implicit Interfaces

ArrayList<T>

constructors



List<T>

int size();
T get(int index);
void add(int index, T item);
Iterator<T> iterator();

read-only list

List\$co<T> // List<? extends T>

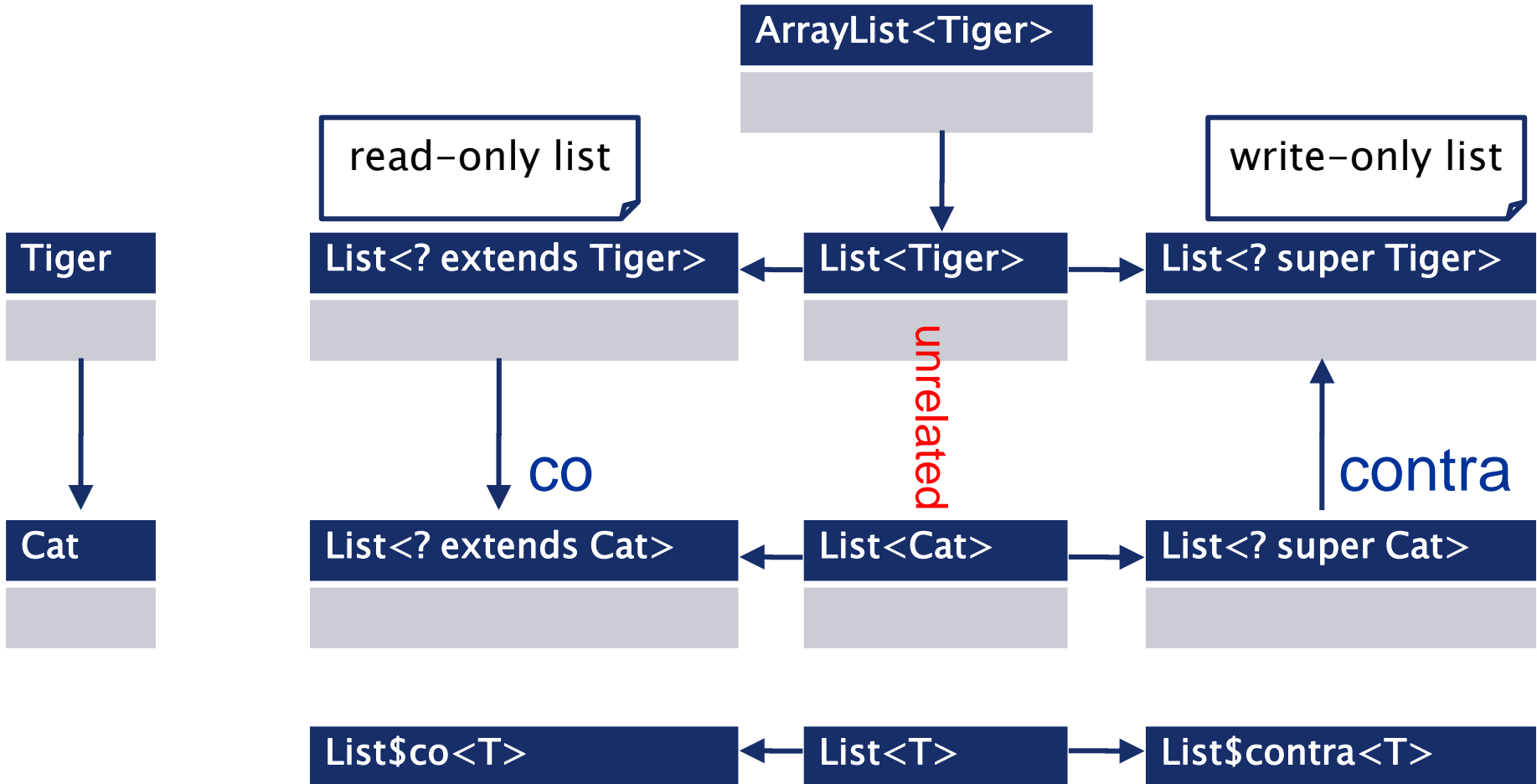
int size();
T get(int index);
Iterator<? extends T> iterator();

write-only list

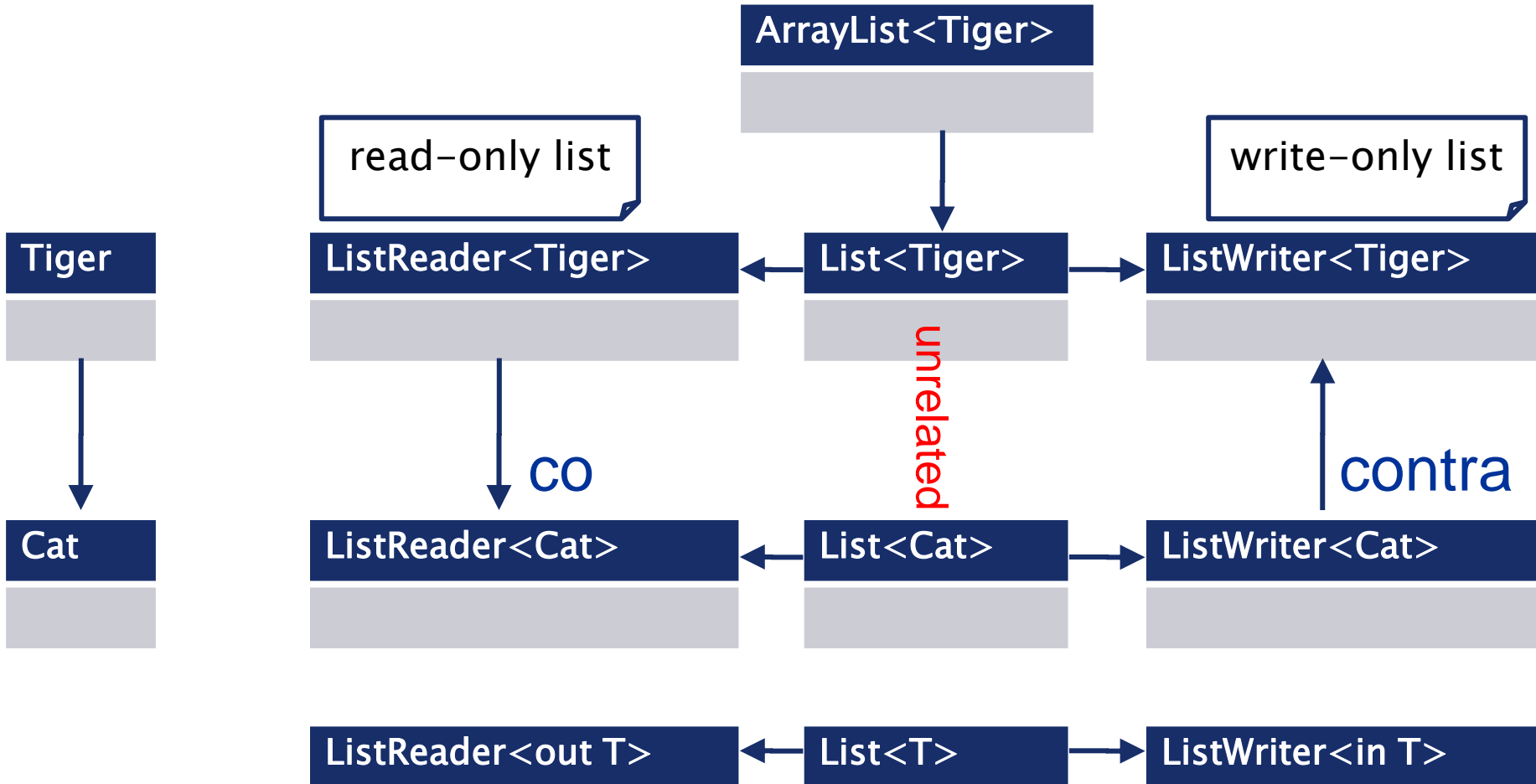
List\$contra<T> // List<? super T>

int size();
void add(int index, T item);

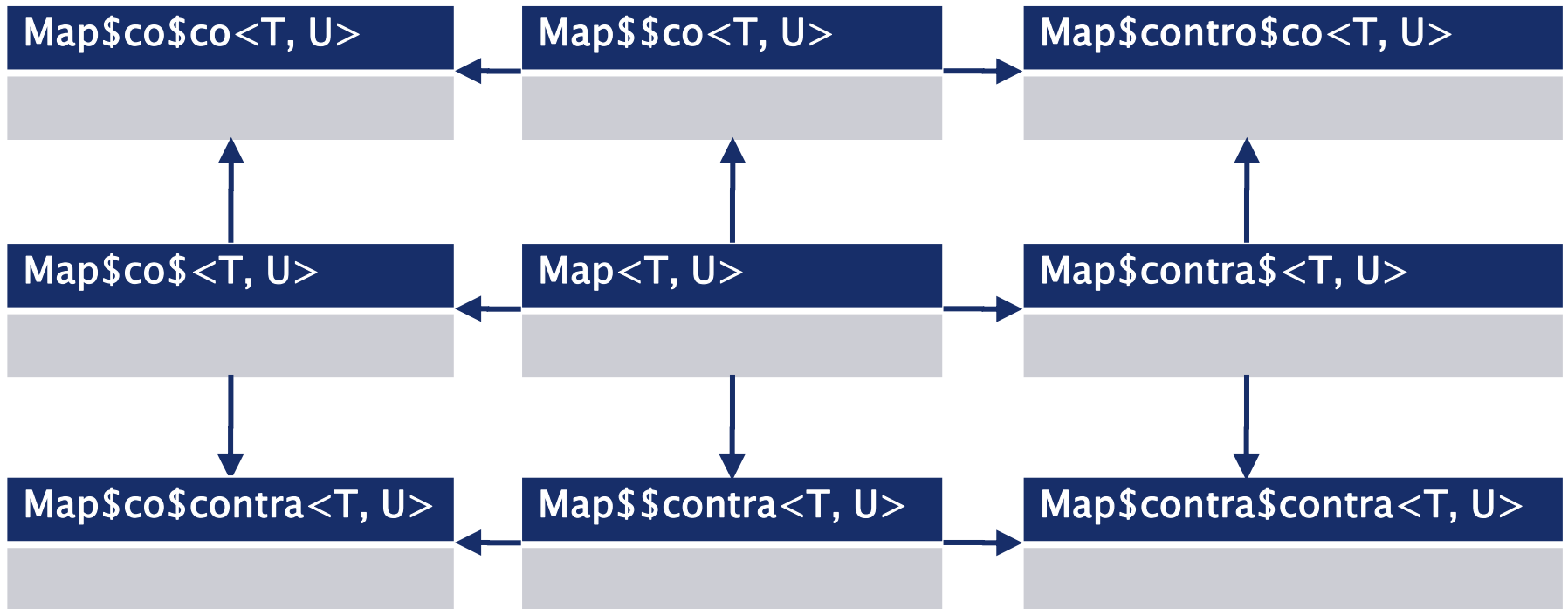
Covariance and Contravariance



Covariance and Contravariance in C#



Multiple Type Parameters



Wildcard vs Variant Interface

- ▶ Wildcard perspective:

List < ? extends T >



- ▶ Variant Interface perspective:

List<?extends T>
List\$co<T>

- ▶ “List of some sub-type of T”

- ▶ “Covariant list of T”

Implementation Hiding

```
interface Car
{
    ArrayList<Wheel> wheels();
}
```

Implementation Hiding

```
interface Car  
{  
    Array<Wheel> wheels();  
}
```

```
interface Car  
{  
    List<Wheel> wheels();  
}
```

Implementation Hiding

```
interface Car  
{  
    Array<Wheel> wheels();  
}
```

```
interface Car  
{  
    List<Wheel> wheels();  
}
```

```
interface Car  
{  
    List<? extends Wheel> wheels();  
}
```

Documentation Aid

```
/**  
 * @return      car's wheels  
 */  
List<Wheel> wheels()  
{  
    return this.wheels;  
}
```

Documentation Aid

```
/**  
 * @return          car's wheels;  
 *                  please don't modify  
 */  
List<Wheel> wheels()  
{  
    return this.wheels;  
}
```

Documentation Aid

```
/**  
 * @return      car's wheels;  
 *              please don't modify  
 *              pretty please  
 */  
List<Wheel> wheels()  
{  
    return this.wheels;  
}
```

Documentation Aid

```
/**
 * @return      car's wheels;
 *              please don't modify
 *              (actually, don't bother trying)
 */
List<Wheel> wheels()
{
    return Collections.unmodifiableList(
        this.wheels);
}
```


Documentation Aid

```
/**  
 * @return      car's wheels  
 */  
List<? extends Wheel> wheels()  
{  
    return this.wheels;  
}
```

Declaration-Site vs Use-Site Variance

- ▶ Declaration-Site Variance

```
interface List<out T>
```

```
{
```

```
    interface Collector<in T>
```

```
    {
```

```
        ...
```

```
    }
```

- ▶ Use-Site Variance

```
List<? extends Cat>
```

```
List<? super Cat>
```

Limitations of Use-Site Variance

- ▶ Cannot inherit from a variant type

```
class ListDecorator<T>
    implements List<? extends T>
{
    private final List<? extends T> target;
    ...
    public Iterator<? extends T> iterator()
    {
        return target.iterator();
    }
}
```

Limitations of Use-Site Variance

- ▶ Cannot inherit from a variant type

```
class ListDecorator<T>
    implements List<T>
{
    private final List<? extends T> target;
    ...
    public Iterator<T> iterator()
    {
        return target.iterator();
    }
}
```

Reading Types

```
public static <T>  
int binarySearch(  
    List<? extends Comparable<? super T>> list,  
    T key)  
{...}
```

```
public static <T>  
int binarySearch(  
    List$co<Comparable$contra<T>> list,  
    T key)  
{...}
```

Questions



Questions

? extends